

Laws of Motion

Force

- ① Gravitational Force
- ② Electromagnetic Force
- ③ Strong Nuclear Force
- ④ Weak Nuclear Force

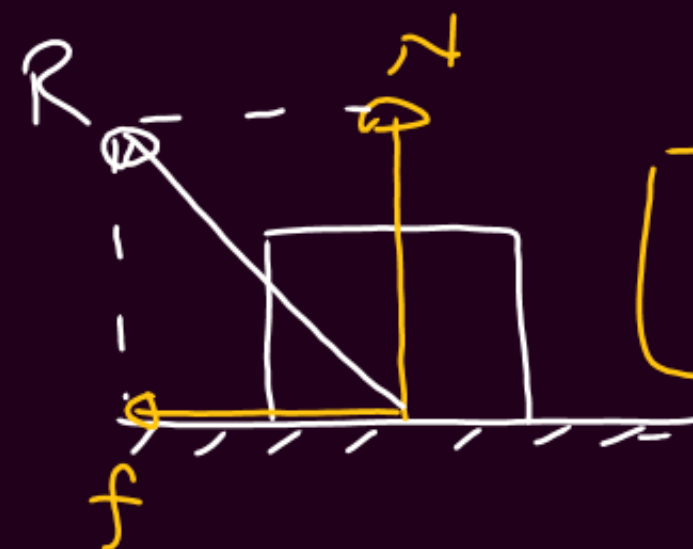
$$GF < WF < EMF < SF$$

$$F = 2g = 20\text{ N}$$
$$= 2\text{ kg-wt}$$

① mg (weight) Vertically Downwards

② Tension in String (T) Towards the string

③ Contact / Reaction Force



$$R = \sqrt{N^2 + f^2}$$

→ Normal Reaction (N) → Towards the object
"Component of R $\perp$ to surface"

→ Friction "Component of R along the surface"

④ Spring

$$F = -kx$$



(Elongation)

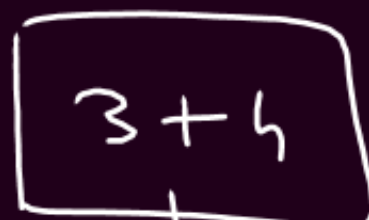
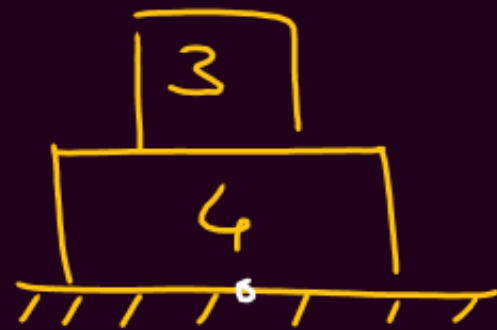


(Compression)

Equilibrium $\vec{F}_{net} = 0$

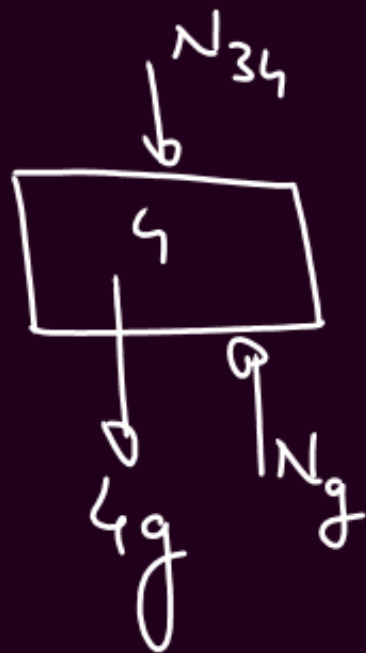
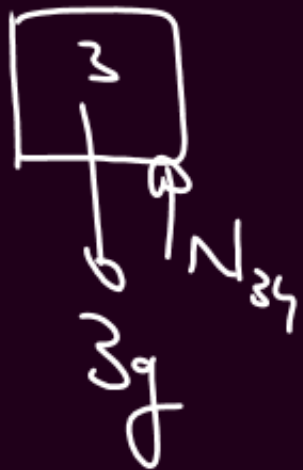


$$N = 5g$$



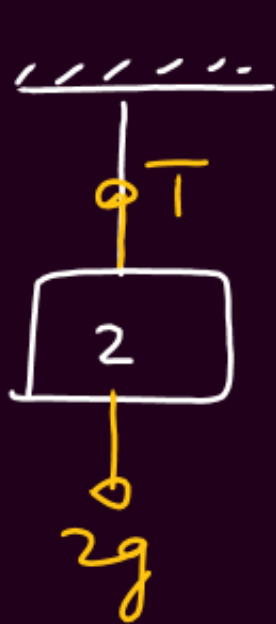
$$N_g = (3+4)g$$

$$N_{34} = 3g$$

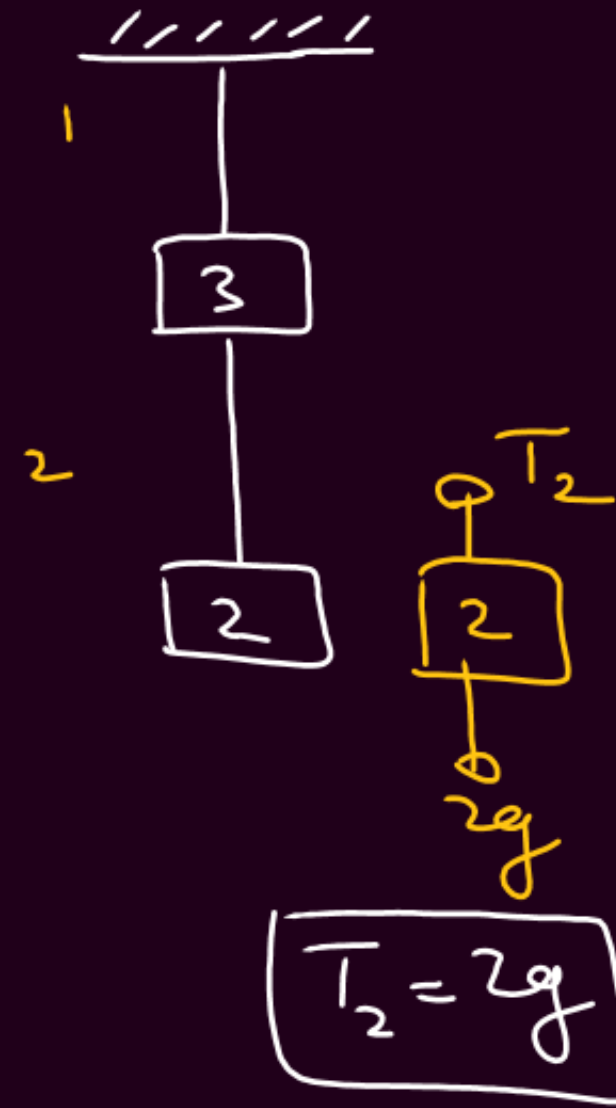


$$N_g = 4g + N_{34}$$

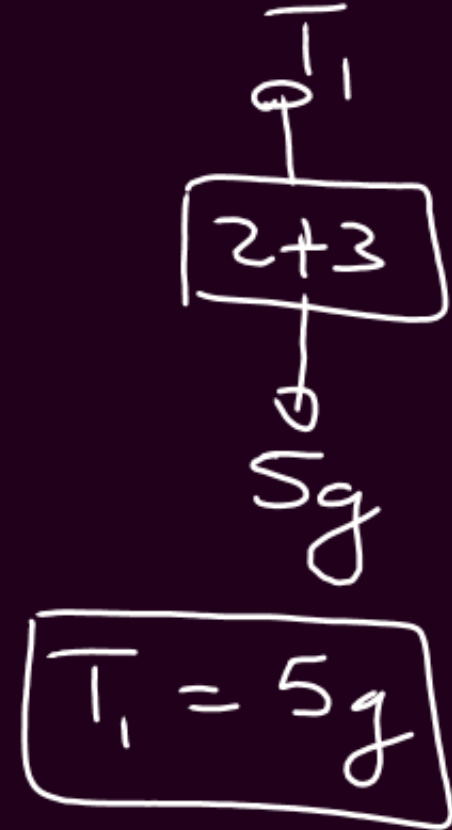
Ideal String $\rightarrow$ massless $\rightarrow$ inextensible (T same at all points)



$$T = 2g$$



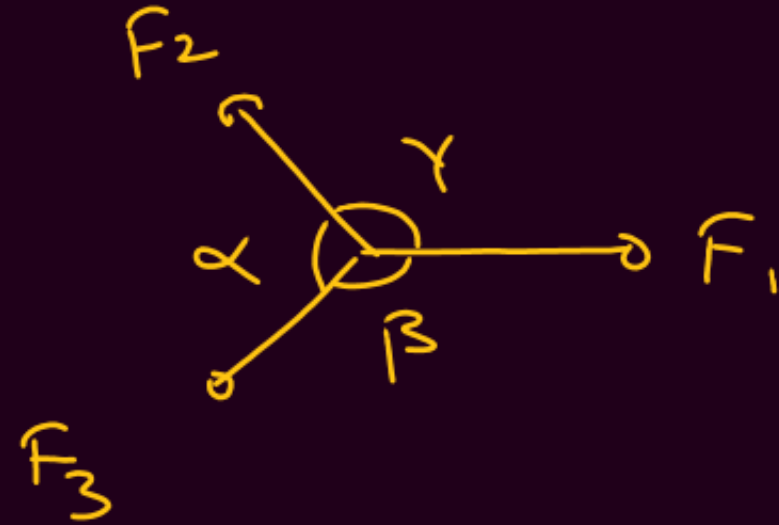
$$T_2 = 2g$$



$$T_1 = 5g$$

Lami's Theorem

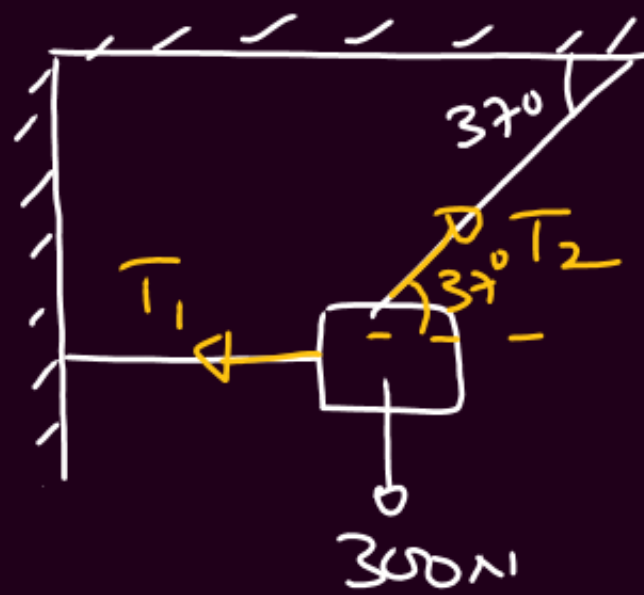
$$\rightarrow \vec{F}_1 + \vec{F}_2 + \vec{F}_3 = 0$$



$$\frac{F_1}{\sin \alpha} = \frac{F_2}{\sin \beta} = \frac{F_3}{\sin \gamma}$$

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(3)



$$\frac{T_1}{\sin(90^\circ + 37^\circ)} = \frac{T_2}{\sin 90^\circ} = \frac{300}{\sin(180^\circ - 37^\circ)}$$

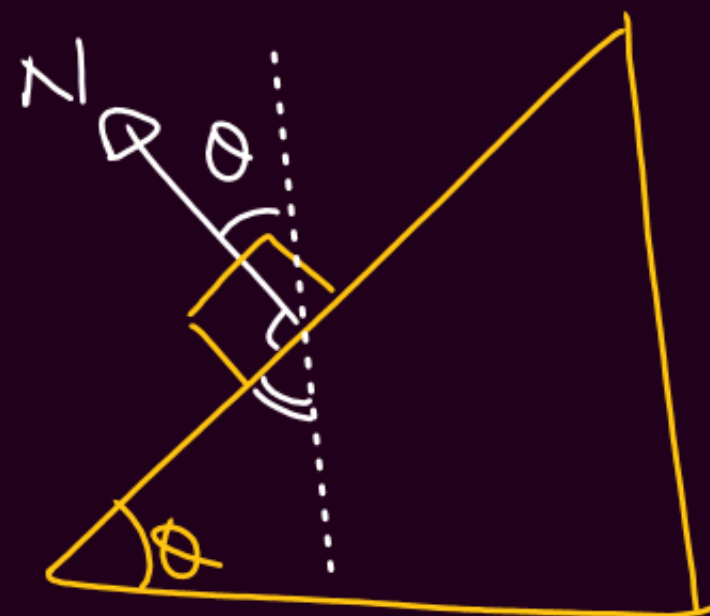
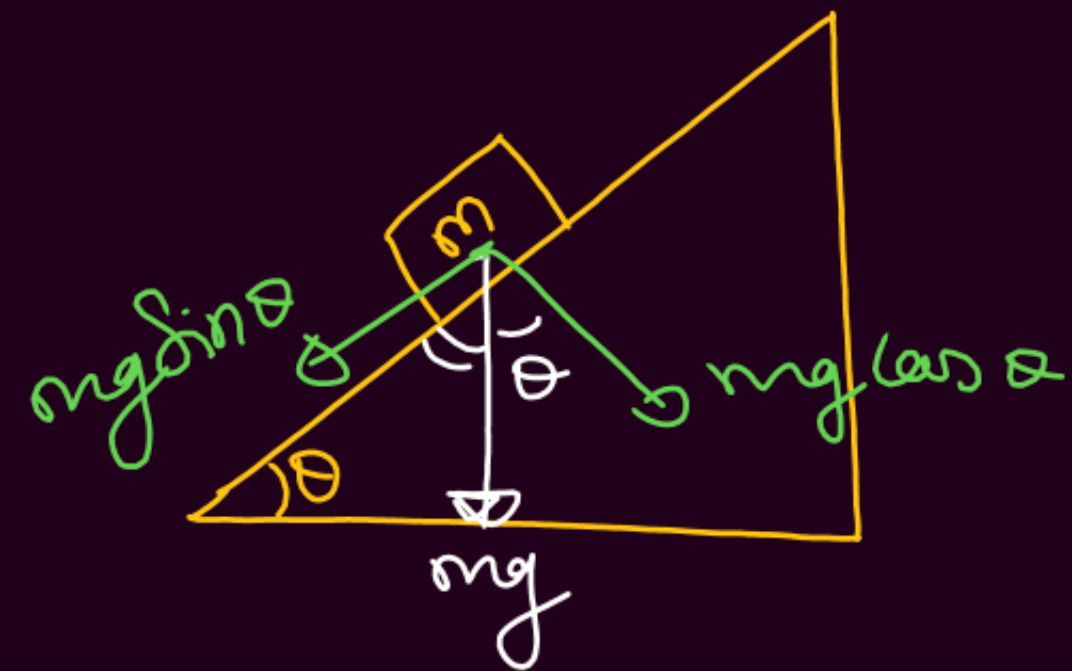
$$\frac{T_1}{\cos 37^\circ} = \frac{T_2}{1} = \frac{300}{\sin 37^\circ}$$

$$\frac{T_1}{4/5} = T_2 = \frac{300}{3/5}$$

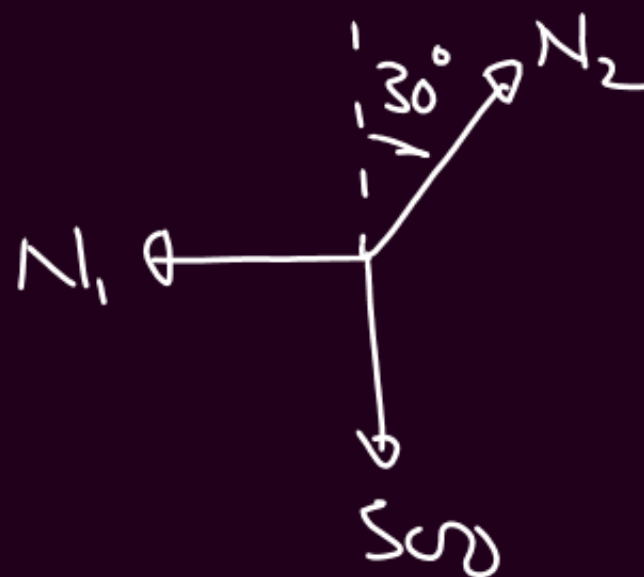
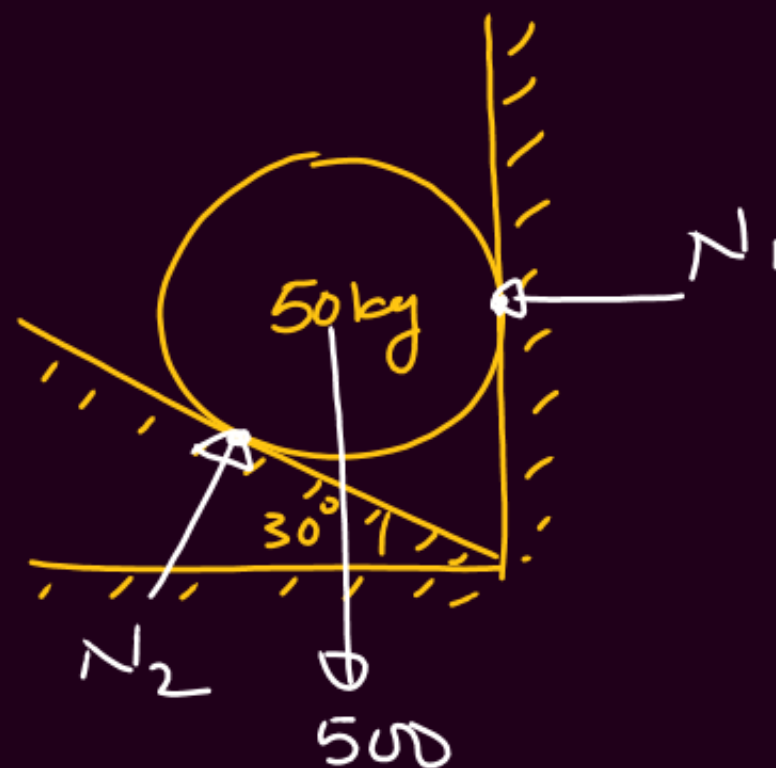
$$T_1 = 400 \text{ N}$$

$$T_2 = 500 \text{ N}$$

Inclined Plane



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(2)



$$\frac{N_1}{\sin(180^\circ - 30^\circ)} = \frac{N_2}{\sin(90^\circ)} = \frac{500}{\sin(90^\circ + 30^\circ)}$$

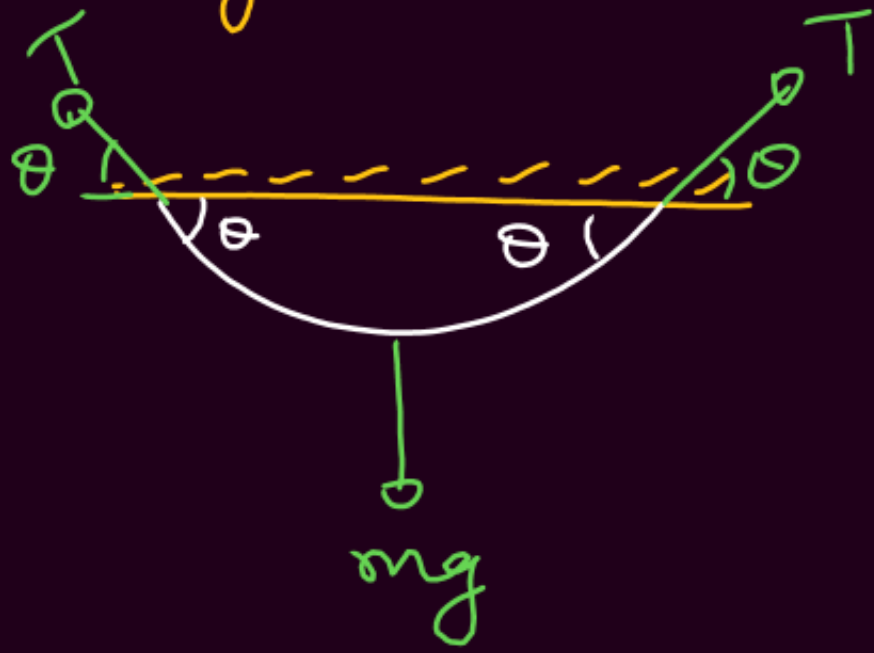
$$\frac{N_1}{\sin 30^\circ} = \frac{N_2}{1} = \frac{500}{\cos 30^\circ}$$

$$\frac{N_1}{1/2} = N_2 = \frac{500}{\sqrt{3}/2}$$

$$N_1 = \frac{500}{\sqrt{3}} \text{ N}$$

$$N_2 = \frac{1000}{\sqrt{3}} \text{ N}$$

Heavy Rope

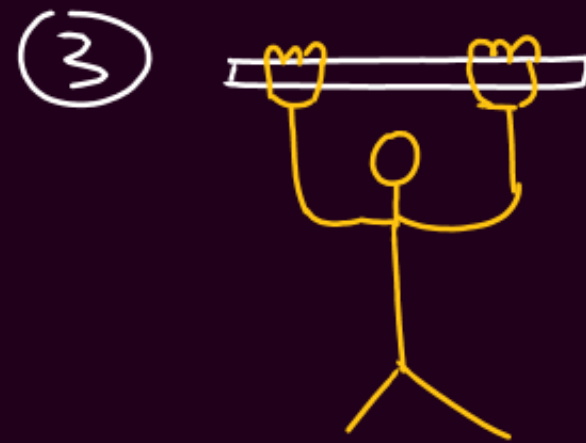


$$2T \sin \theta = mg$$

$$\theta \rightarrow 0 \quad T \rightarrow \infty$$

① F req. to keep a rope horizontal is ∞

② It is impossible to keep the rope horizontal



To have min strain
[Arms must be parallel]

Newton's Laws of Motion

① 1st Law (Law of Inertia)

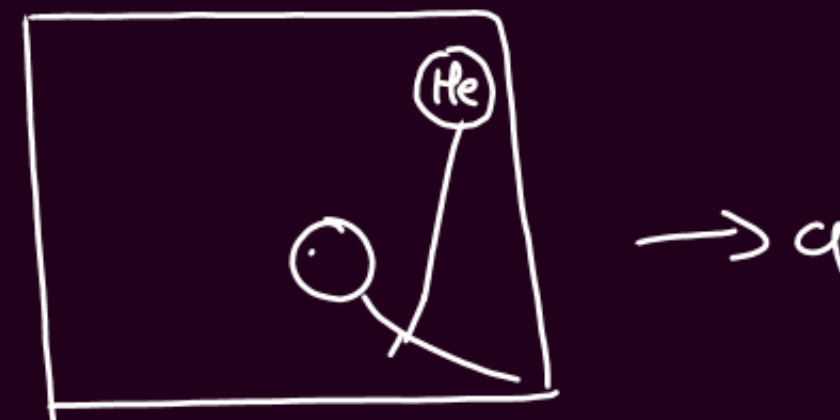
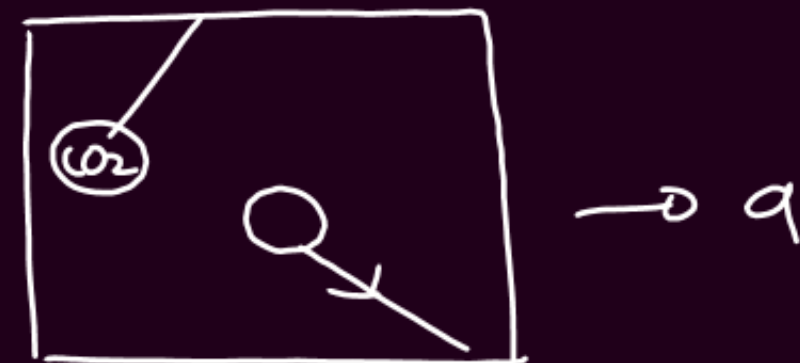
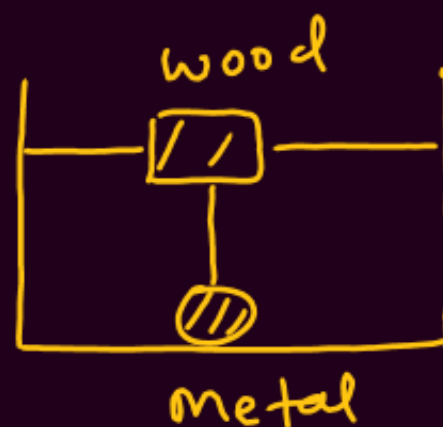
Rest $\rightarrow$ Rest
 Motion $\rightarrow \vec{v} = \text{const}$ } until $\vec{F}_{\text{ext}}$

[if $\vec{F}_{\text{ext}} = 0$ then $\vec{v} = \text{const}$
 & vice versa]

Inertia $\rightarrow$ Opposes the change in $\vec{v}$

$\rightarrow$ Proportional to mass

$\rightarrow$ Rest
 $\rightarrow$ motion
 $\rightarrow$ direction



slowly ②
 sudden ①



Momentum $\vec{p} = m \vec{v}$

$$K = \frac{1}{2} m v^2 = \frac{p^2}{2m}$$

$$p = \sqrt{2mk}$$

2nd Law

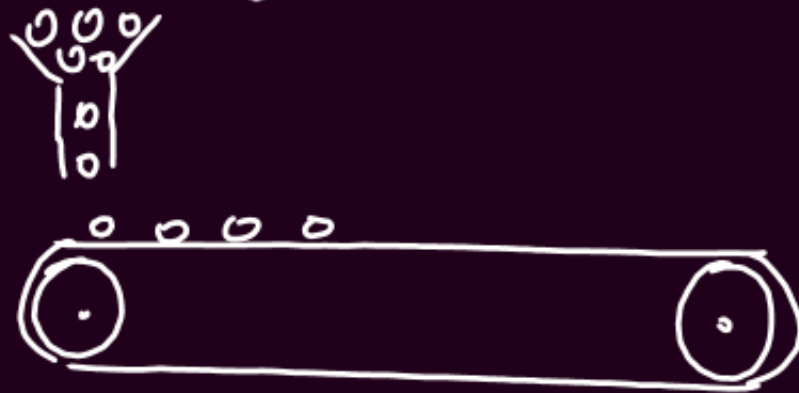
$$\vec{F}_{\text{ext}} = \frac{d\vec{p}}{dt}$$

$$F_{av} = \frac{\Delta p}{\Delta t}$$

① if $m = \text{const.}$ $F = m a$

② $m = \text{variable}$
 $v = \text{const.}$ $F = v \frac{dm}{dt}$

Conveyer Belt



$$F = v \frac{dm}{dt}$$

$$F = (5)(2) = 10 \text{ N}$$

Q. $\vec{F} = (3\hat{i} - 4\hat{j} + 5\hat{k}) \text{ N}$

$$m = 5 \text{ kg}$$

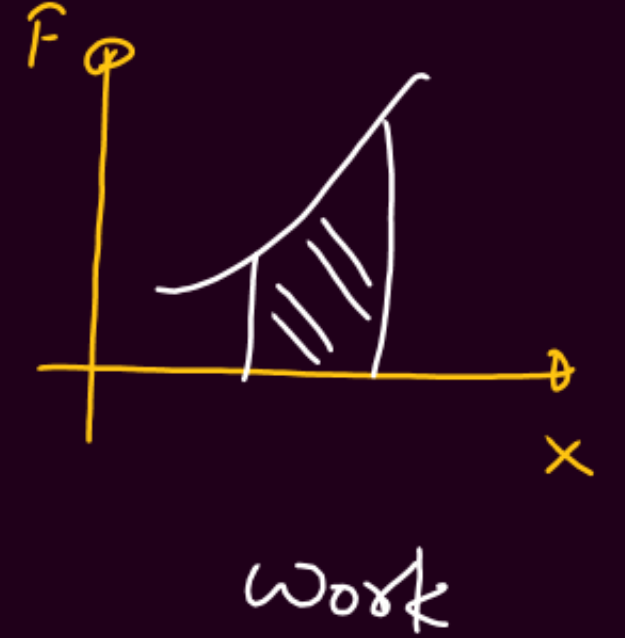
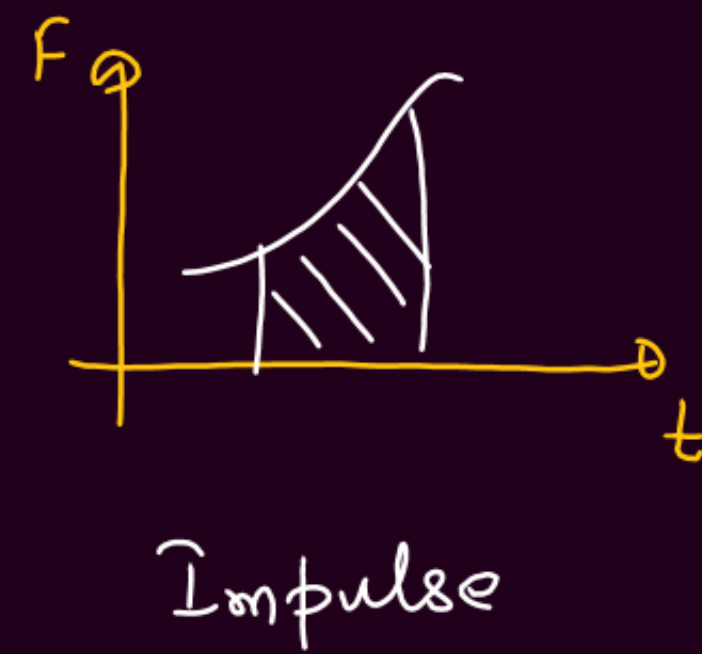
mag. of acc. ?

$$a = \frac{F}{m} = \frac{\sqrt{3^2 + 4^2 + 5^2}}{5} = \frac{5\sqrt{2}}{5} = \sqrt{2} \text{ m/s}^2$$

Impulse. $\Delta \vec{p} = m(\vec{v}_2 - \vec{v}_1) = \int \vec{F} dt$

→ large force
↳ shorter period

Gravitational } non-impulsive
Spring }



	General / Inelastic	Perfectly Inelastic	<u>Elastic</u>	
			Normal incidence	oblique
Change in Vel.	 $(v_2 + v_1)$	 v	 $2v$	 $2v \cos \theta$
Avg. Acc.	$a_{av} = \frac{v_2 + v_1}{t}$	$a_{av} = \frac{v}{t}$	$a_{av} = \frac{2v}{t}$	$a_{av} = \frac{2v \cos \theta}{t}$
Avg. Force	$F_{av} = \frac{m(v_2 + v_1)}{t}$	$F_{av} = \frac{mv}{t}$	$F_{av} = \frac{2mv}{t}$	$F_{av} = \frac{2mv \cos \theta}{t}$
				<u>Deviation</u> $\delta = 180^\circ - 2\theta$

Q. Dropped 20m
Same height

$$\Delta t = 0.2 \text{ s}$$

then $a_{av} = ?$

$$v = \sqrt{2(10)(20)} = 20 \text{ m/s}$$

$$a_{av} = \frac{2v}{\Delta t} = \frac{2 \times 20}{0.2} = 200 \text{ m/s}^2$$

Q/P

Q. Dropped 45m to 20m

$$m = 2 \text{ kg}$$

$$\Delta t = 0.5 \text{ s}$$

$$v_1 = \sqrt{2(10)(45)} = 30 \text{ m/s}$$

$$v_2 = \sqrt{2(10)(20)} = 20 \text{ m/s}$$

① Impulse

$$\Delta p = m \Delta v = (2) [30 + 20] = 100 \text{ N-s}$$

$$\textcircled{2} F_{av} = \frac{\Delta p}{\Delta t} = \frac{100}{0.5} = 200 \text{ N}$$

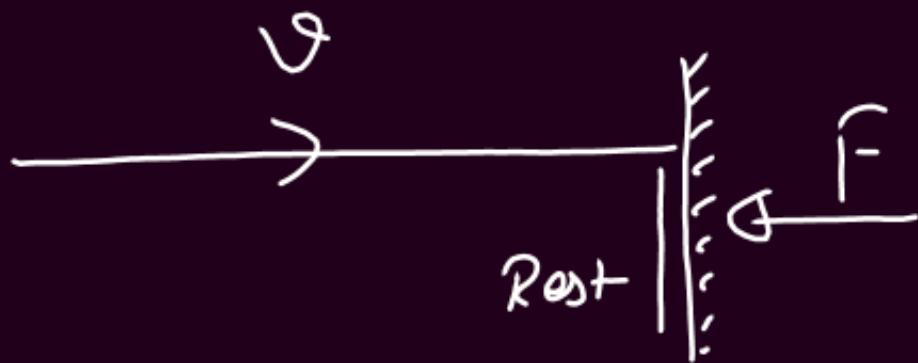
Fluid

① Vol. flow Rate

$$\boxed{\frac{dV}{dt} = A v}$$

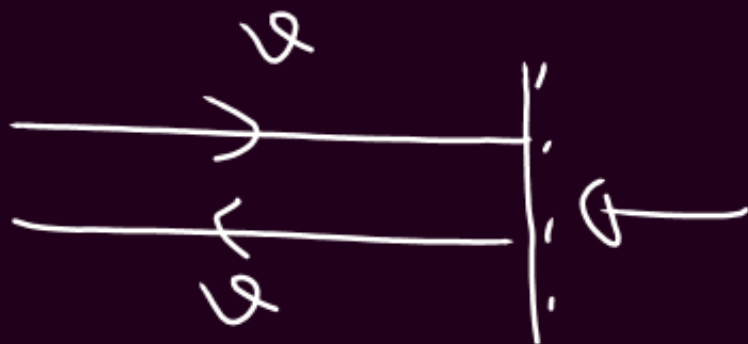
② Mass flow rate

$$\boxed{\frac{dm}{dt} = \rho A v}$$



$$F = v \frac{dm}{dt}$$

$$\boxed{F = \rho A v^2}$$



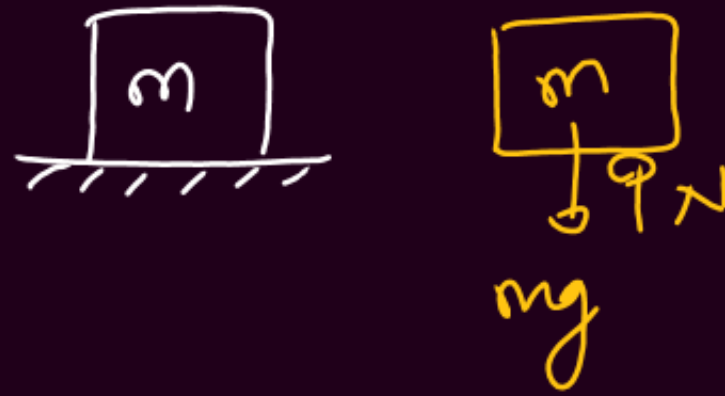
$$\boxed{F = 2 \rho A v^2}$$

force req. to hold the plate

Newton's 3rd Law

$$\vec{F}_{BA} = -\vec{F}_{AB}$$

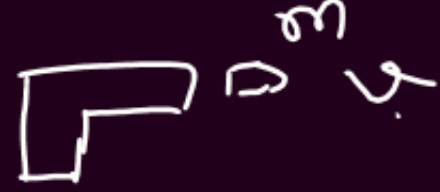
- Different objects
- Simultaneously
- Any Action / Reaction
- Same type
- Pairs



Examples

- Swimming
- Gun-Bullet
- Birds
- A stick figure is shown in a jumping pose, with one leg extended downwards and the other bent. Two arrows originate from the feet: one pointing downwards and to the left, and another pointing upwards and to the right, representing the action and reaction forces during a jump.
- [α - emission]
- Walking / Running

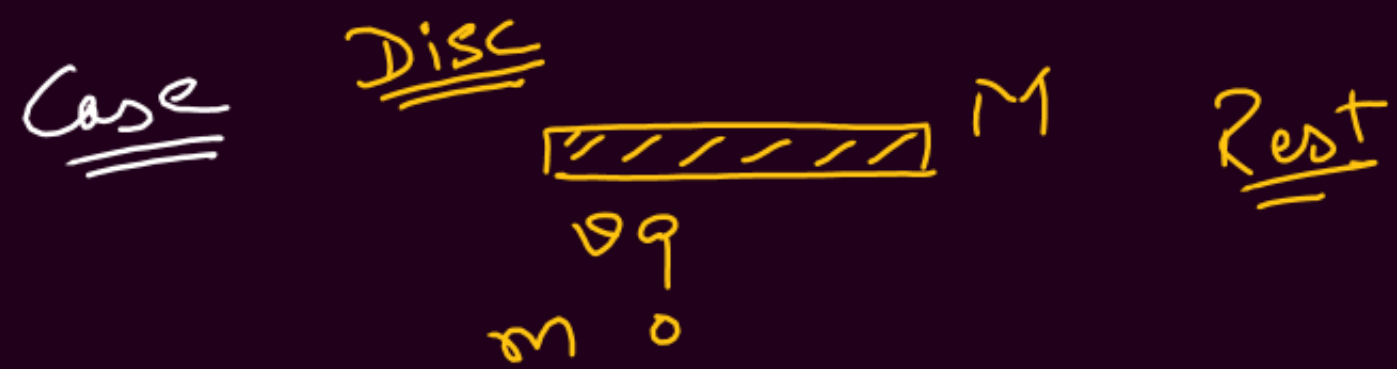
Case Machine Gun



N in t

$$n = \frac{N}{t} = \text{no. of Bullets per sec}$$

$$\text{Recoil force} = \frac{Nmv}{t} = nmv$$



① After collision $\rightarrow$ Rest

$$Mg = nmv$$

② Rebounds with same speed

$$Mg = 2nmv$$

Q. Machine Gun

100 bullets/min

each [10g, 500 m/s]

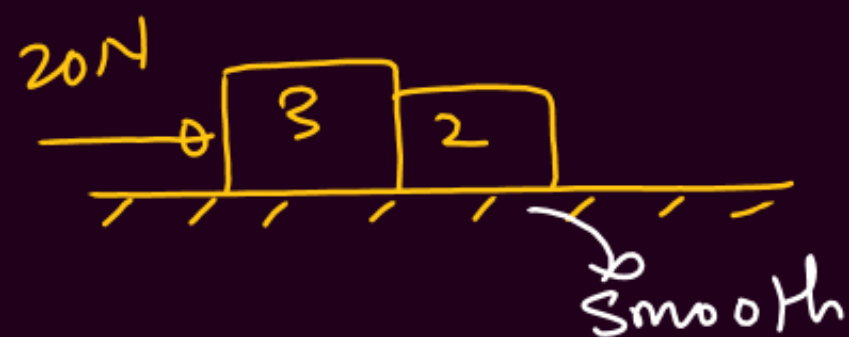
$F = ?$

$$F = \frac{Nmv}{t}$$

$$F = \frac{100 \times 10 \times 500}{1000 \times 60} = \frac{25}{3} \text{ N}$$

Bodies in contact

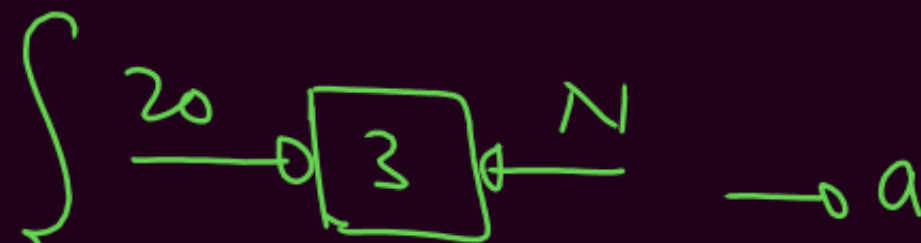
Q.



$$\textcircled{1} a = \frac{20}{3+2} = 4 \text{ m/s}^2$$



$$N = 2a = 8 \text{ N}$$



$$20 - N = 3a$$

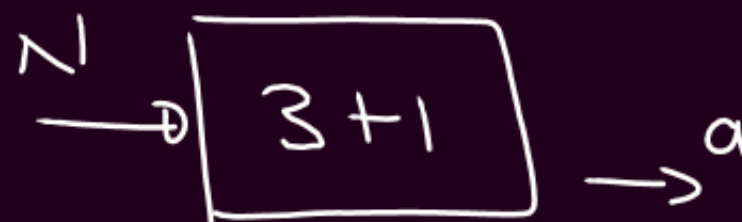
Q.



$$\textcircled{1} a = \frac{30}{6+3+1} = 3 \text{ m/s}^2$$

$$\textcircled{2} F_{\text{net on 3kg}} = ma = 3(3) = \underline{\underline{9 \text{ N}}}$$

$\textcircled{3}$ Force exerted by 6 kg on 3 kg

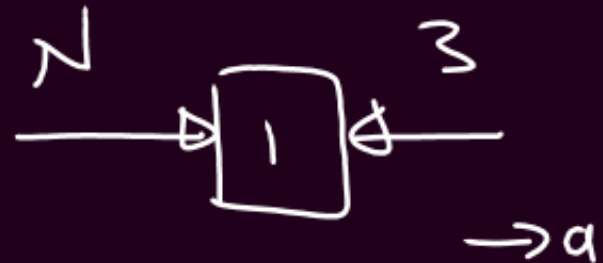


$$N = (3+1)(3) = \underline{\underline{12 \text{ N}}}$$

Pg-160
⑦

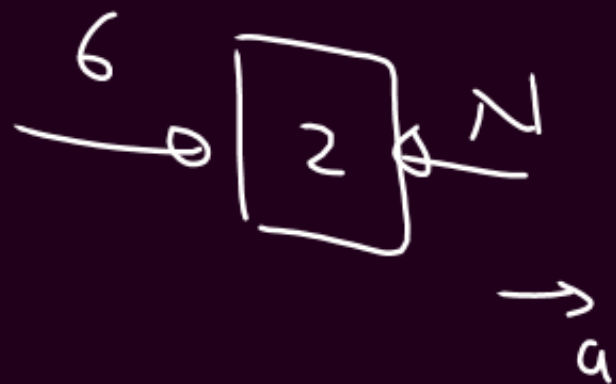


$$a = \frac{6-3}{2+1} = 1 \text{ m/s}^2$$



$$N-3=1a$$

$$\underline{\underline{N=4}}$$

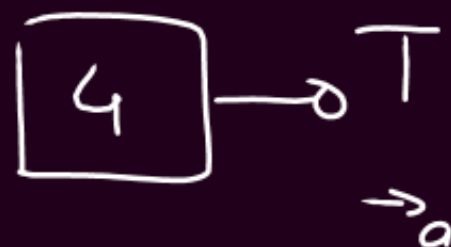


$$6-N=2a$$

$$\underline{\underline{N=4}}$$

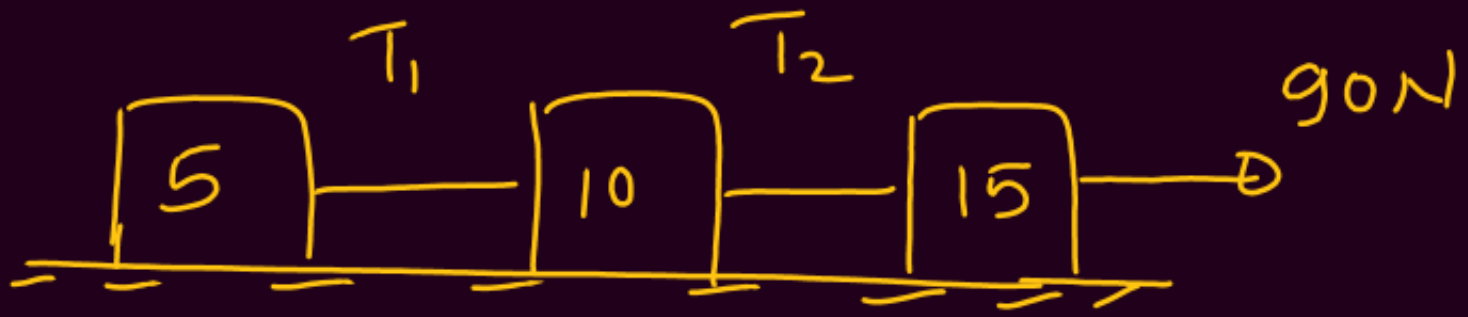


$$a = \frac{35}{4+3} = 5 \text{ m/s}^2$$



$$T = 4(5) = \underline{\underline{20 \text{ N}}}$$

Q.



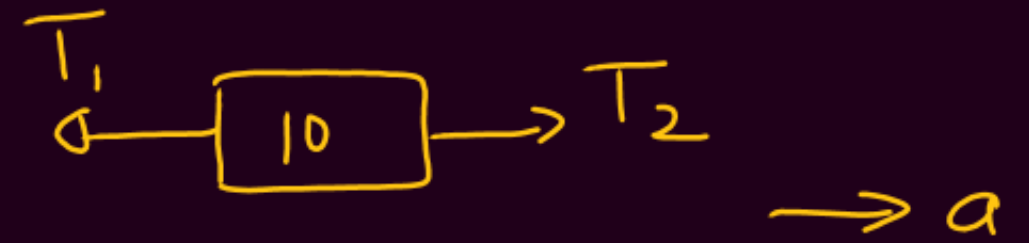
$$a = \frac{90}{5+10+15} = 3 \text{ m/s}^2$$



$$T_1 = 5(3) = 15 \text{ N}$$



$$T_2 = (5+10)(3) = 45 \text{ N}$$

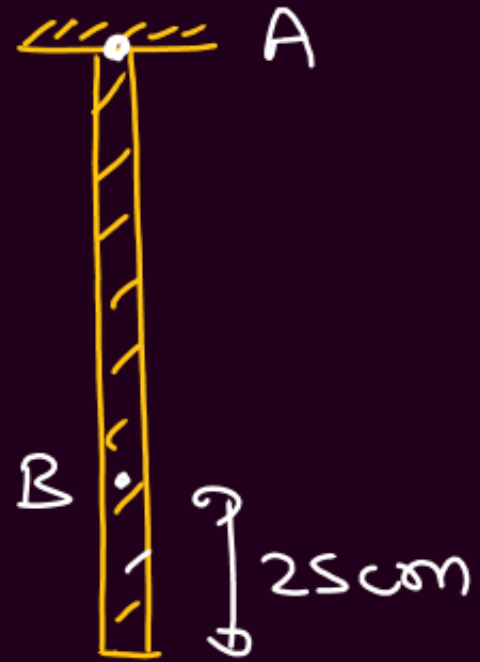


$$T_2 - T_1 = 10(a)$$

$$T_2 - 15 = 10 \times 3$$

$$\underline{T_2 = 45 \text{ N}}$$

Heavy Rope [Uniform]



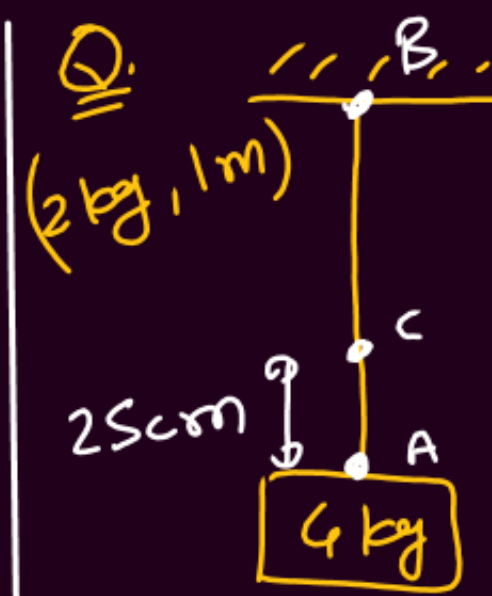
$$\textcircled{1} T_A = 2g = 20\text{N}$$

$$\textcircled{2} T_B = 0.25g = 2.5\text{N}$$

(2kg, 2m)

2m $\rightarrow$ 2kg

0.25m $\rightarrow$ $\left(\frac{2}{2} \times 0.25\right)$ kg



$$T_A = 4g = 40\text{N}$$

$$T_B = 6g = 60\text{N}$$

$$T_C = (4 + 0.5)g = 45\text{N}$$

100 $\rightarrow$ 2kg

25 $\rightarrow$ $\frac{2}{100} \times 25 = \underline{0.5 \text{ kg}}$

Pg-127
⑤

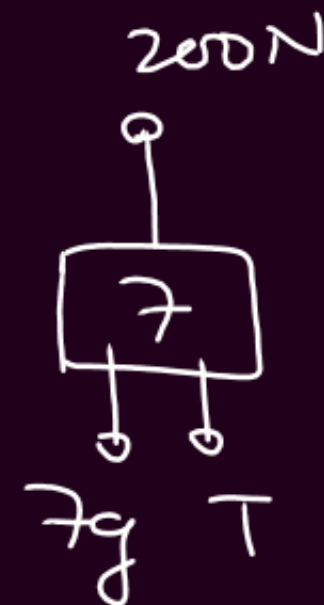


$$a = \frac{F}{M}$$



$$T = \frac{M(L-x)}{L} a = F \frac{(L-x)}{L}$$

Pg-160
⑪



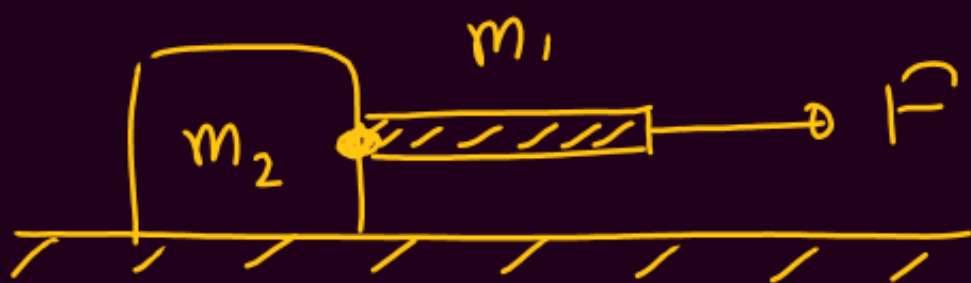
$$a = \frac{200 - 16g}{16} = 2.5 \text{ m/s}^2$$

$$200 - 70 - T = 7(2.5)$$

$$130 - T = 17.5$$

$$T = 112.5 \text{ N}$$

Q



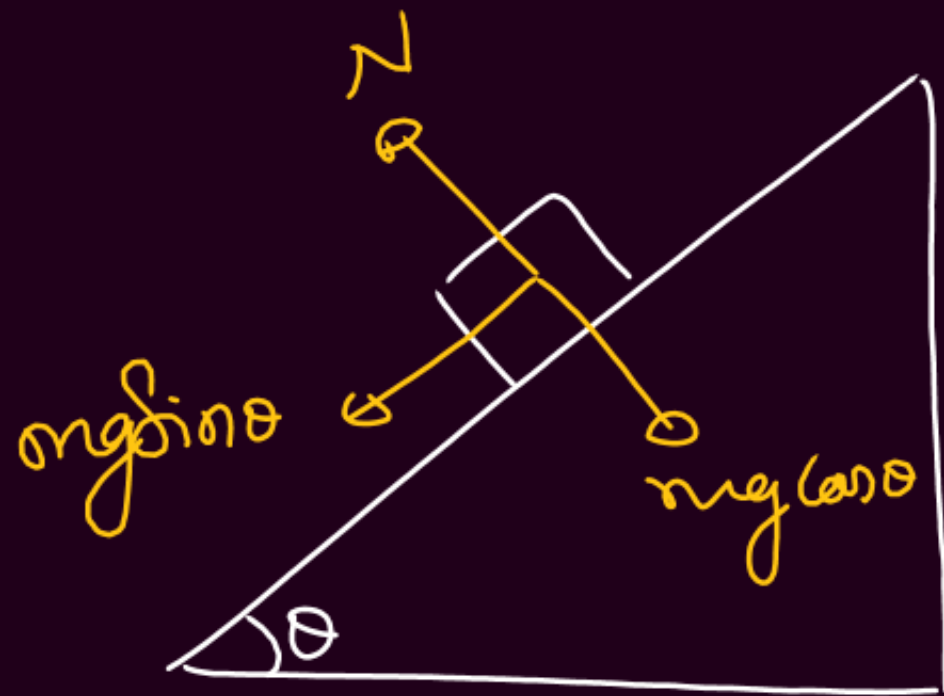
$$a = \frac{F}{m_1 + m_2}$$



$$T = m_2 a = \frac{m_2 F}{m_1 + m_2}$$

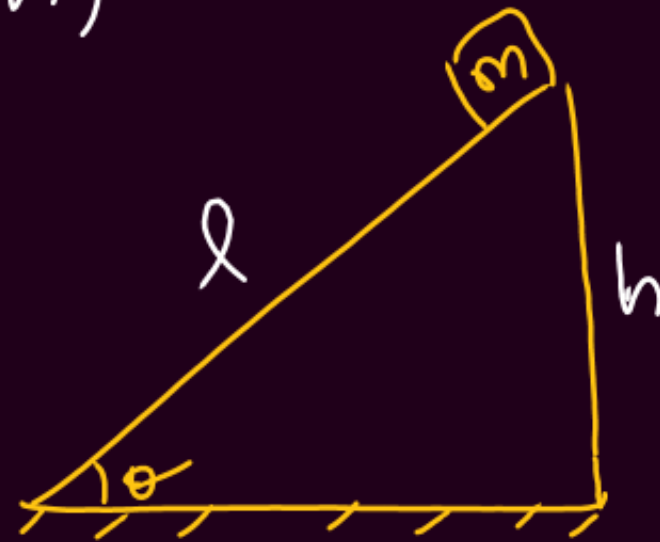
Inclined Plane

(smooth)



$$\textcircled{1} N = mg \cos \theta$$

$$\textcircled{2} a = g \sin \theta$$



$$\textcircled{1} a = g \sin \theta$$

$$\textcircled{2} v = \sqrt{2gh}$$

$$v = \sqrt{2(g \sin \theta) \frac{h}{\sin \theta}}$$

$$\textcircled{3} t = \frac{1}{\sin \theta} \sqrt{\frac{2h}{g}}$$

$$\frac{h}{\sin \theta} = \frac{1}{2} g \sin \theta t^2$$

free fall

—

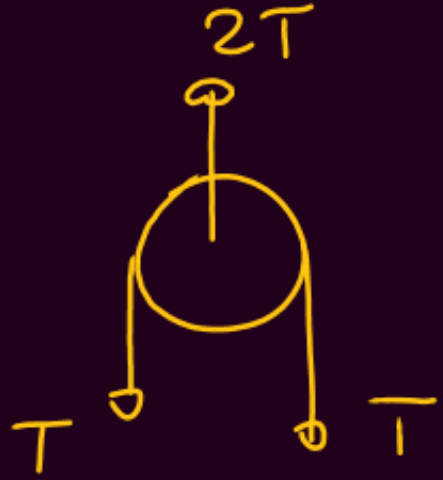
$$a = g$$

$$v = \sqrt{2gh}$$

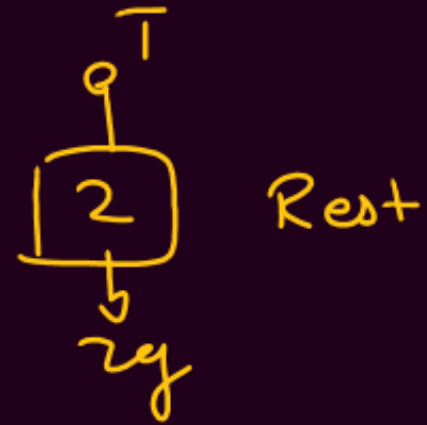
$$t = \sqrt{\frac{2h}{g}}$$

Pulley

Ideal → massless
frictionless



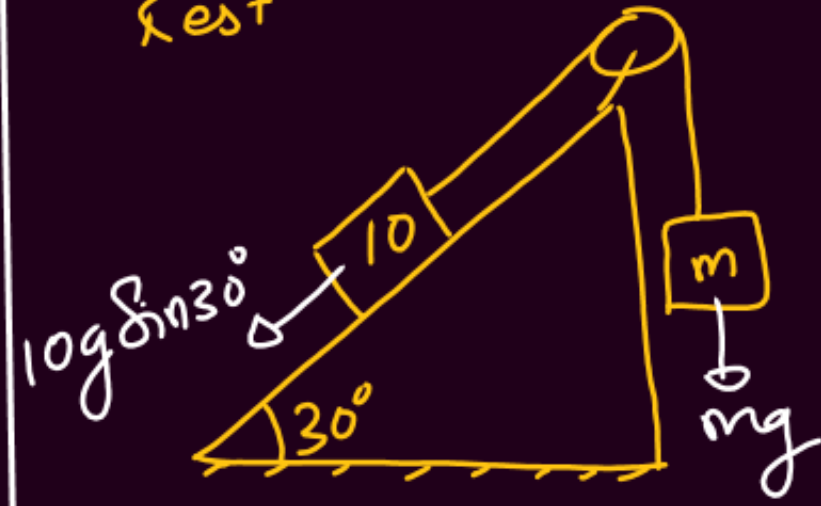
$$a = 0$$



$$T_1 = 2g$$

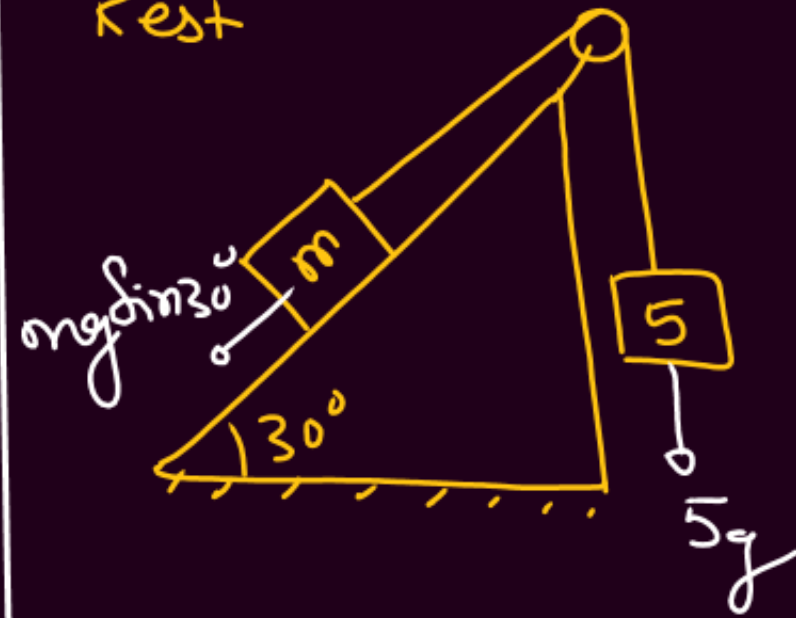
$$T_2 = 2T_1 = 4g$$

Rest



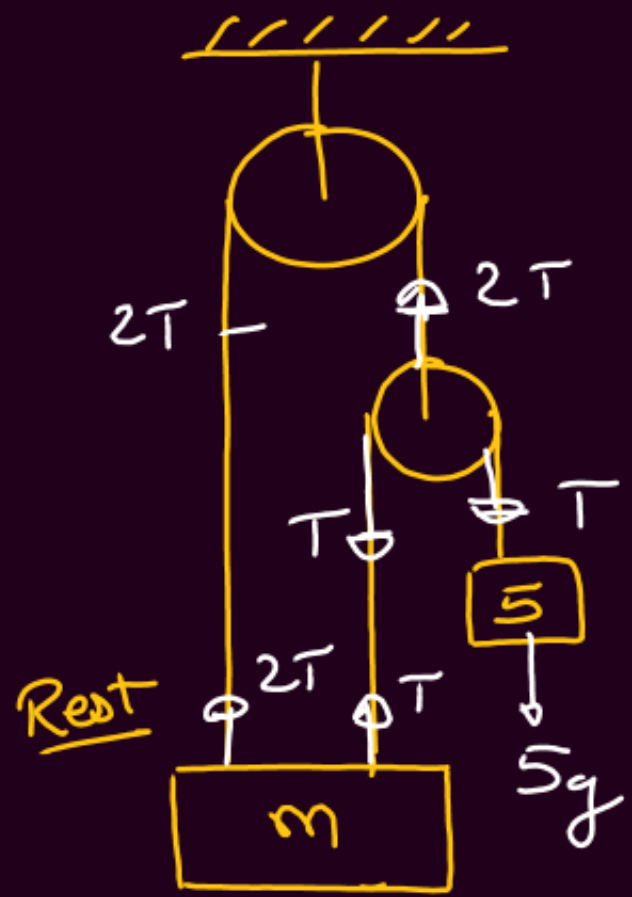
$$mg = 10g \sin 30^\circ$$
$$m = 5 \text{ kg}$$

Rest



$$mg \sin 30^\circ = 5g$$

$$m = 10 \text{ kg}$$



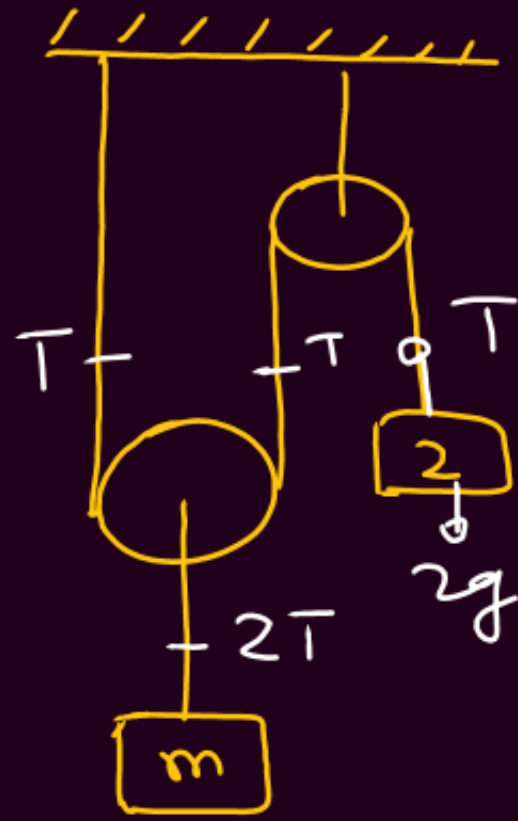
$$(1) T = 5g$$

$$(2) 2T + T = mg$$

$$15g = mg$$

$$m = 15 \text{ kg}$$

Rest



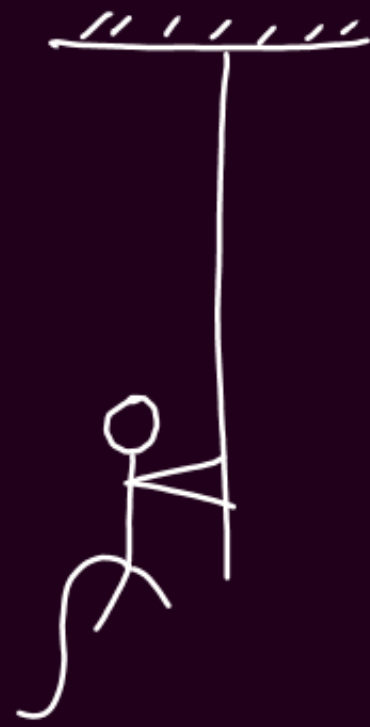
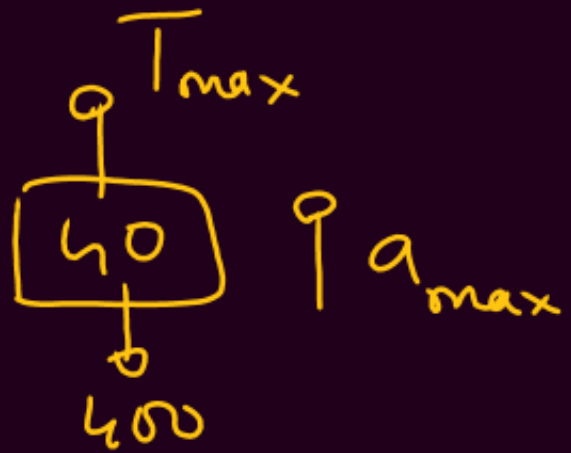
$$(1) T = 2g$$

$$(2) 2T = mg$$

$$m = 4 \text{ kg}$$

Monkey - Rope

Q Rope $\rightarrow$ 600 N
 $m = 40 \text{ kg}$

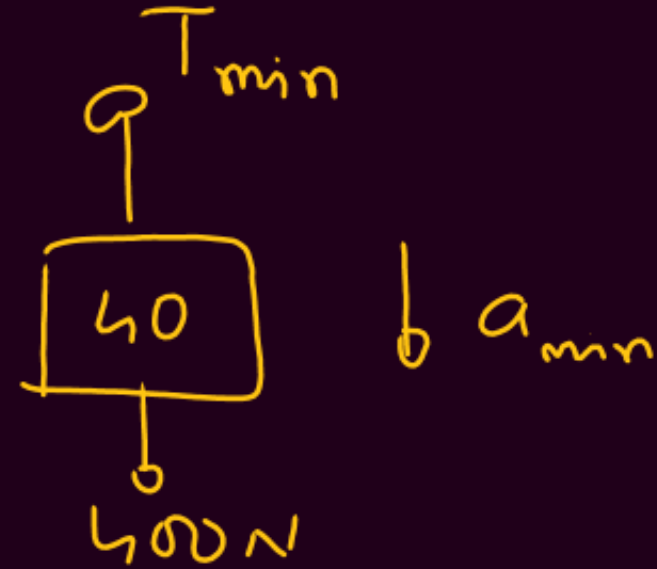


$$600 - 400 = 40a$$

$$200 = 40a$$

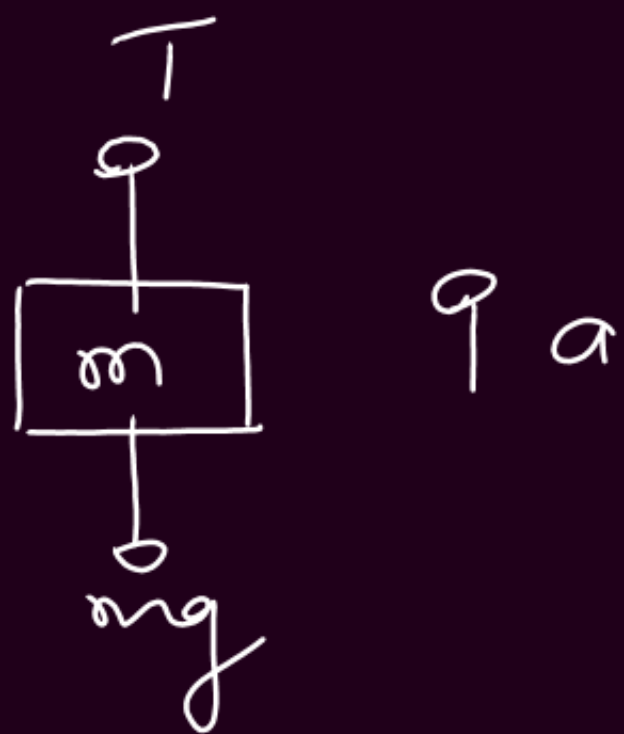
$$a = 5 \text{ m/s}^2$$

Q Rope $\rightarrow$ 300 N
 $m = 40 \text{ kg}$



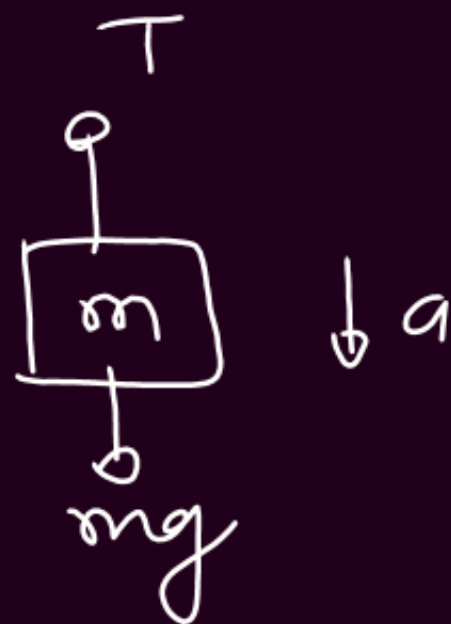
$$400 - 300 = 40a$$

$$a = \frac{100}{40} = 2.5 \text{ m/s}^2$$



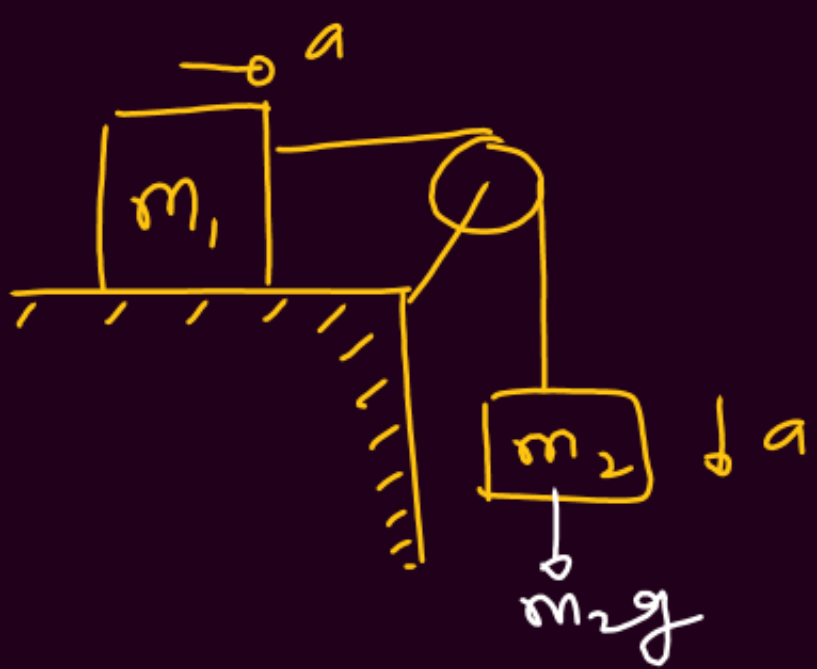
$$T - mg = ma$$

$$T = m(g + a)$$



$$mg - T = ma$$

$$T = m(g - a)$$

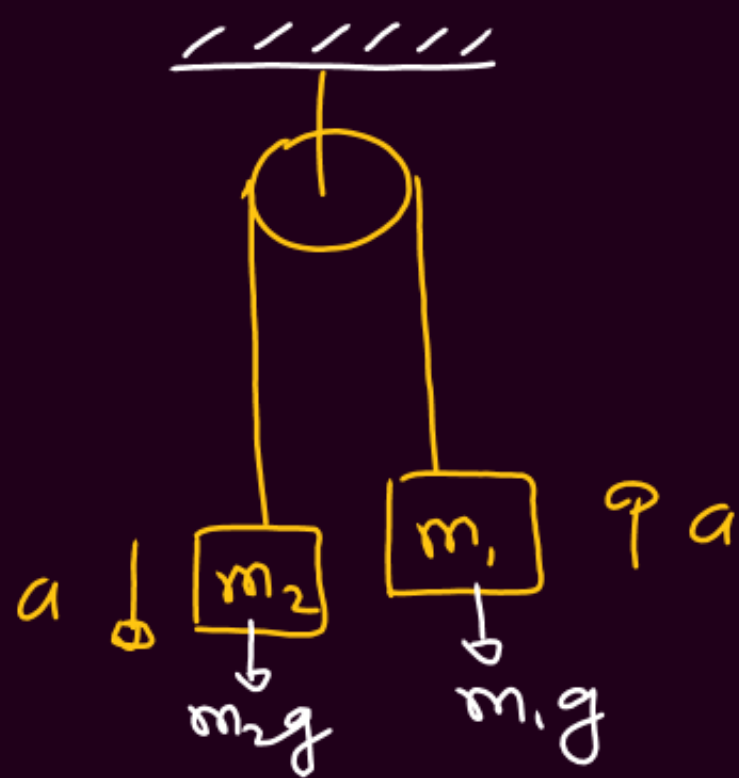


$$\textcircled{1} \quad a = \frac{m_2 g}{m_1 + m_2}$$

$$\textcircled{2} \quad T = \frac{m_1 m_2 g}{m_1 + m_2}$$

$$T = m_1 a$$

$$T = m_2 (g - a)$$



$$\textcircled{1} \quad a = \frac{(m_2 - m_1) g}{m_2 + m_1}$$

$$\textcircled{2} \quad T = \frac{2 m_1 m_2 g}{m_1 + m_2}$$

$$T = m_2 (g - a)$$

$$T = m_1 (g + a)$$

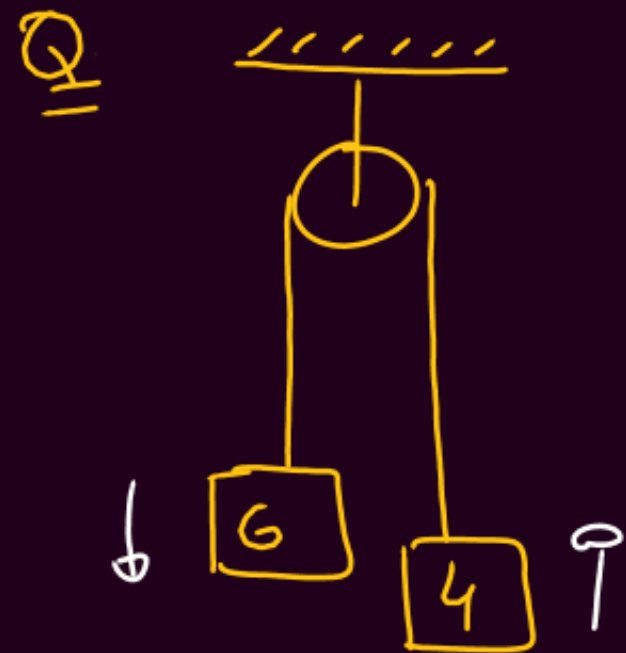


$$a = \frac{4g}{6+4}$$

$$a = 4 \text{ m/s}^2$$

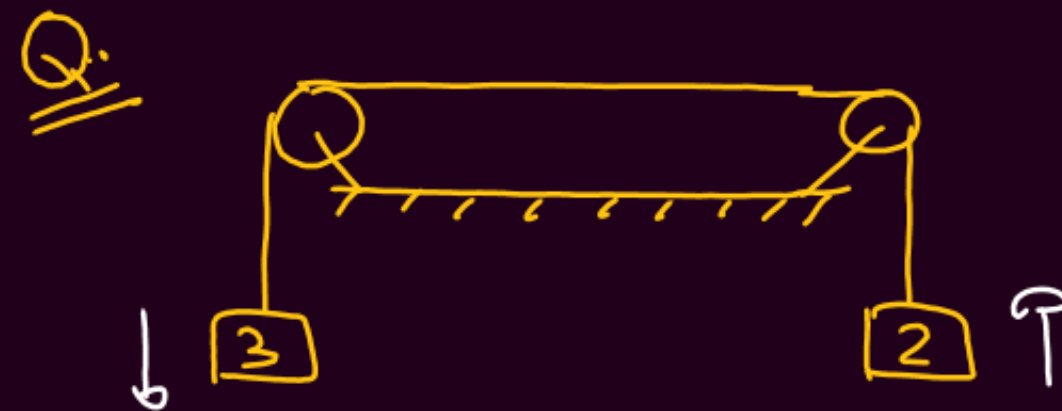
$$T = 4(g - 4)$$

$$T = 24 \text{ N}$$



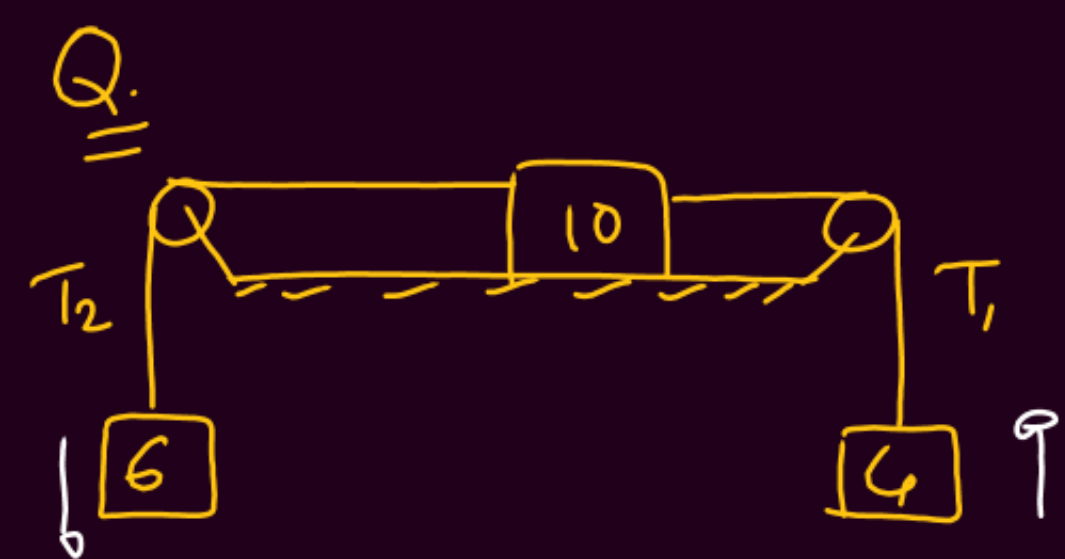
$$a = \frac{(6-4)g}{6+4} = 2 \text{ m/s}^2$$

$$T = 4(g + 2) = 48 \text{ N}$$



$$a = \frac{(3-2)g}{3+2} = 2 \text{ m/s}^2$$

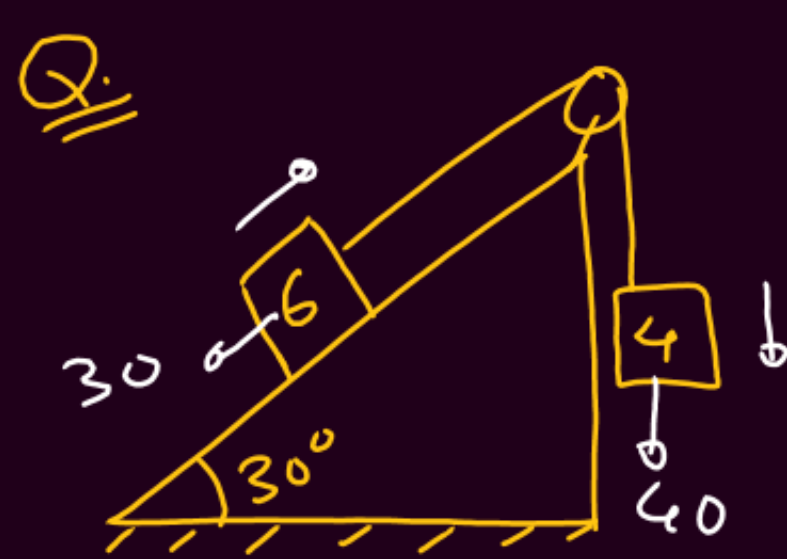
$$T = 2(g + 2) = 24 \text{ N}$$



$$a = \frac{(6-4)g}{6+10+4} = 1 \text{ m/s}^2$$

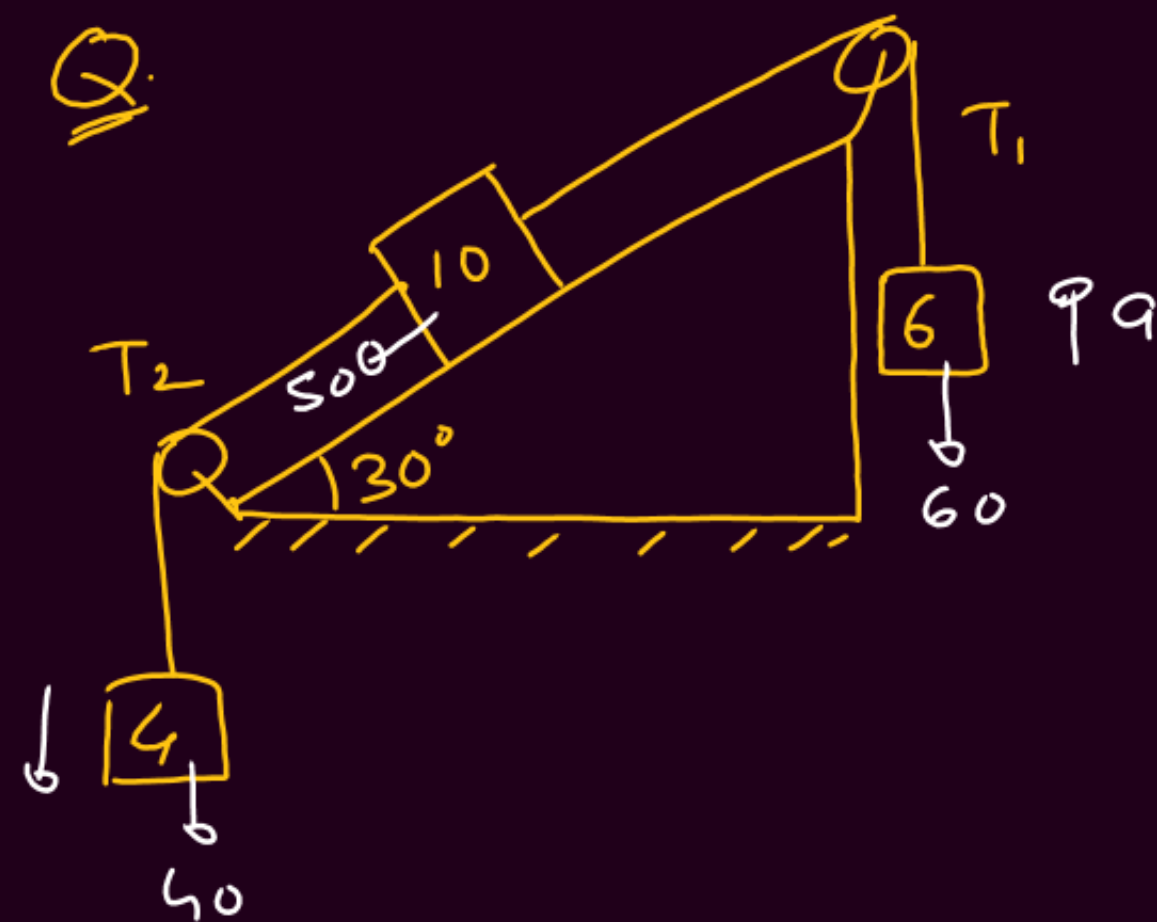
$$T_1 = 4(g+1) = 44 \text{ N}$$

$$T_2 = 6(g-1) = 54 \text{ N}$$



$$a = \frac{40-30}{6+4} = 1 \text{ m/s}^2$$

$$T = 4(g-1) = 36 \text{ N}$$



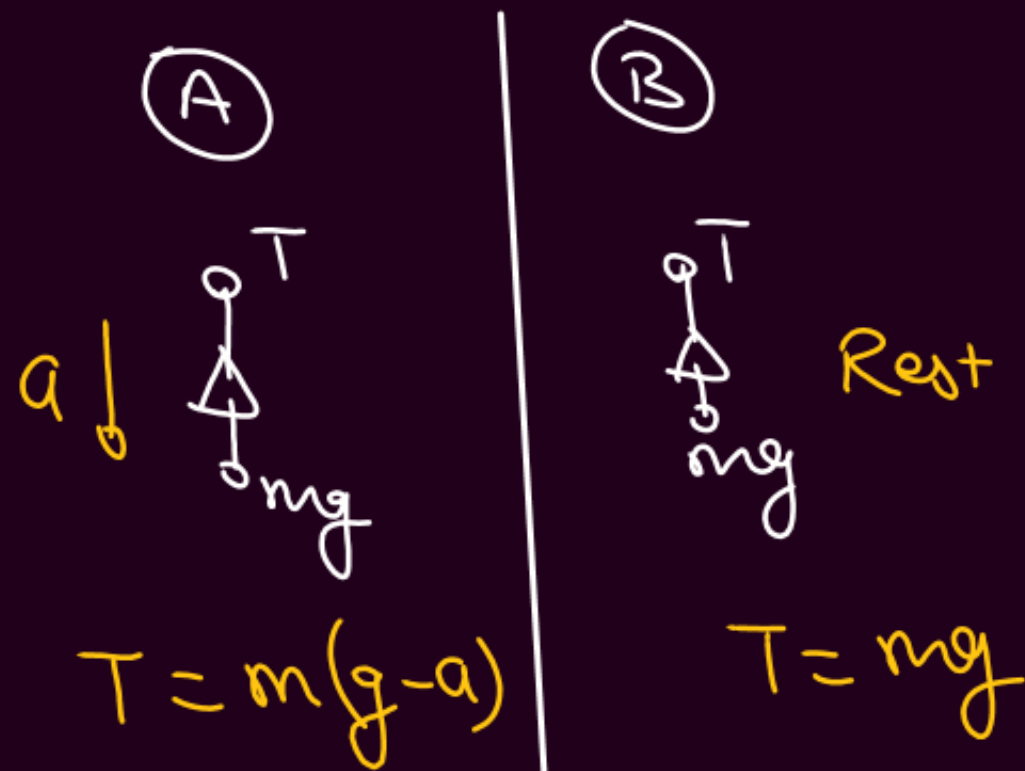
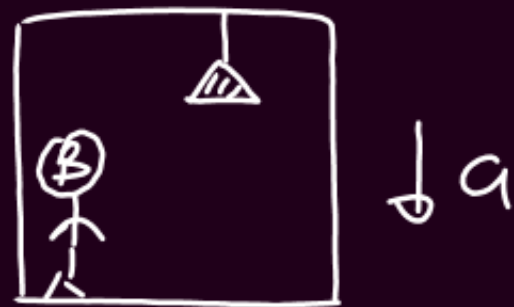
$$a = \frac{40+50-60}{4+10+6} = 3/2 \text{ m/s}^2$$

$$T_1 = 6(g+1.5) = 69 \text{ N}$$

$$T_2 = 4(g-1.5) = 34 \text{ N}$$

Inertial & Non-inertial frames

→ Ideal Concept



→ Ground

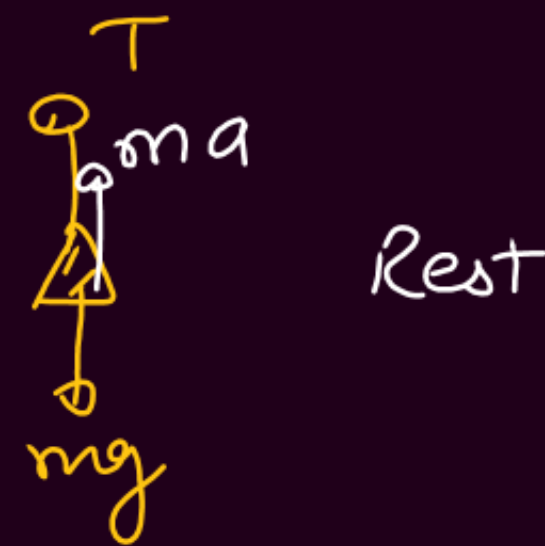
Pseudo Force

- Not Real
- Non-inertial

$$F = -m_o a_f$$

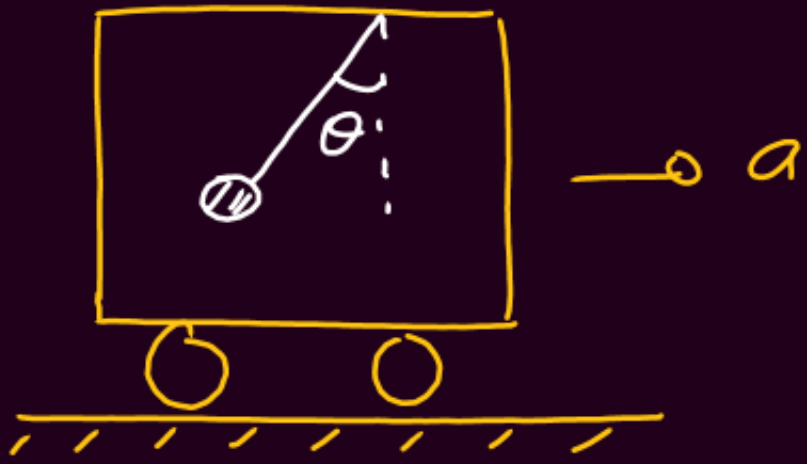
m_o = mass of object
 a_f = acc. of frame

$a \downarrow$ B



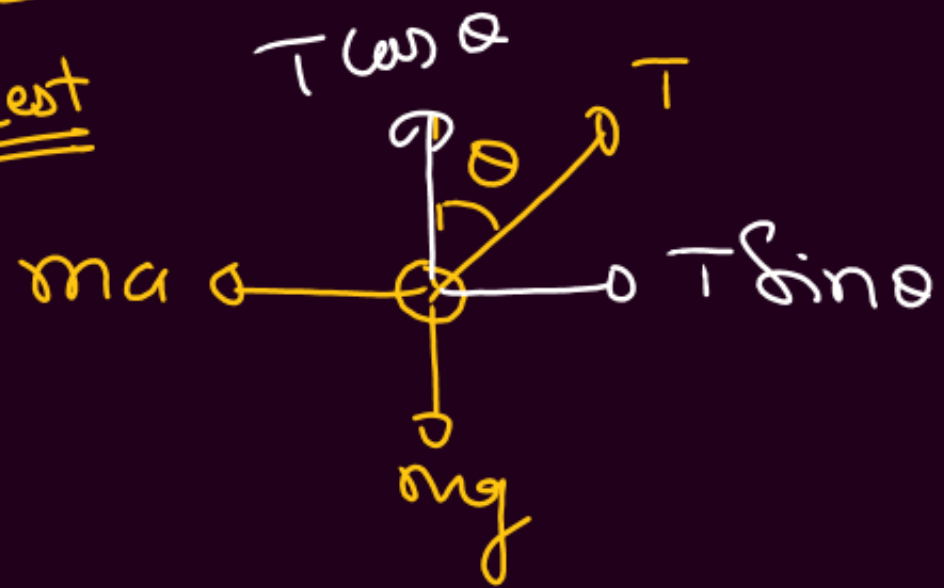
$$T + ma = mg$$
$$T = m(g - a)$$





Car frame

Rest

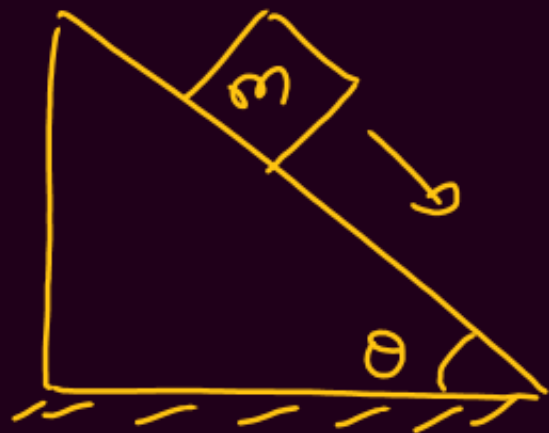


$$\textcircled{1} T \sin \theta = ma$$

$$\textcircled{2} T \cos \theta = mg$$

$$\textcircled{3} \tan \theta = \frac{a}{g}$$

$$\textcircled{4} T = m \sqrt{g^2 + a^2}$$



fixed wedge

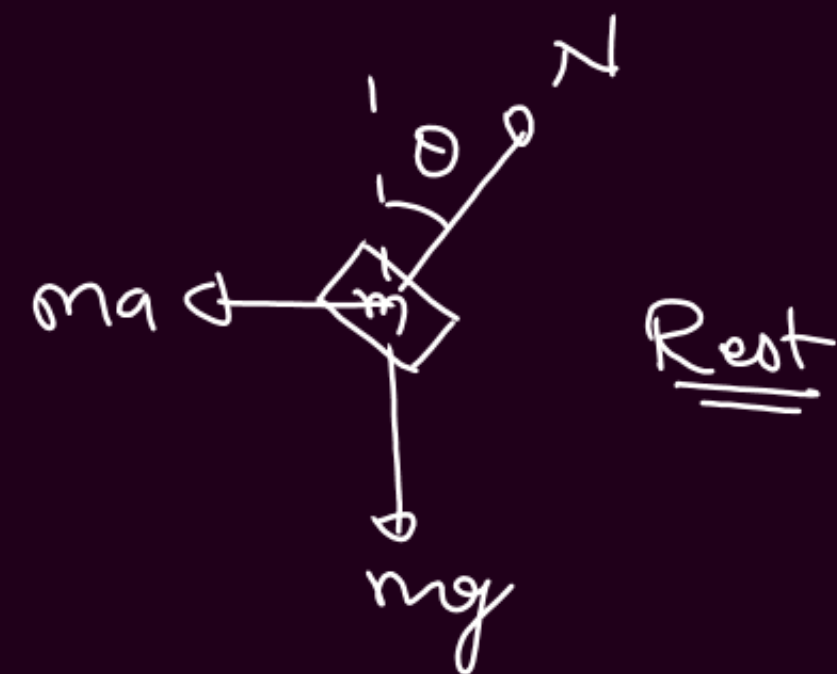
$$N = mg \cos \theta$$



$\left\{ \begin{array}{l} a = ? \\ \text{such that Block} \\ \text{doesn't slide on} \\ \text{wedge} \end{array} \right.$

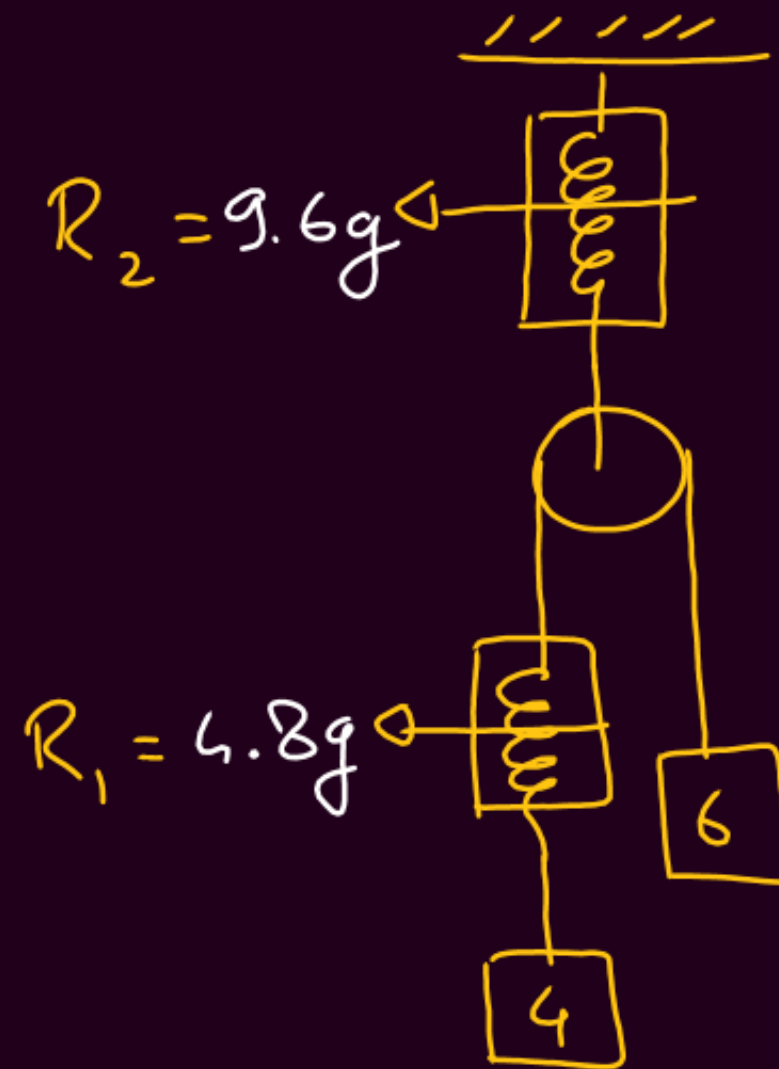
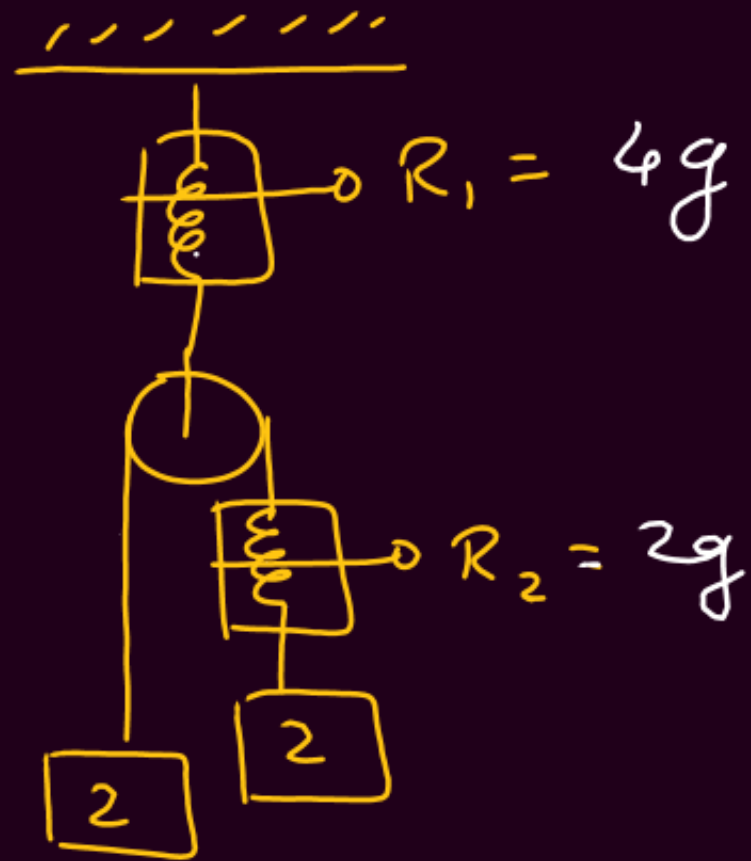
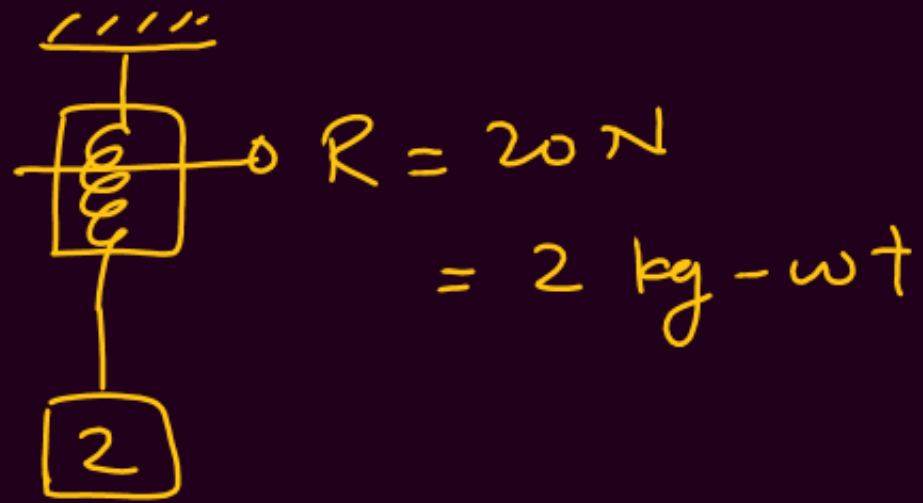
① $a = g \tan \theta$

② $N = \frac{mg}{\cos \theta}$

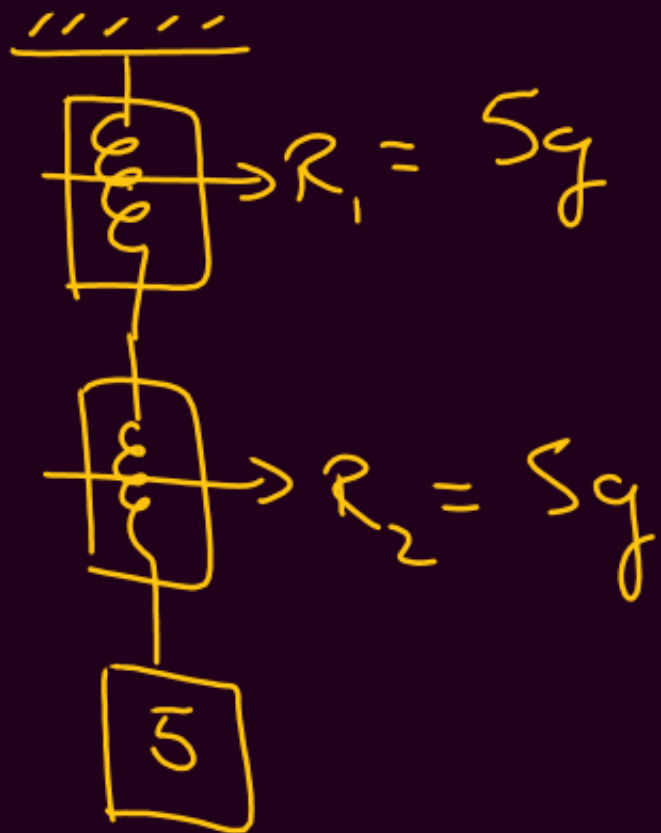


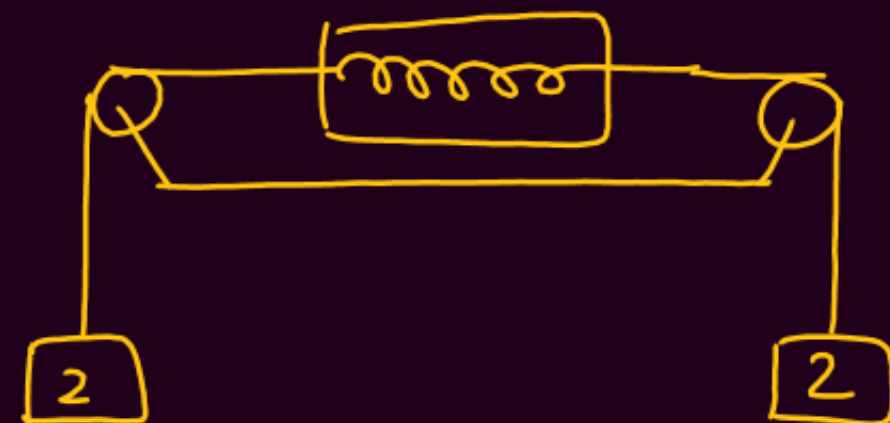
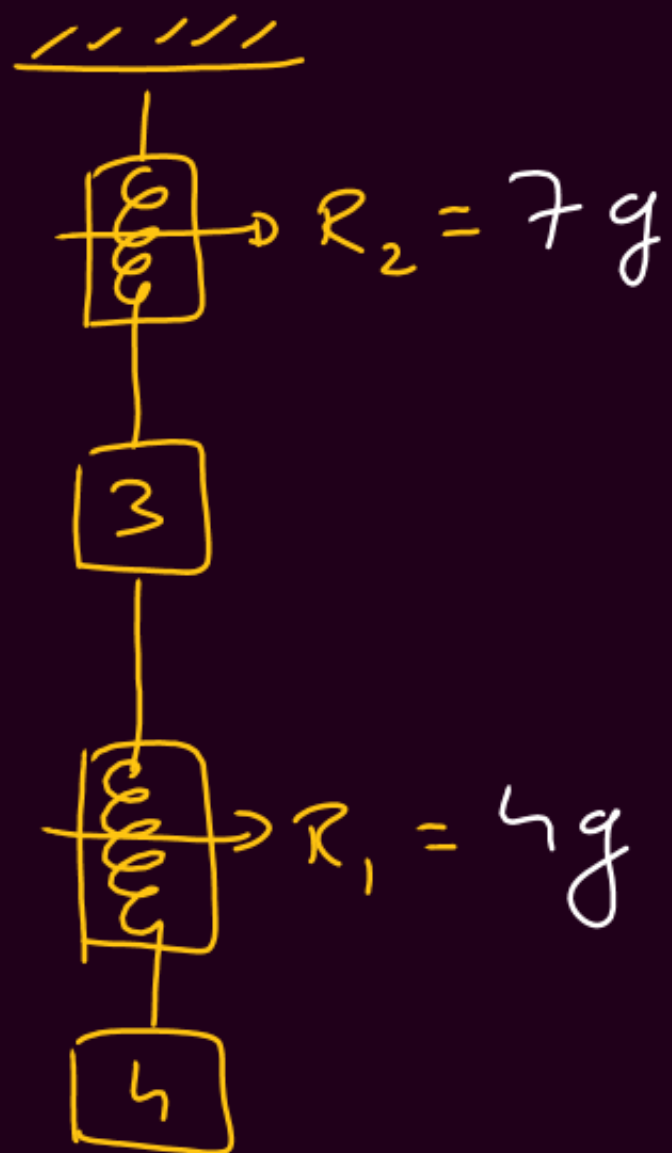
$$N \cos \theta = mg$$

Spring Balance (Tension)



$$R_1 = \frac{2(4)(6)g}{4+6} = 4.8g$$





$$R = 2g$$



$$R = 100N$$

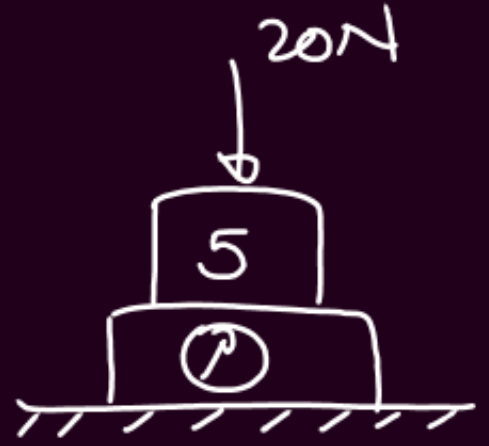


$$R = 100N$$

Weighing Machine (N) = App Weight



$$R = 5g$$



$$R = 50 + 20 \\ = 70 \text{ N}$$



$$R = 50 - 30 \\ = 20 \text{ N}$$



Lift



Rest / Const
vel

$$R = mg$$

$a \uparrow$



$$R = m(g + a)$$

$a \downarrow$ ($a < g$)



$$R = m(g - a)$$

$a = g \downarrow$
Satellite / free fall.

weightlessness

$$R = 0$$



Q Rest $R = 80 \text{ kg}$

$a = 2 \text{ m/s}^2$ $R = ?$

$$\begin{aligned} R &= m(g+a) \\ &= 80(10+2) \\ &= 960 \text{ N} \end{aligned}$$

Q.

$$m(g+a) = 90g$$

$$m(g-a) = 60g$$

Add

$$2mg = 150g$$

$$\boxed{m = 75 \text{ kg}}$$

$$75(g+a) = 90g$$

$$a = 2 \text{ m/s}^2$$

Bird Cage

① Wired Cage



$m_1 = \text{Bird}$

$m_2 = \text{Cage}$

① Bird at Rest

$$R = (m_1 + m_2)g$$

② Bird is flying

$$R < (m_1 + m_2)g$$

② Air Tight Cage

① Rest / const. vel

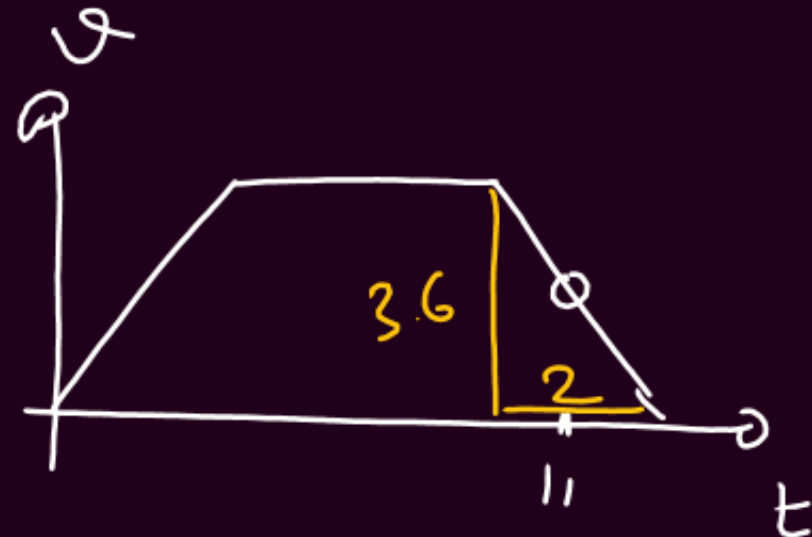


$$R = (m_1 + m_2)g$$

② ↑ a Bird

$$R = m_1(g + a) + m_2g$$

Pg - 127
(4)



$$R = m(g - a)$$

$$R = 1500 \left(9.8 - \frac{3.6}{2} \right)$$

$$\underline{R = 12000 \text{ N}}$$

Pg - 162
(28)



$$F \rightarrow m_1 \leftarrow kx$$

$$F - kx = m_1 a_1$$

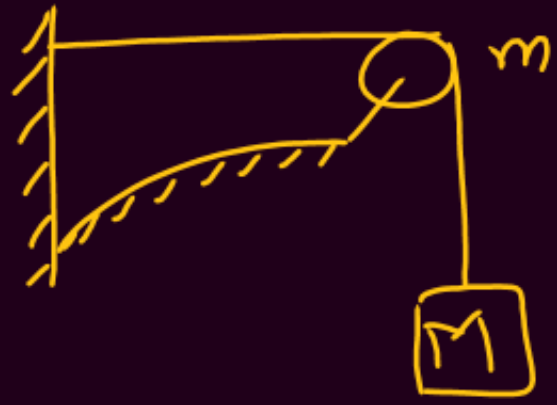
$$F - m_2 a_2 = m_1 a_1$$

$$F - m_1 a_1 = m_2 a_2$$

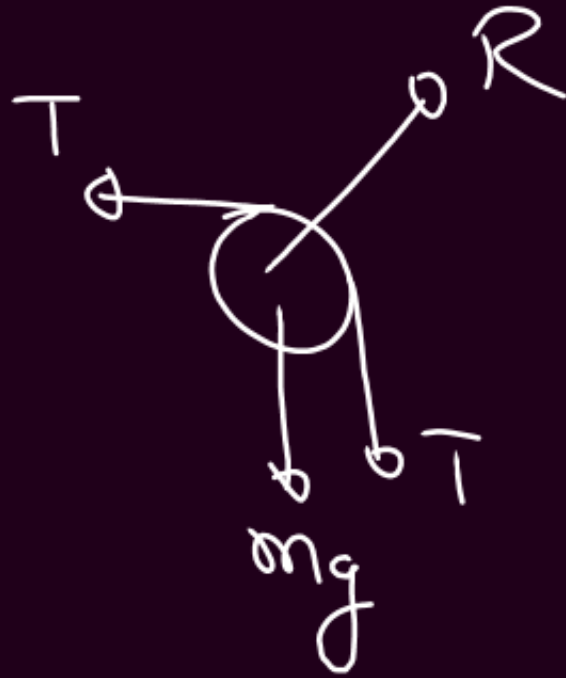
$$kx \rightarrow m_2$$

$$kx = m_2 a_2$$

Pg-133
⑤



Pulley



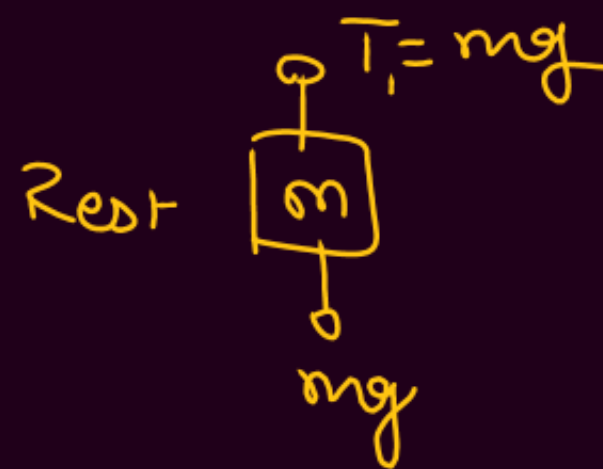
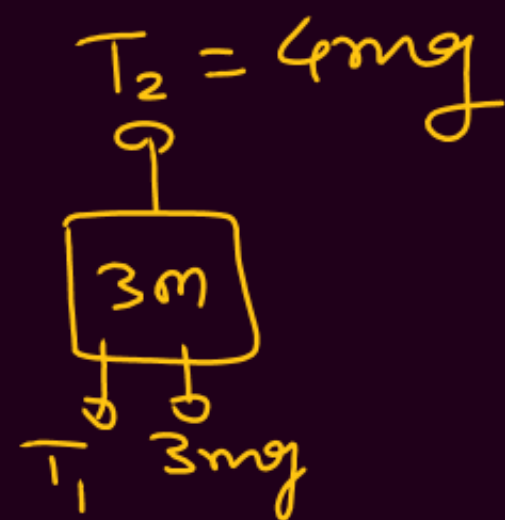
$$R = \sqrt{(mg + T)^2 + T^2}$$

$$R = \sqrt{(mg + Mg)^2 + (Mg)^2}$$

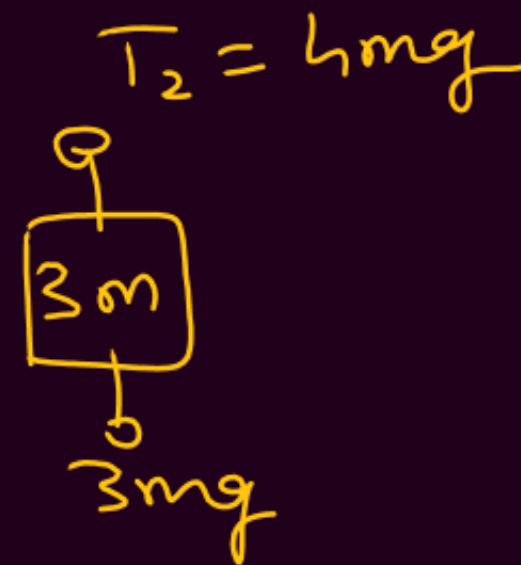
Pg-173
(22)



Just Before



Just After

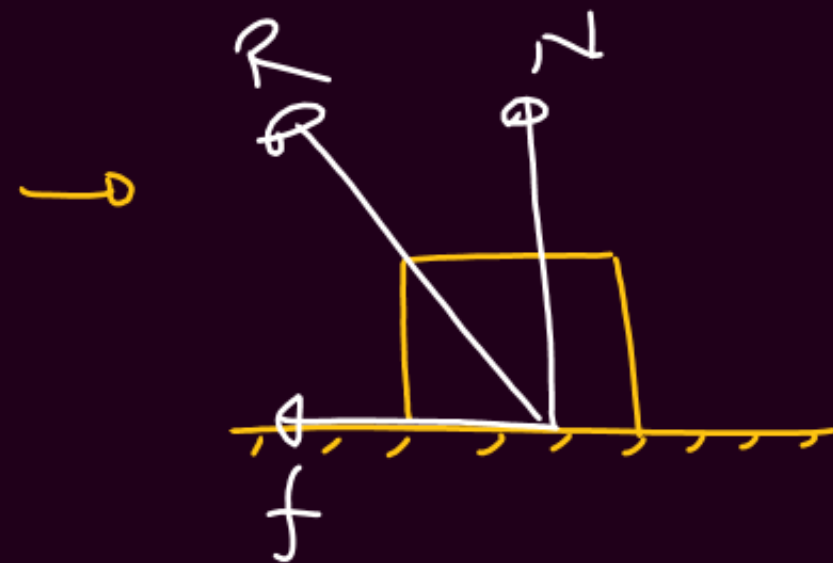


$$a = \frac{4mg - 3mg}{3m} = g/3$$

$$\downarrow a = \frac{mg}{m} = g \downarrow$$

Friction

→ opposes the relative motion
betⁿ surfaces



$$R = \sqrt{N^2 + f^2}$$

- Static → no rel. motion betⁿ surfaces
- Kinetic → rel. motion
(sliding)

Macroscopic View → roughness



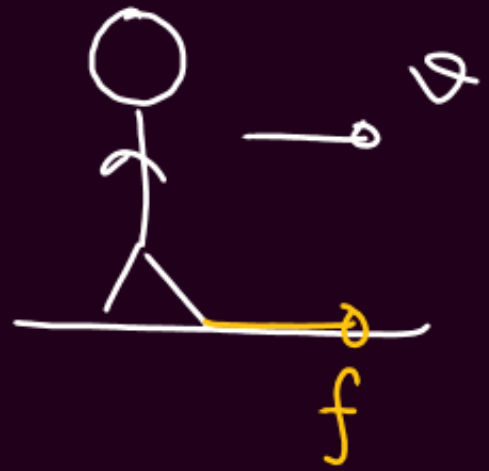
Microscopic View → Actual pts. in contact

- ① Smooth $f \downarrow$
- ② Very smooth $f \uparrow \uparrow$ (cold welding)



Static friction (f_s)

→ walking / Running



Limiting Friction
(max f_s)

$$f_L = \mu_s N$$

μ_s = coeff of static friction

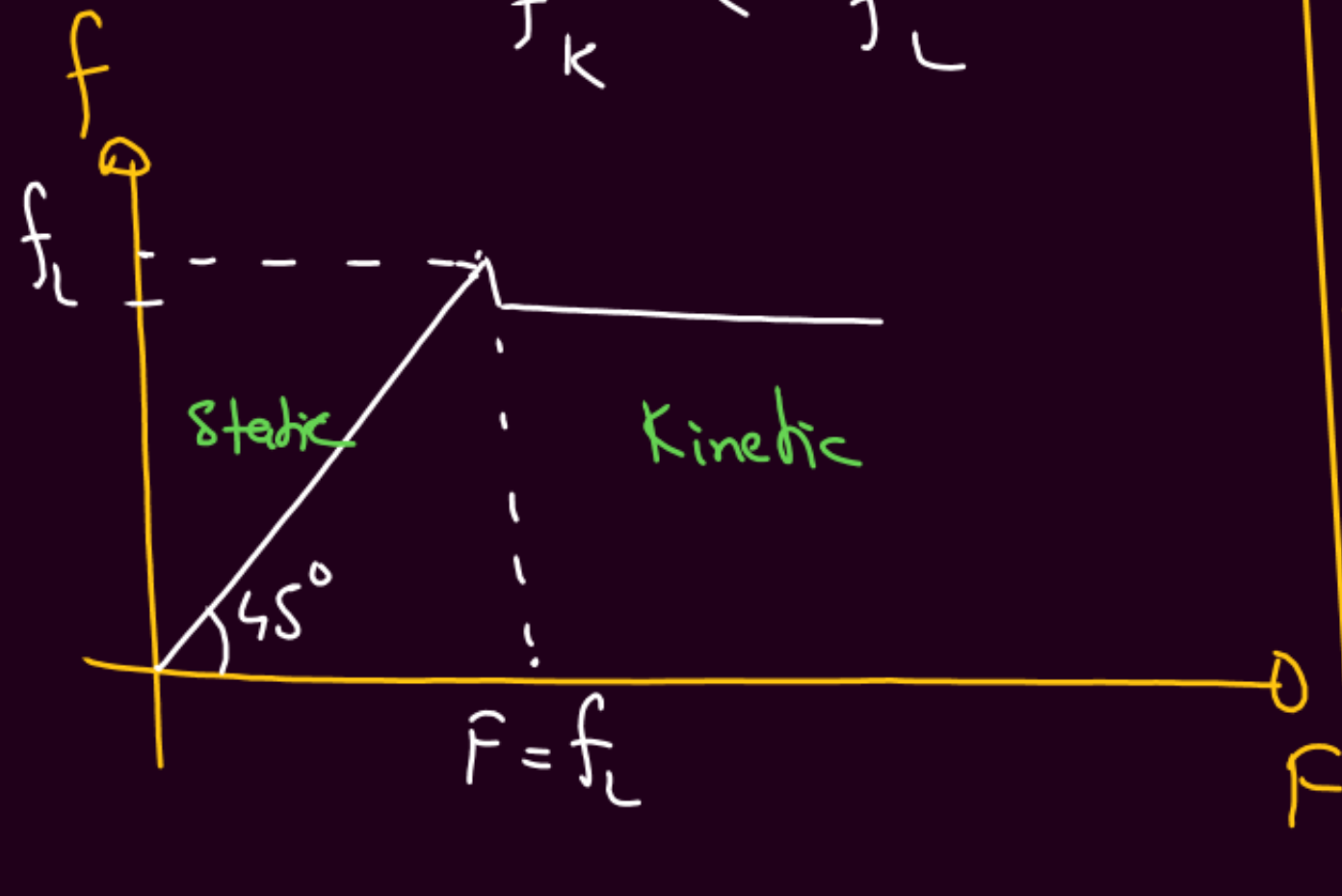
Kinetic (f_k)

$$f_k = \mu_k N$$

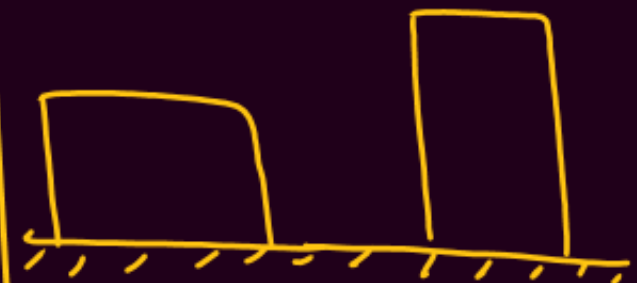
μ_k = coeff of kinetic friction

$$\mu_k < \mu_s$$

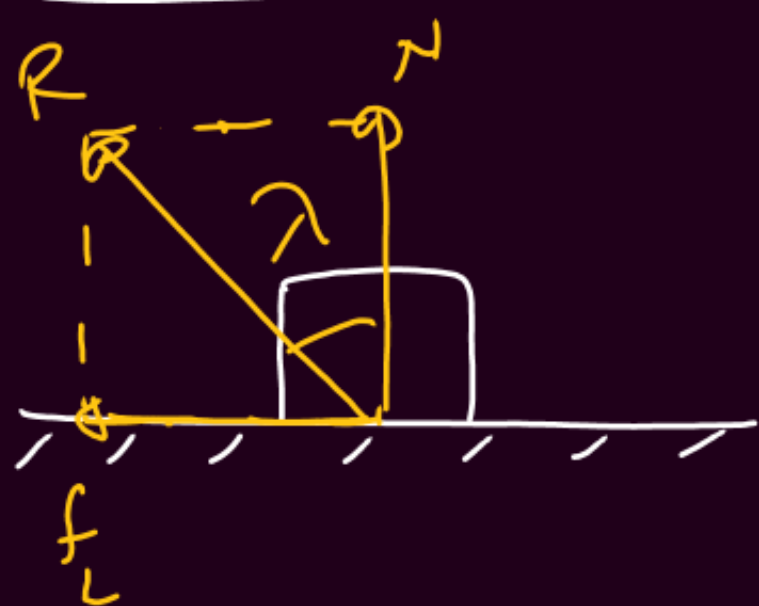
$$f_k < f_L$$



f_k / f_L
is independent
of Surface Area



Angle of Friction



$$\tan \lambda = \frac{f_L}{N} = \frac{\mu_s N}{N}$$

$$\boxed{\tan \lambda = \mu_s}$$



$$\mu_k = 0.4$$

$$\mu_s = 0.5$$

$$\textcircled{1} N = 50 \text{ N}$$

$$\textcircled{2} f_k = 0.4(50) = 20 \text{ N}$$

$$\textcircled{3} f_L = 0.5(50) = 25 \text{ N}$$

① $F = 10 \text{ N}$	Rest	$f_s = 10 \text{ N}$
② $F = 22 \text{ N}$	Rest	$f_s = 22 \text{ N}$
③ $F = 25 \text{ N}$	Rest	$f_L = 25 \text{ N}$
④ $F = 26 \text{ N}$	$a = \frac{26-20}{5}$	$f_k = 20 \text{ N}$
⑤ $F = 30 \text{ N}$	$a = \frac{30-20}{5}$	$f_k = 20 \text{ N}$

Q.



$$\mu_s = 0.4$$

$$\mu_k = 0.35$$

$$N = 100 \text{ N}$$

$$f_s = 40 \text{ N}$$

$$f_k = 35 \text{ N}$$

$$a = ?$$

$$a = \frac{50 - 35}{10} = 1.5 \text{ m/s}^2$$

Q.



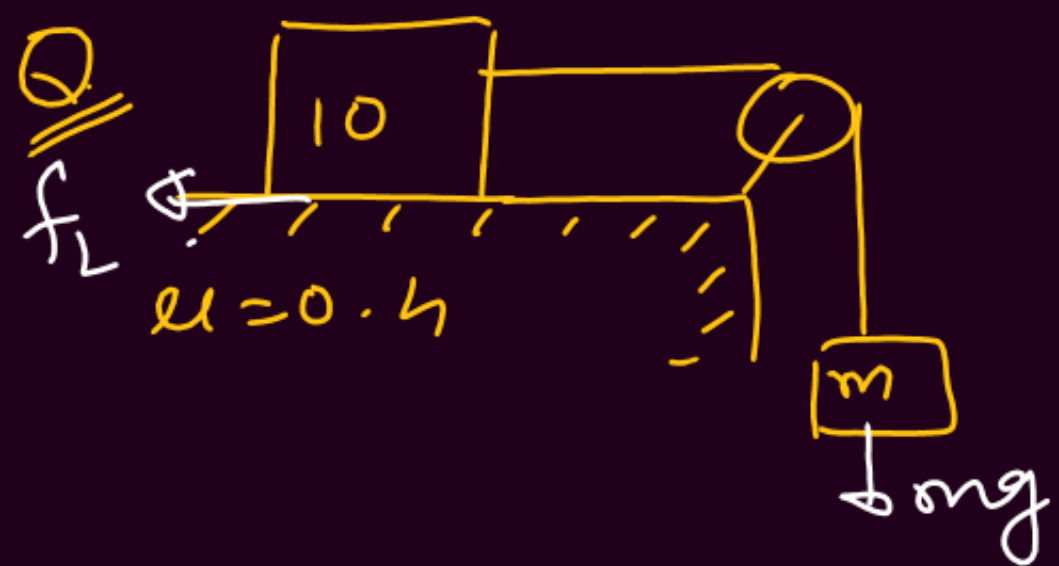
$$\mu = 0.5$$

Distance before Rest?

$$a = \frac{f_k}{m} = \frac{\mu mg}{m}$$

$$\boxed{a = \mu g}$$

$$\boxed{s = \frac{u^2}{2(\mu g)}} = \frac{(10)^2}{2 \times 0.5 \times 10} = 10 \text{ m}$$



max m for rest?

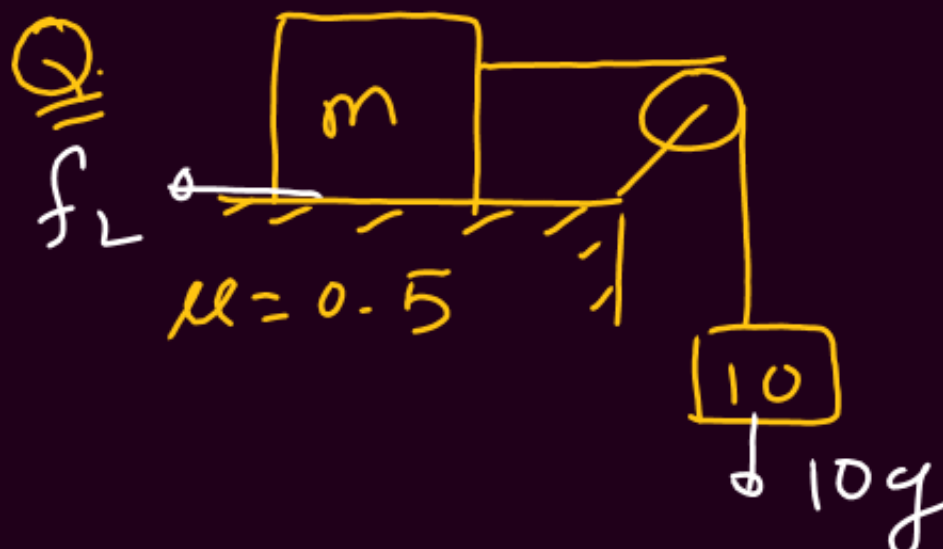
$$N = 100 \text{ N}$$

$$f_L = 0.4(100) = 40 \text{ N}$$

$$mg = f_L$$

$$m(10) = (40)$$

$$m = 4 \text{ kg}$$



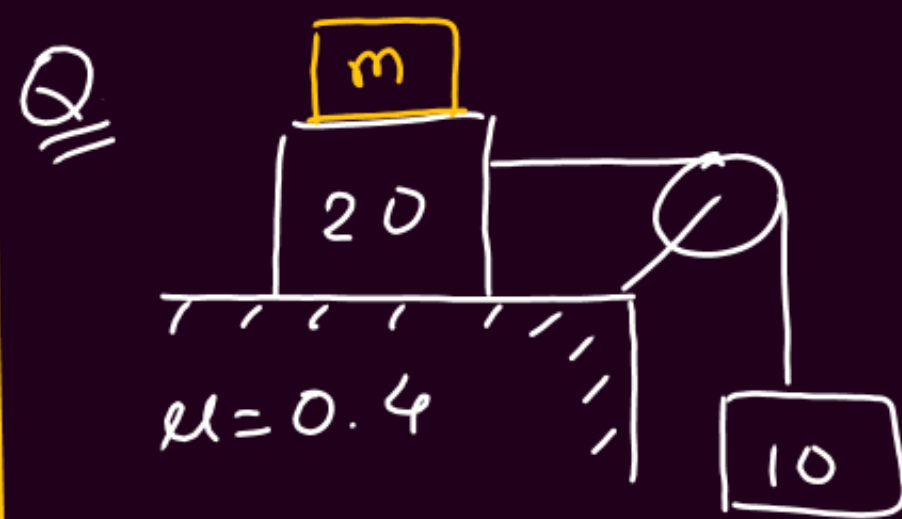
min m for rest?

$$N = mg$$

$$f_L = 0.5mg$$

$$0.5mg = 10g$$

$$m = 20 \text{ kg}$$

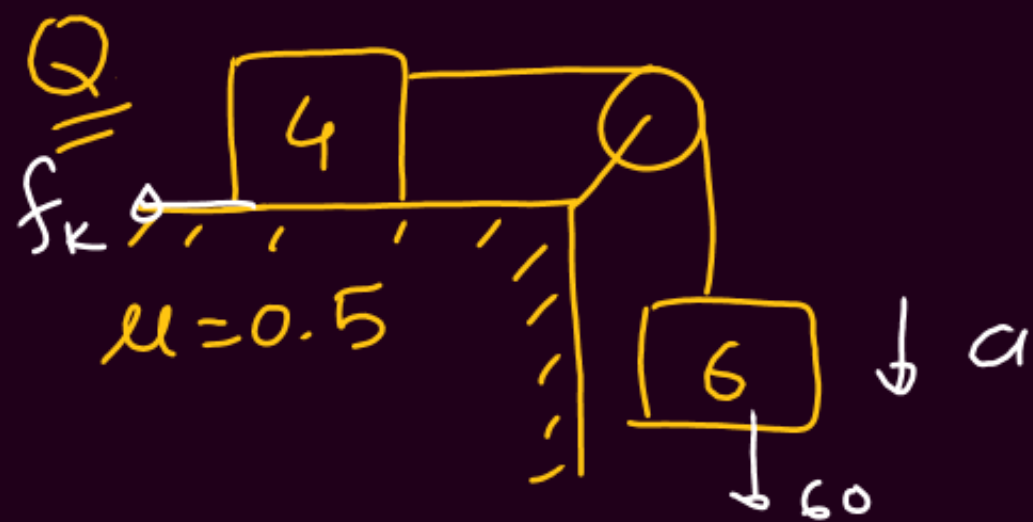


min m for rest?

$$f_L = 0.4(m+20)g = 10g$$

$$(m+20) = \frac{10}{0.4} = 25$$

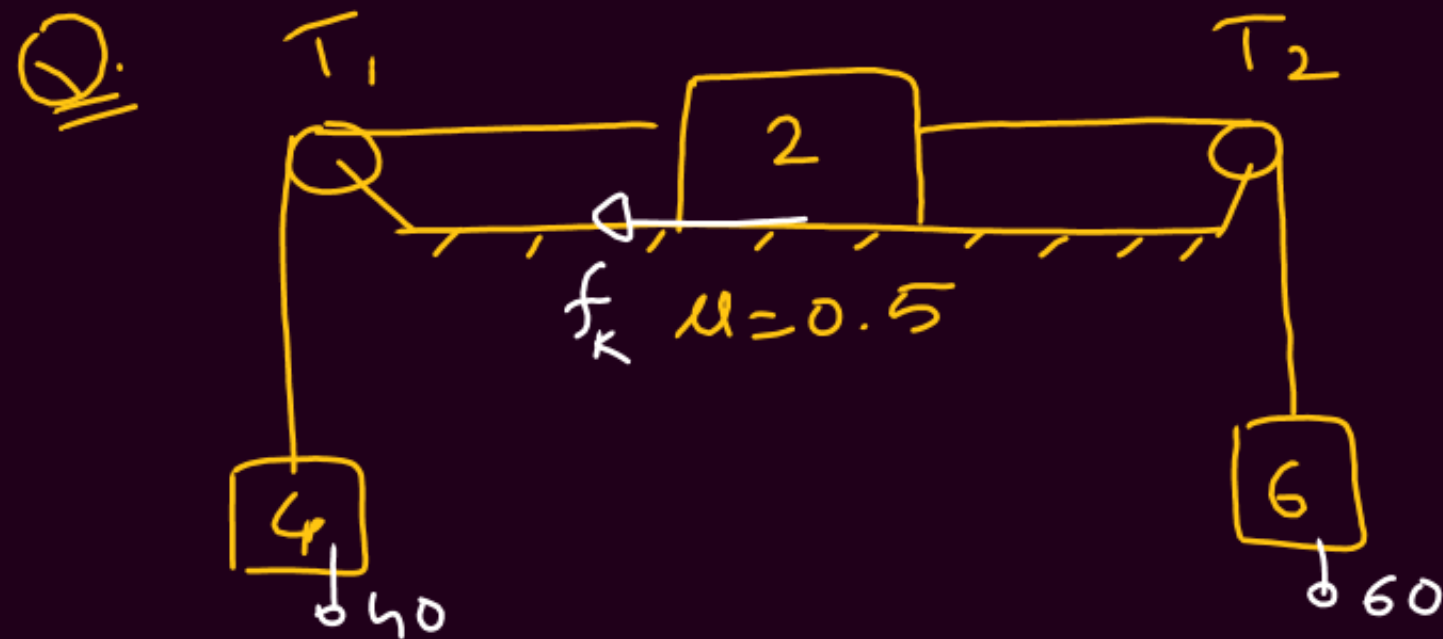
$$m = 5 \text{ kg}$$



$$\textcircled{1} f_L = 0.5 (4g) = 20 \text{ N}$$

$$\textcircled{2} a = \frac{60 - 20}{6 + 4} = 4 \text{ m/s}^2$$

$$\textcircled{3} T = 6(g - 4) = 36 \text{ N}$$

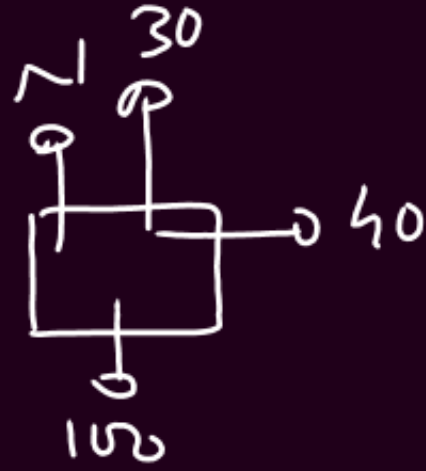
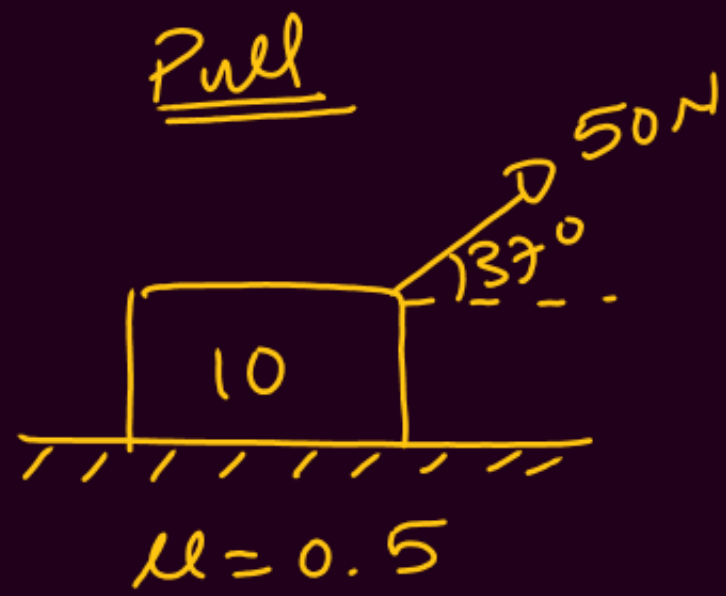


$$\textcircled{1} f_L = 0.5 (20) = \underline{10 \text{ N}}$$

$$\textcircled{2} a = \frac{60 - 40 - 10}{6 + 4 + 2} = \underline{\underline{5/6 \text{ m/s}^2}}$$

$$\textcircled{3} T_1 = 4(g + 5/6)$$

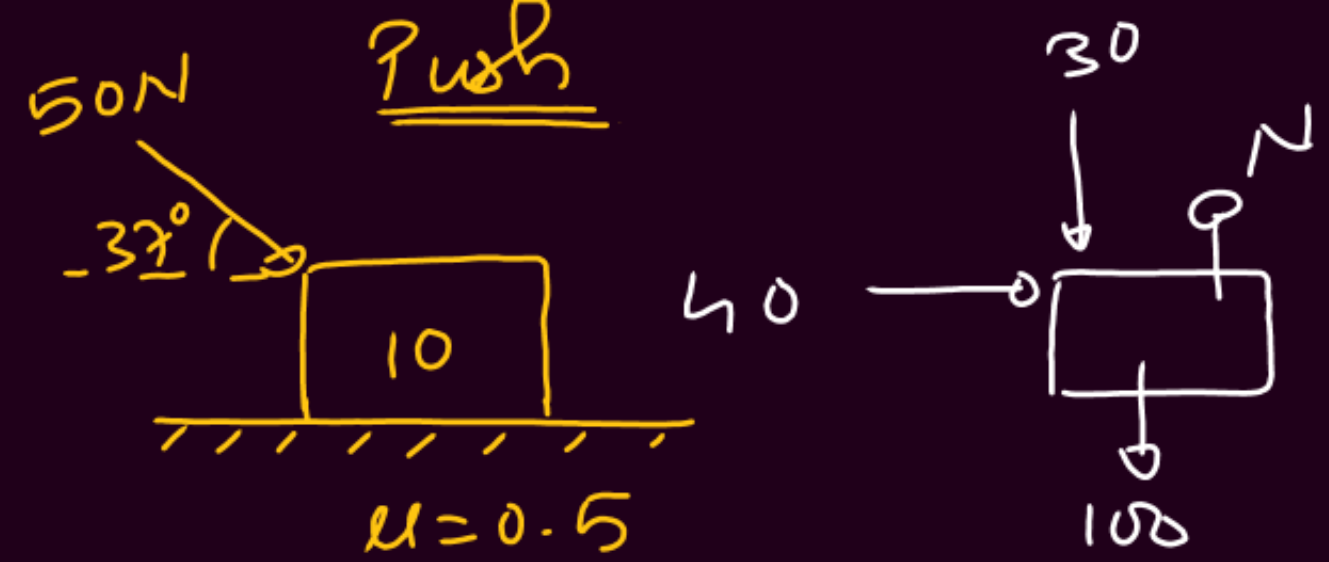
$$\textcircled{4} T_2 = 6(g - 5/6)$$



$$\textcircled{1} N = 100 - 30 = 70 \text{ N}$$

$$\textcircled{2} f_L = 0.5(70) = 35 \text{ N}$$

$$\textcircled{3} a = \frac{40 - 35}{10} = 0.5 \text{ m/s}^2$$



$$\textcircled{1} N = 100 + 30 = 130 \text{ N}$$

$$\textcircled{2} f_L = 0.5(130) = 65 \text{ N}$$

$$\textcircled{3} a = 0 \text{ (Rest)}$$

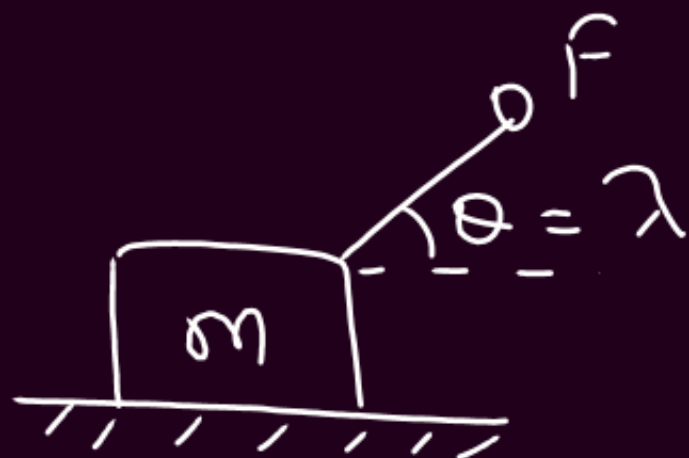
$$\textcircled{4} f_s = 40 \text{ N}$$

①



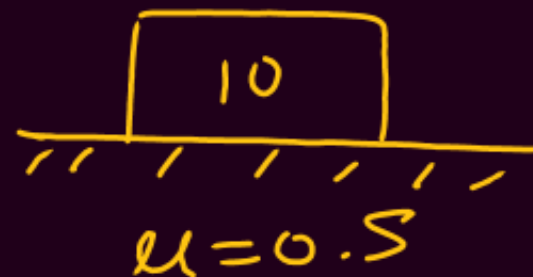
$$F = \mu mg$$

②



$$F_{\min} = \frac{\mu mg}{\sqrt{1 + \mu^2}}$$

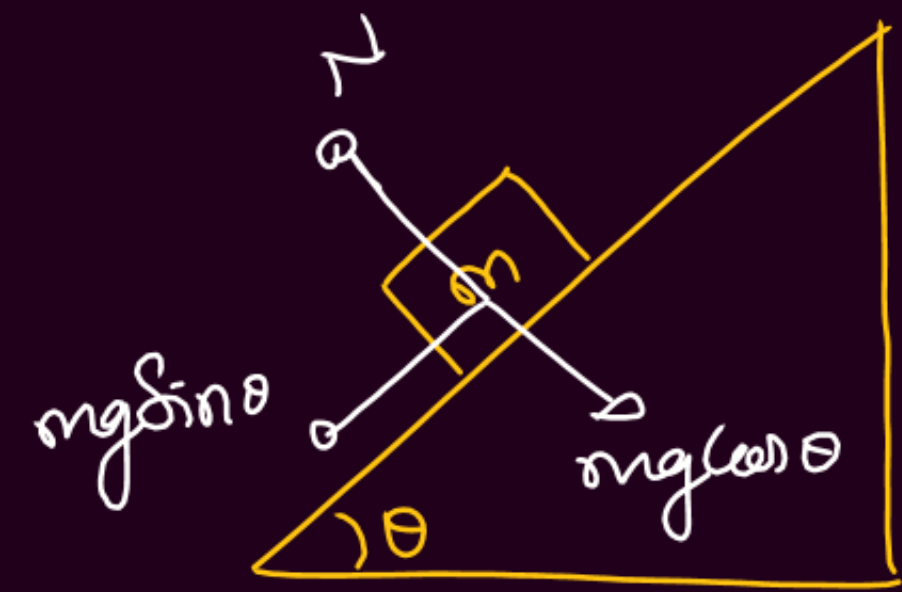
Q.11



① Min Horizontal $F = 0.5(100) = 50\text{N}$

② Min force $F = \frac{0.5(100)}{\sqrt{1 + (0.5)^2}} \approx \frac{50}{1.1}$

Friction on Inclined Plane



$$① N = mg \cos \theta$$

$$② f_l = \mu mg \cos \theta$$

if ① $mg \sin \theta \leq f_l$ $f_s = mg \sin \theta$

② $mg \sin \theta > f_l$ $f_k = \mu mg \cos \theta$

Angle of Repose (α)



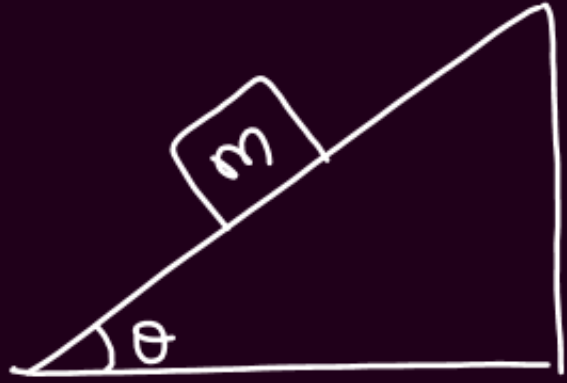
just

$$\tan \alpha = \mu = \tan \lambda$$

$$① \tan \theta \leq \mu \quad \text{Rest}$$

$$② \tan \theta > \mu \quad \text{Acc.}$$

① $\tan \theta \leq \mu$



① Rest

② $f_s = mg \sin \theta$

③ $R = mg$

$$R = \sqrt{N^2 + f^2} = \sqrt{(mg \cos \theta)^2 + (mg \sin \theta)^2}$$



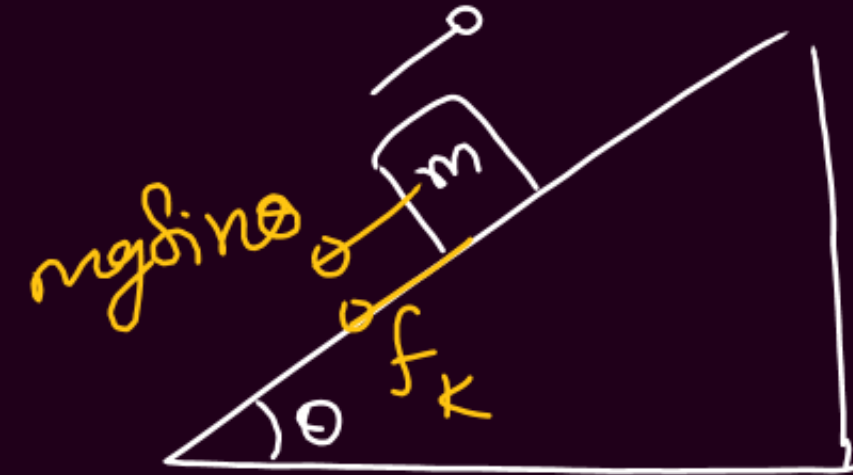
② $\tan \theta > \mu$



$$a = \frac{mg \sin \theta - \mu mg \cos \theta}{m}$$

$$a = g(\sin \theta - \mu \cos \theta)$$

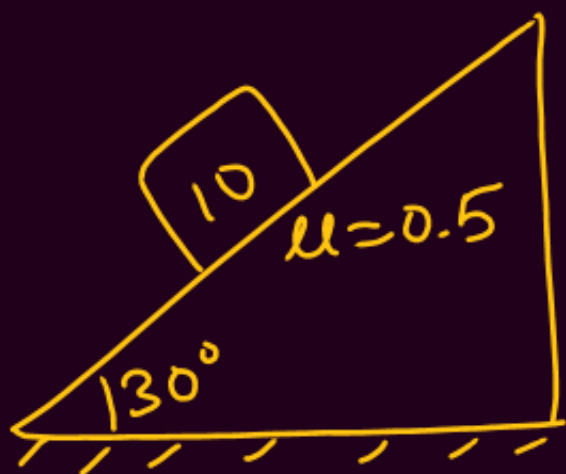
③ Projected Up



Retard

$$a = g(\sin \theta + \mu \cos \theta)$$

Q.



$$\tan 30^\circ = \frac{1}{\sqrt{3}} = 0.577$$

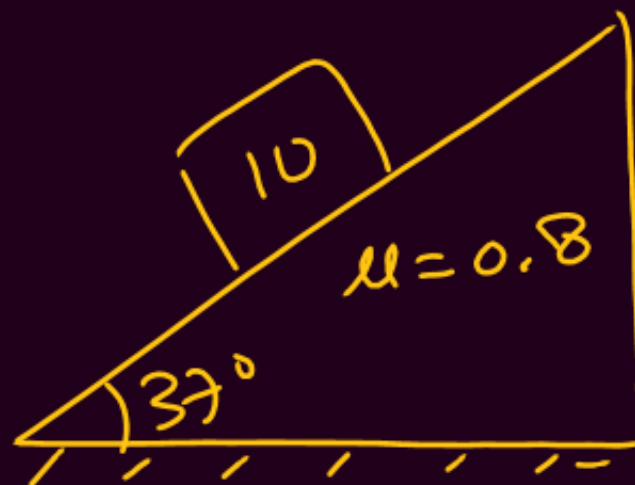
$$\tan \theta > \mu$$

$$f_k = (0.5)(100 \cos 30^\circ)$$

$$a = g(\sin 30^\circ - 0.5 \cos 30^\circ)$$

$$\frac{1}{\sqrt{2}} = 0.707$$

$$\frac{1}{\sqrt{3}} = 0.577$$



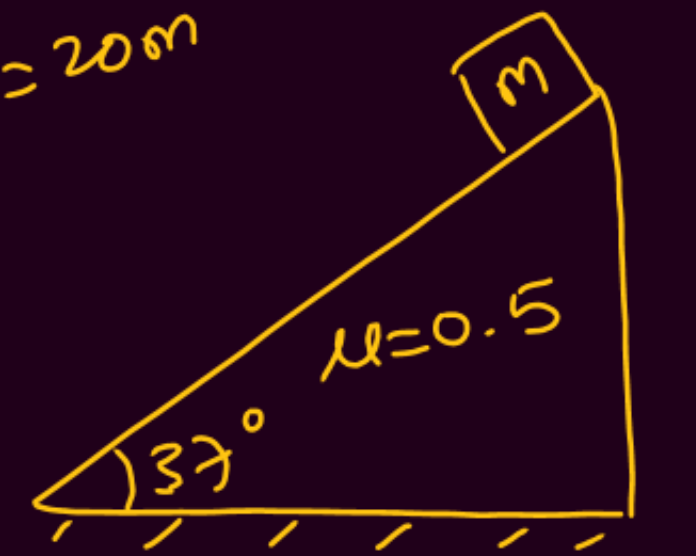
$$\tan 37^\circ = \frac{3}{4} < \mu$$

Rest

$$f_s = 10g \sin 37^\circ = 60 \text{ N}$$

$$a = 0$$

$$l = 20 \text{ m}$$



Bottom

$$v = ? \quad t = ?$$

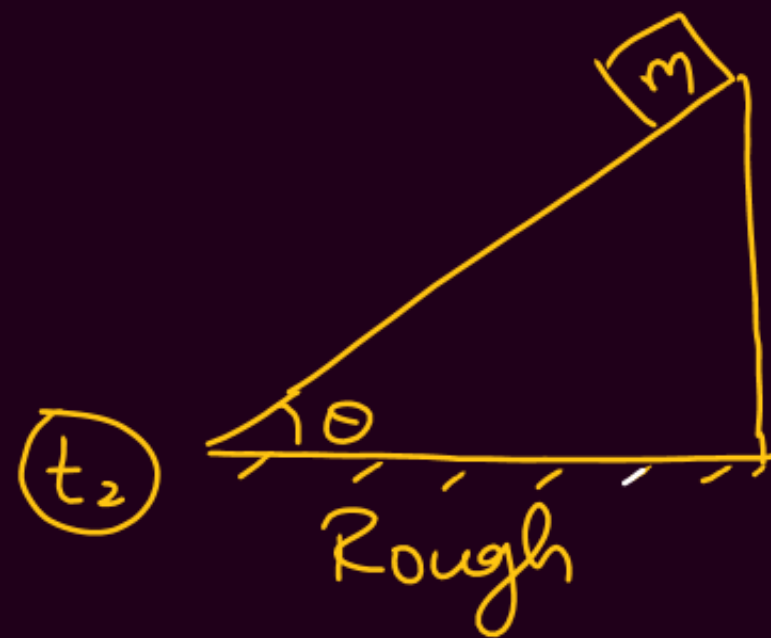
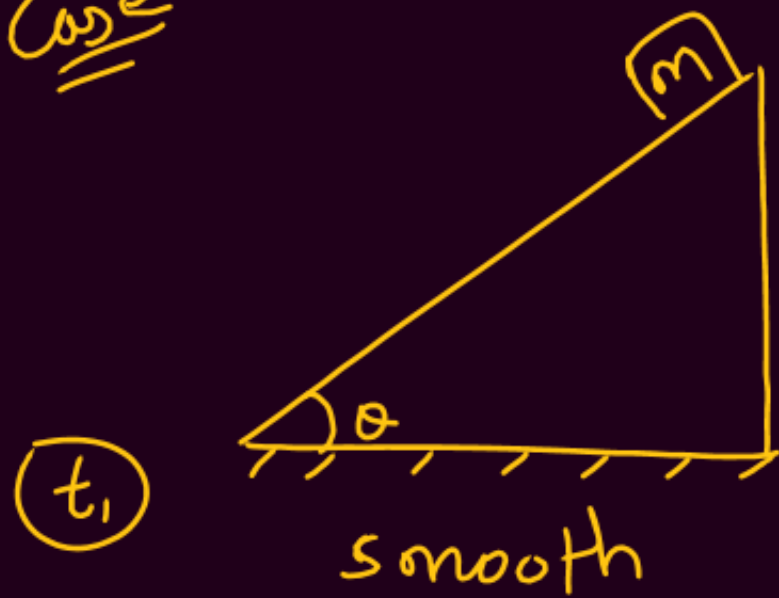
$$\textcircled{1} a = 10 \left(\frac{3}{5} - 0.5 \left(\frac{4}{5} \right) \right) = 2 \text{ m/s}^2$$

$$\textcircled{2} v = \sqrt{2 \times 2 \times 20} = 4\sqrt{5} \text{ m/s}$$

$$\textcircled{3} 20 = \frac{1}{2}(2)t^2$$

$$t = 2\sqrt{5} \text{ s}$$

Case



then

$$t_2 = n t_1$$

$$\mu = \tan \theta \left(1 - \frac{1}{n^2} \right)$$

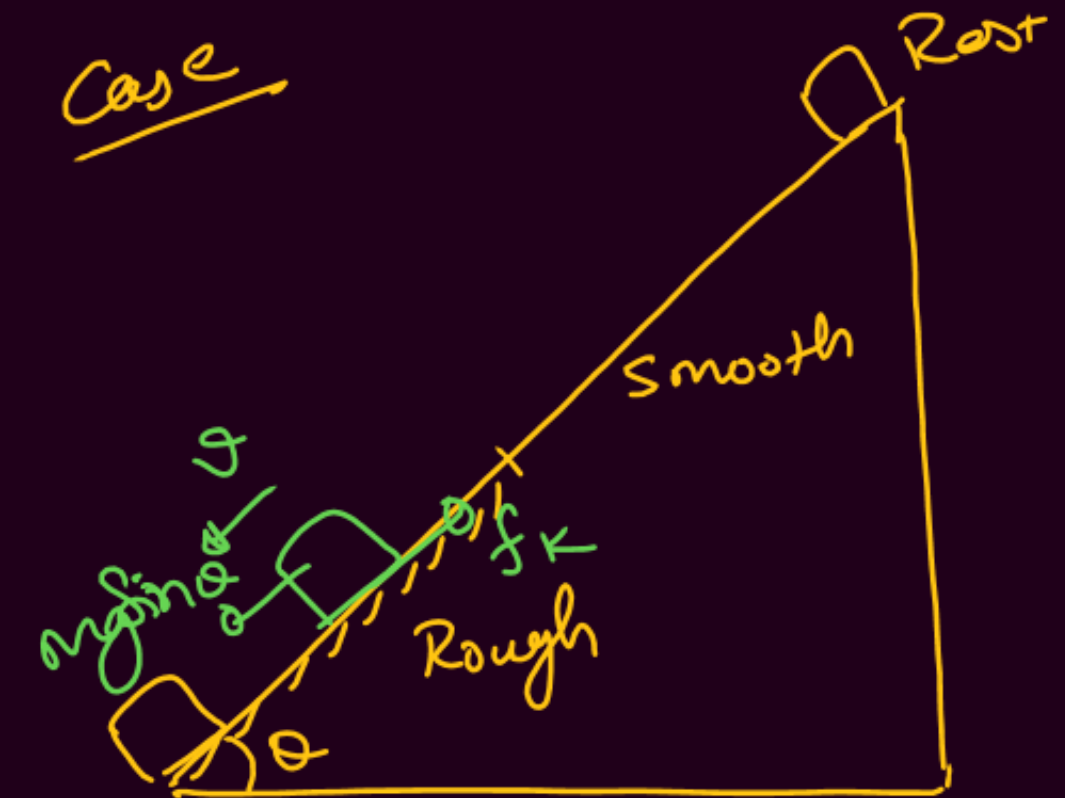
$$l_1 = l_2$$

$$\frac{1}{2} g \sin \theta t_1^2 = \frac{1}{2} g (\sin \theta - \mu \cos \theta) t_2^2$$

$$\sin \theta = (\sin \theta - \mu \cos \theta) n^2$$

$$\tan \theta = (\tan \theta - \mu) n^2$$

Case



Just reaches the Bottom

$$\mu = 2 \tan \theta$$

$$v^2 = 2a_1x_1 = 2a_2x_2$$

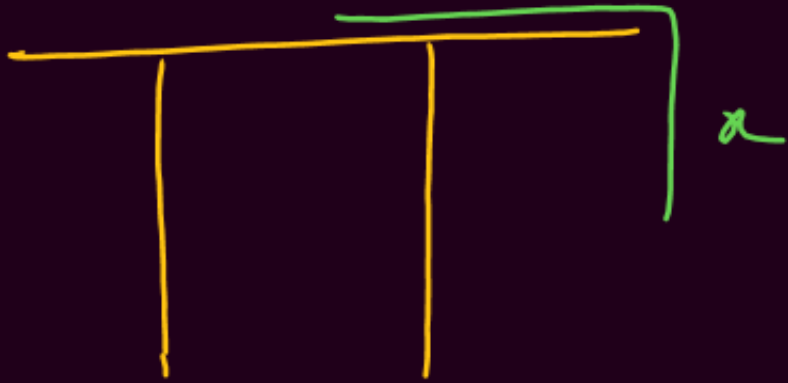
$$a_1 = a_2$$

$$g \sin \theta = g(\mu \cos \theta - \sin \theta)$$

$$\sin \theta = \mu \cos \theta - \sin \theta$$

$$2 \sin \theta = \mu \cos \theta$$

Uniform Rope / Chain



Max length that can be
Hanged

$$x = \frac{\mu l}{\mu + 1}$$

$$\left(\frac{m}{l} x\right) g = \mu \frac{m}{l} (l - x) g$$

Q. $m = 4 \text{ kg}$
 $l = 1 \text{ m}$
 $\mu = 0.5$

$$x = \frac{0.5(1)}{1 + 0.5} = \frac{0.5}{1.5} = \frac{1}{3} \text{ m}$$

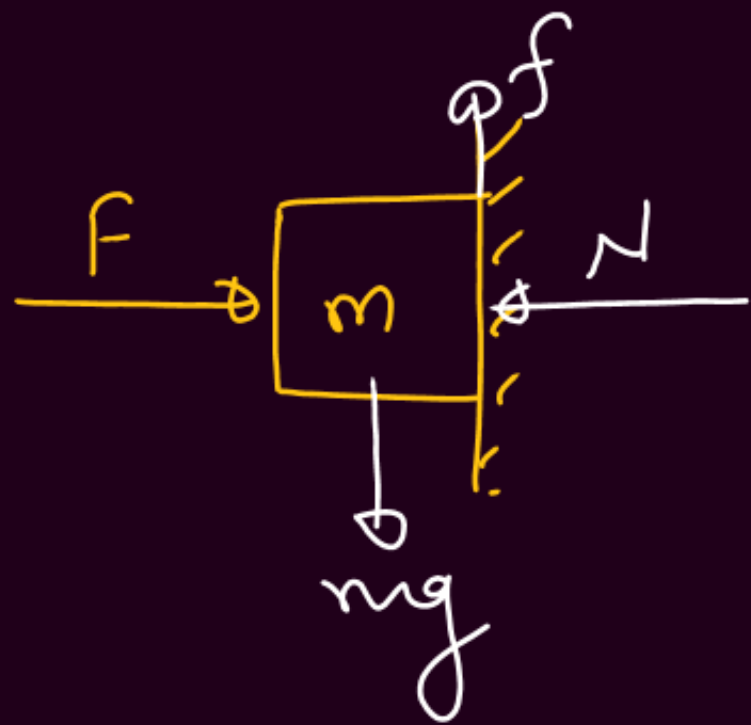
Q. max 25%

$$l \left(\frac{25}{100} \right) = \frac{\mu l}{\mu + 1}$$

$$\mu + 1 = 4 \mu$$

$$\mu = \frac{1}{3}$$

Block Pressed against Wall



① $N = F$

② $f_L = \mu F$

Just

$$mg = \mu F$$

$$F = \frac{mg}{\mu}$$

If

① $F \geq \frac{mg}{\mu}$

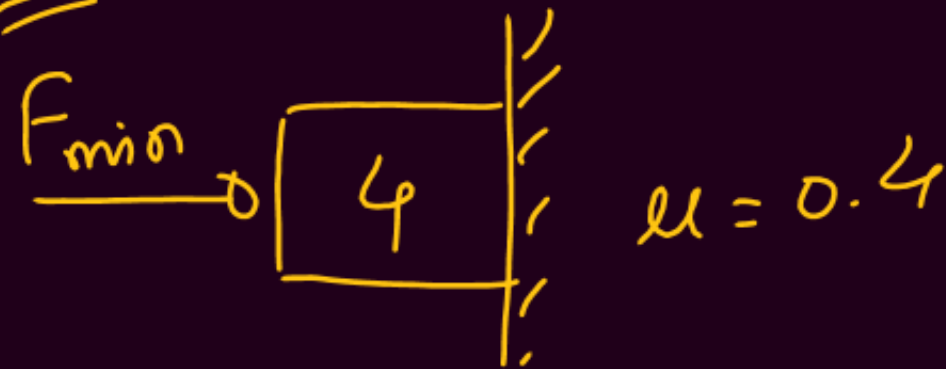
Rest $f_s = mg$

② $F < \frac{mg}{\mu}$

a $f_k = \mu F$

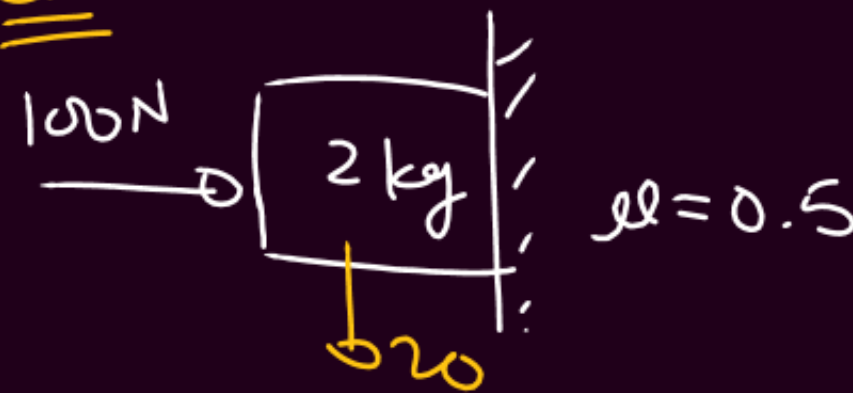
$$\text{Rest } F \geq \frac{mg}{\mu}$$

Q



$$F_{\min} = \frac{mg}{\mu} = \frac{40}{0.4} = 100 \text{ N}$$

Q



$$f = ?$$

$$a = ?$$

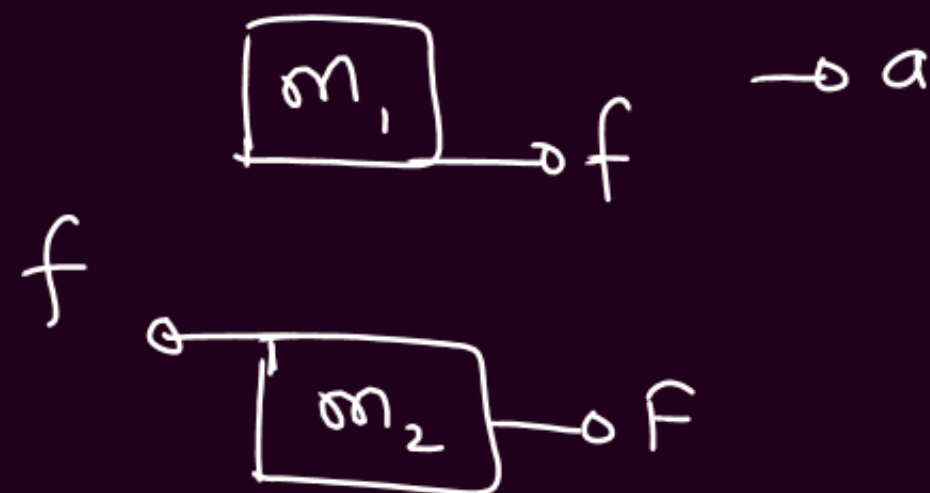
① $N = 100 \text{ N}$

② $f_L = 0.5(100) = 50 \text{ N}$

③ $f_s = mg = \underline{\underline{20 \text{ N}}}$

④ $a = 0$

Two Block

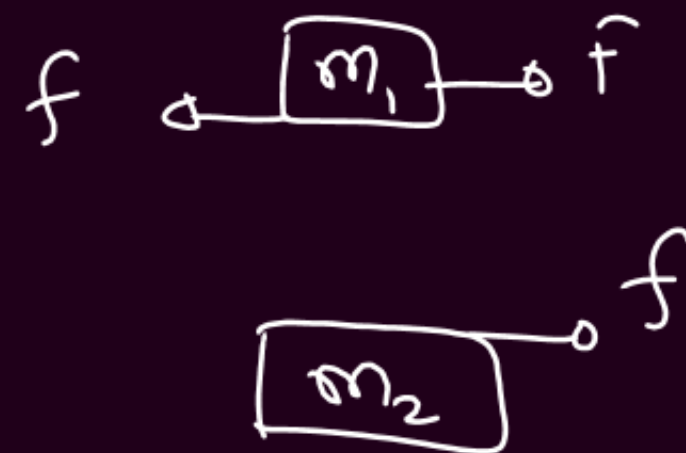
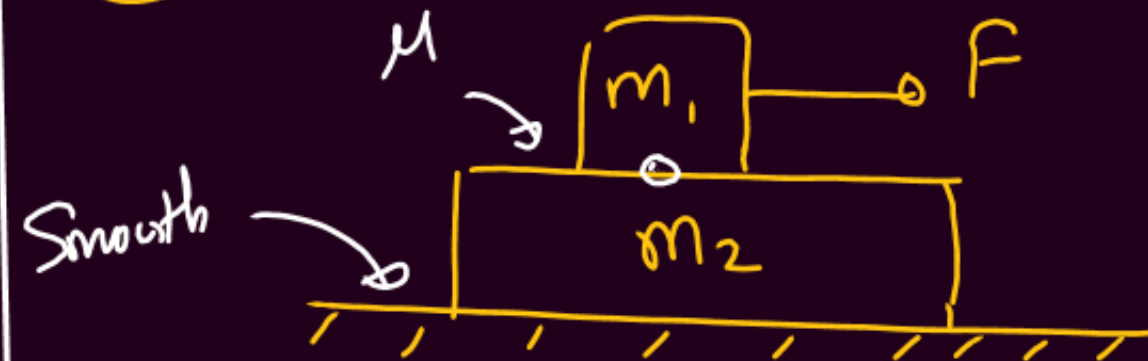


[max Acc for no Rel Motion]

$$a_{\max} = \mu g$$

$$f_{\max} = \mu m_1 g$$

② Extra



$$a_{\max} = \frac{\mu m_1 g}{m_2}$$



① $a = 1 \text{ m/s}^2$

$$f = 4(1) = 4 \text{ N}$$

Diagram showing a single block labeled '4' with one wheel underneath it. An arrow labeled 'f' points to the right, and the equation $f = ma$ is written below it.

$$a_{\text{max}} = \mu g = 0.2(10) = 2 \text{ m/s}^2$$

② $a = 4 \text{ m/s}^2$

$$f_k = \mu mg = 0.2(4g) = \underline{\underline{8 \text{ N}}}$$

$$(3) \quad v^2 = 2as$$

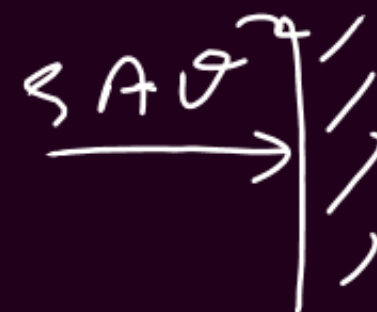
$$(100)^2 = 2 \frac{F}{\left(\frac{5}{1000}\right)} \left(\frac{6}{100}\right)$$



$$2T \cos \theta = Mg$$

$$2mg \cos \theta = Mg$$

$$\cos \theta = \frac{M}{2m} < 1$$



§

$$\frac{26N}{10} = 2.6m$$

$$\frac{m(g+a)}{g}$$