

Work - Energy & Power

Work

$$W = \int \vec{F} \cdot d\vec{s} = \int F ds \cos \theta$$

$$\theta = 90^\circ$$

$$W = 0$$

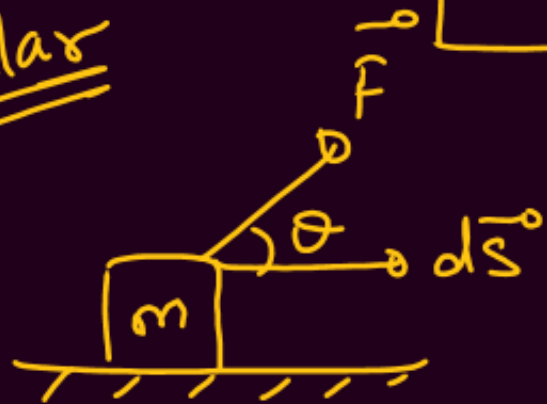
$$0 \leq \theta < 90^\circ$$

$$W = (+)$$

$$90^\circ < \theta \leq 180^\circ$$

$$W = (-)$$

Scalar



Special Case $\vec{F} = \text{const}$

$$W = \vec{F} \cdot \vec{s} = F s \cos \alpha$$

Unit J (SI)

erg (CGS)

$$① 1 \text{ cal} = 4.2 \text{ J}$$

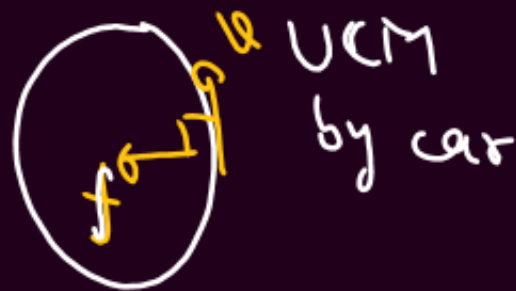
$$② 1 \text{ J} = 10^7 \text{ erg}$$

$$[W] = [ML^2 T^{-2}]$$

① If $\vec{s} = 0$ then W may be non-zero



② W_f $\oplus / \ominus$



③ $W_{\text{internal forces}}$ may be non-zero

$$\oplus \frac{F}{s_1} \quad \frac{F}{s_2} \ominus$$

④ W depends on f or R

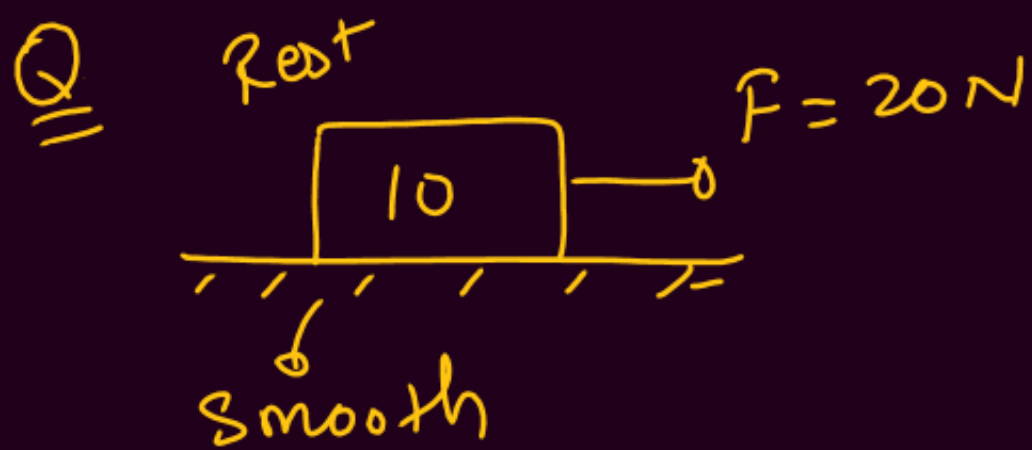
⑤ P+ of app at Rest $W = 0$

- walking / Running
- Rope climbing
- Stair

$$W_f = 0$$

$$W_T = 0$$

$$W_N = 0$$



w by F in 2s

$$\begin{cases} W = F S \cos 0^\circ \\ = (20)(4)(1) \\ = \underline{\underline{80 \text{ J}}} \end{cases}$$

$$a = 2 \text{ m/s}^2$$

$$S = \frac{1}{2}(2)(2)^2$$

$$W_N = 0$$

$$W_{\text{mg}} = 0$$



w by F in 2s

$$a = \frac{40}{10} = 4 \text{ m/s}^2$$

$$S = \frac{1}{2}(4)(2)^2 = 8 \text{ m}$$

$$\begin{aligned} W &= F S \cos 37^\circ \\ &= 50(8) \frac{4}{5} \end{aligned}$$

$$= 40(8)$$

$$= \underline{\underline{320 \text{ J}}}$$



① w by T on 4 kg in 2s

$$a = \frac{6g}{10} = 6 \text{ m/s}^2$$

$$S = \frac{1}{2}(6)(2)^2 = 12 \text{ m}$$

$$T = 4(6) = 24 \text{ N}$$

$$W = T S = 24(12) = \underline{\underline{288 \text{ J}}}$$

② w by T on 6 kg in 2s

$$W = -(24)(12) = \underline{\underline{-288 \text{ J}}}$$

Q $\vec{F} = (3\hat{i} - 2\hat{j} + \hat{k}) \text{ N}$

$$\vec{S} = (\hat{i} - \hat{j} + 2\hat{k}) \text{ m}$$

$W = ?$

$$W = \vec{F} \cdot \vec{S}$$

$$W = (3)(1) + (-2)(-1) + (1)(2)$$

$$\underline{W = 7 \text{ J}}$$

Q Displaced from $(1, -1, 2)$ to $(0, 2, -1)$
 $\hat{i}$ $\hat{j}$ $\hat{k}$

$$\vec{F} = (2\hat{i} - 3\hat{j} + 4\hat{k}) \text{ N}$$

$W = ?$

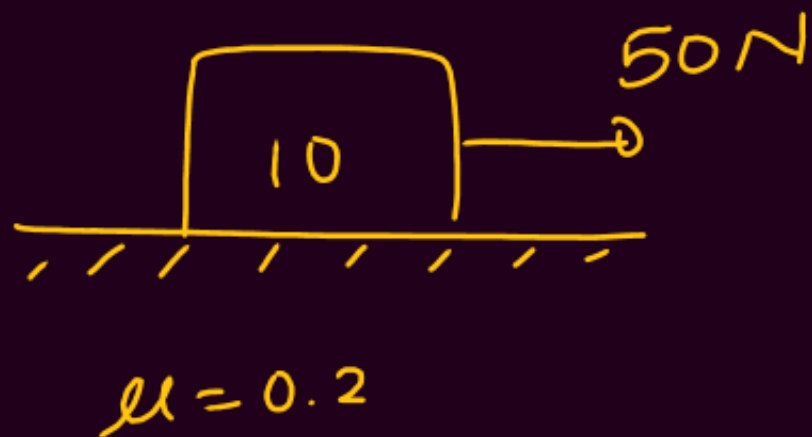
$$\vec{S} = \vec{r}_f - \vec{r}_i = (0-1)\hat{i} + (2-(-1))\hat{j} + (-1-2)\hat{k}$$

$$\vec{S} = -\hat{i} + 3\hat{j} - 3\hat{k}$$

$$W = (2)(-1) + (-3)(3) + 4(-3)$$

$$\underline{W = -23 \text{ J}}$$

Q Rest



In 38

$$W_f = 50 \times \frac{27}{2} = 675 \text{ J}$$

$$W_f = -(20) \left(\frac{27}{2} \right) = -270 \text{ J}$$

$$W_N = 0$$

$$W_{mg} = 0$$

$$N = 100 \text{ N}$$

$$f_L = 0.2(100) = 20 \text{ N}$$

$$a = \frac{50 - 20}{10} = 3 \text{ m/s}^2$$

$$S = \frac{1}{2} (3) (3)^2 = 13.5 \text{ m}$$

Q: $F = 4x$

W in $x=1\text{m}$ to $x=3\text{m}$

$$W = \int F dx$$

$$W = \int 4x dx$$

$$W = \left[4 \frac{x^2}{2} \right]_1^3 = \left[2x^2 \right]_1^3$$

$$W = 2(3)^2 - 2(1)^2$$

$$\underline{W = 16\text{J}}$$

Q: $F = (3x^2 - 2x)$

W in displacing from $x=2\text{m}$ to $x=4\text{m}$

$$W = \int (3x^2 - 2x) dx$$

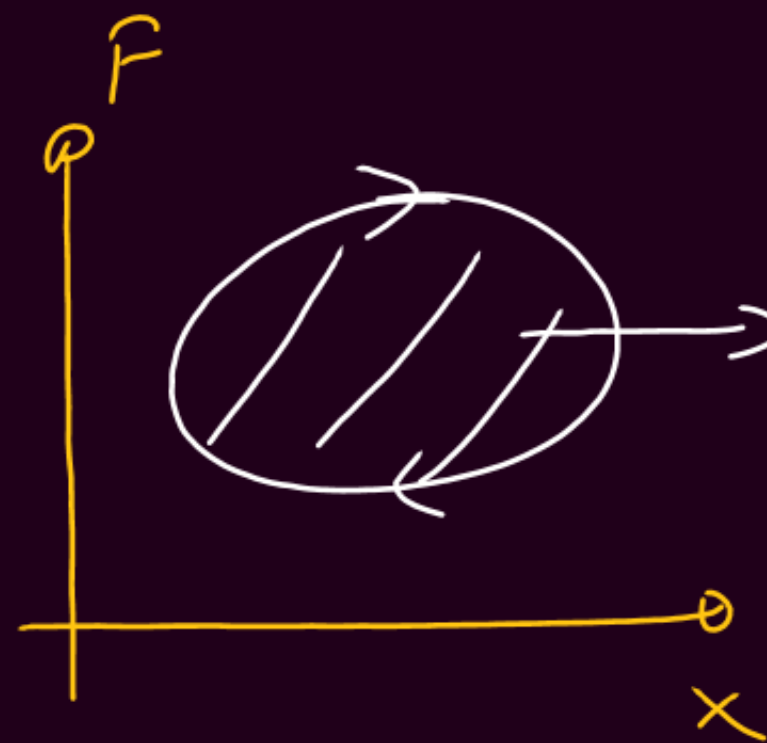
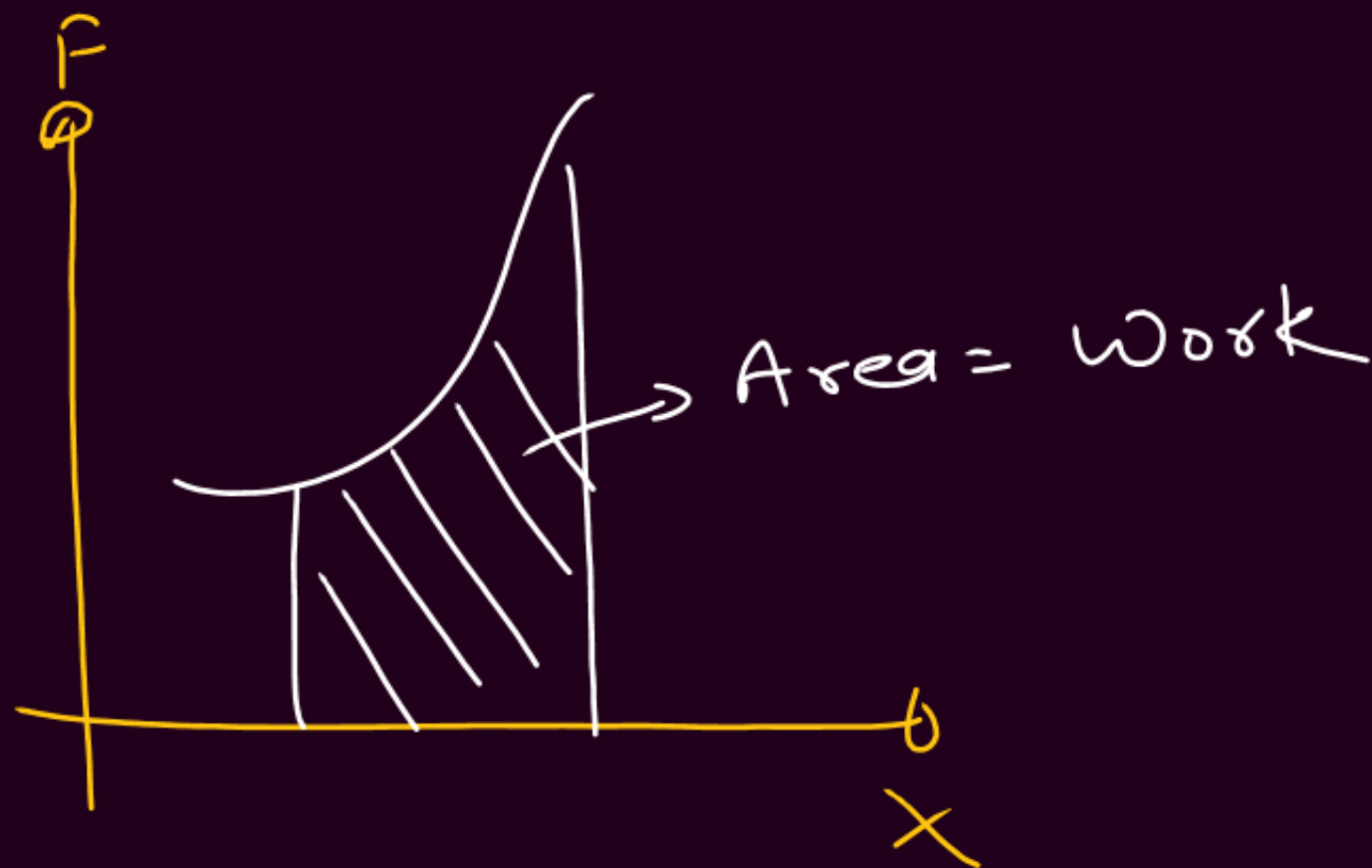
$$W = \left(3 \frac{x^3}{3} - 2 \frac{x^2}{2} \right) = \left[x^3 - x^2 \right]_2^4$$

$$W = (4^3 - 4^2) - (2^3 - 2^2)$$
$$= 48 - 4$$

$$\underline{= 44\text{J}}$$

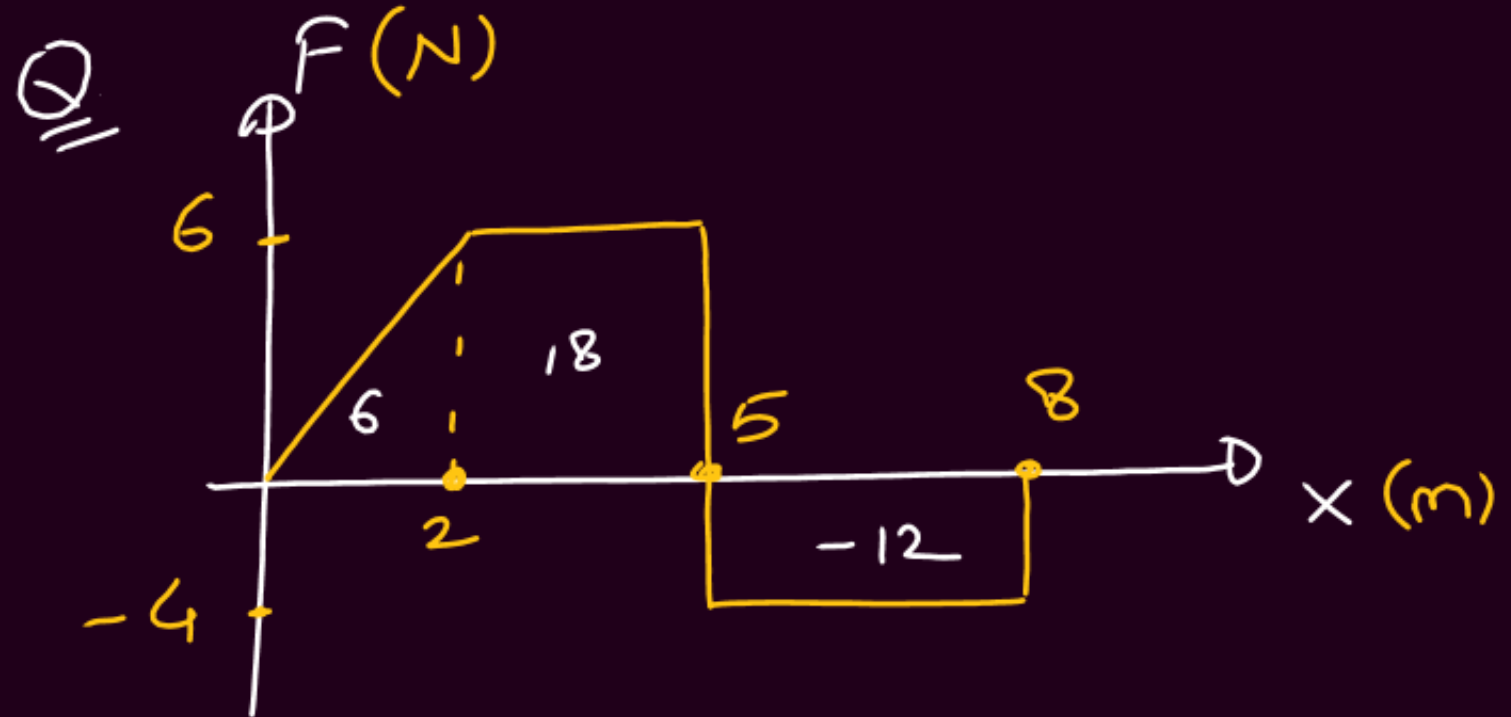
Graphs

$$W = \int F dx$$

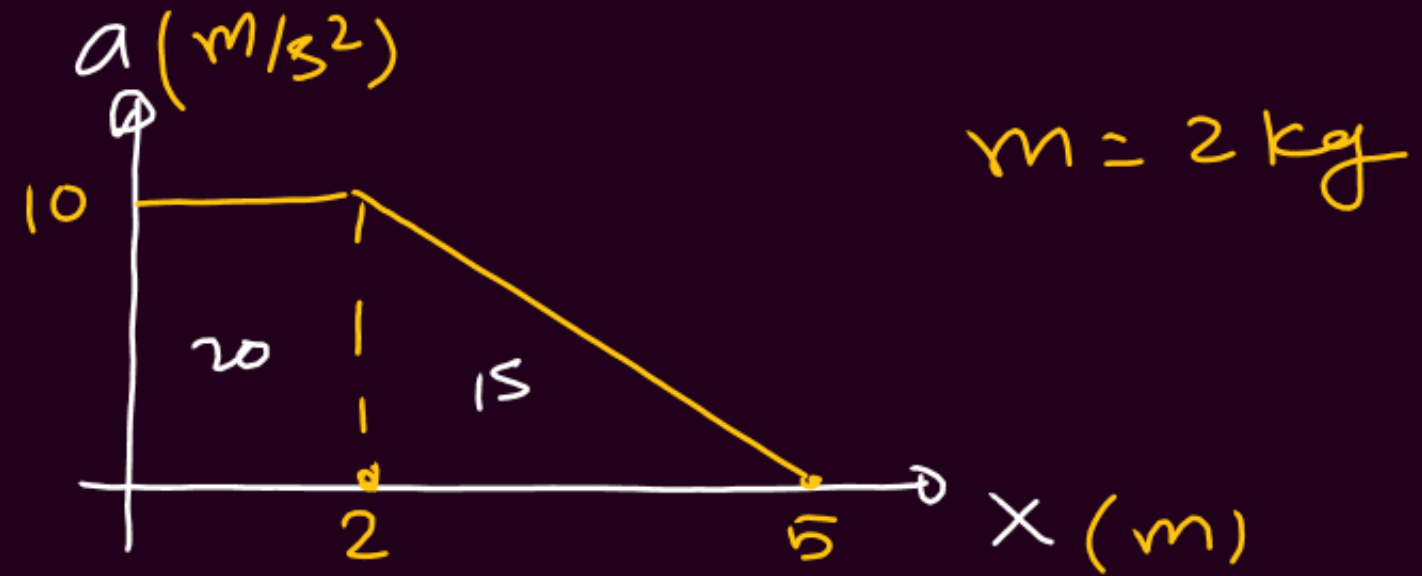


$$\text{Area} = W$$

CW	$W = \oplus$
ACW	$W = \ominus$



$$W = 6 + 18 - 12 = 12 \text{ J}$$



$$W = 2 [20 + 15] = 70 \text{ J}$$

Conservative & Non-conservative Forces

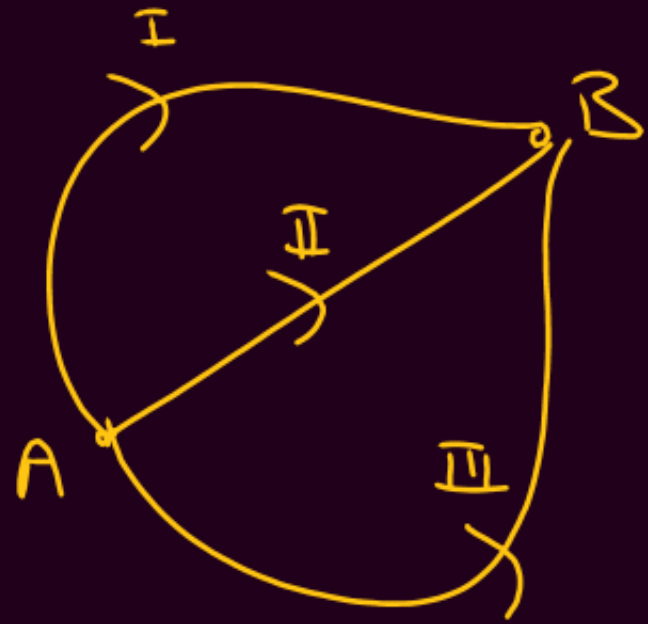
- W.D. is independent of path
- e.g. gr / electrostatic / Spring / Const F
- NCF → Friction / Air / Viscous

Conservative

- W.D. in closed path = 0
- depends only on i & f

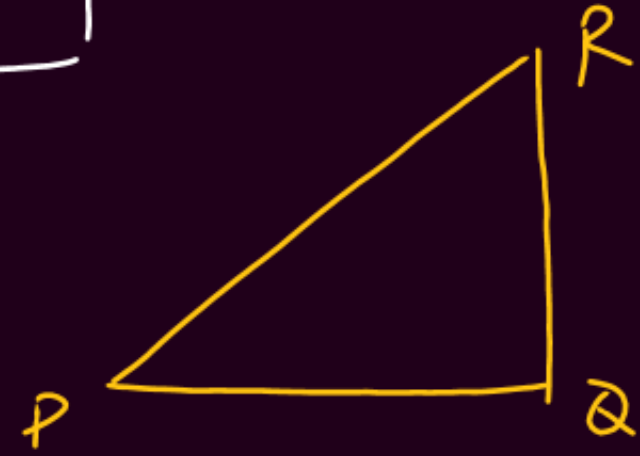


$$W_{B \rightarrow A} = -W_{A \rightarrow B}$$



$$W_I = W_{II} = W_{III}$$

If force is conservative

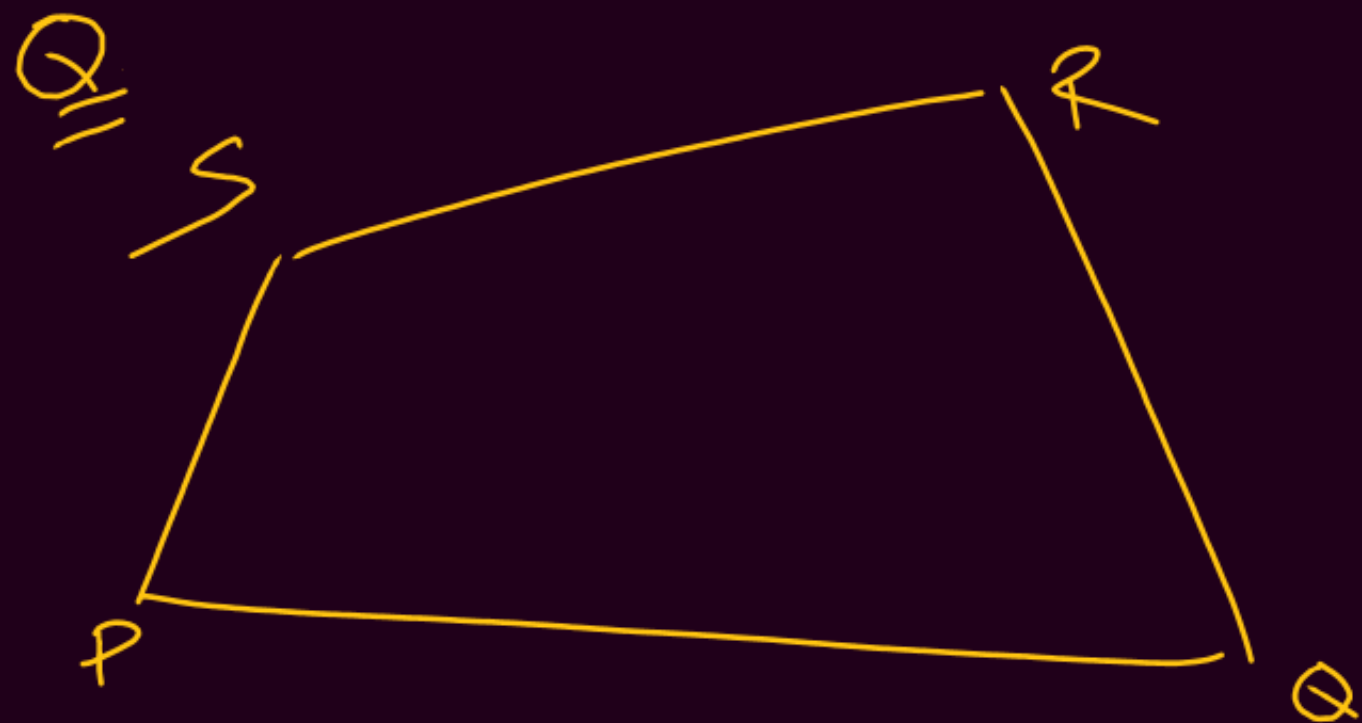


$$W_{P \rightarrow Q} = 3 \text{ J}$$

$$W_{Q \rightarrow R} = 4 \text{ J}$$

$$W_{P \rightarrow R} = ?$$

$$\begin{aligned} W_{P \rightarrow R} &= W_{P \rightarrow Q} + W_{Q \rightarrow R} \\ &= 3 + 4 = \underline{\underline{7 \text{ J}}} \end{aligned}$$



$$W_{P \rightarrow R} = 10 \text{ J}$$

$$W_{S \rightarrow P} = -5 \text{ J}$$

$$W_{S \rightarrow Q} = 6 \text{ J}$$

$$\begin{aligned} \textcircled{1} W_{P \rightarrow Q} &= (P \rightarrow S) + (S \rightarrow Q) \\ &= (+5) + 6 = \underline{\underline{11 \text{ J}}} \end{aligned}$$

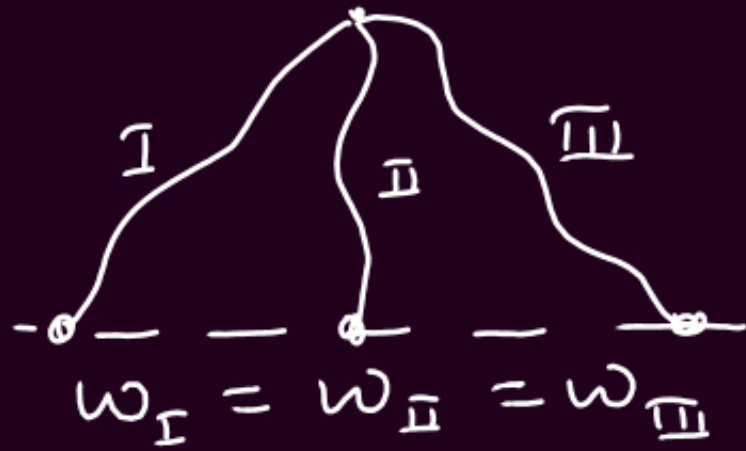
$$\begin{aligned} \textcircled{2} W_{S \rightarrow R} &= (S \rightarrow P) + (P \rightarrow R) \\ &= (-5) + 10 = \underline{\underline{5 \text{ J}}} \end{aligned}$$

$$\begin{aligned} \textcircled{3} W_{Q \rightarrow R} &= (Q \rightarrow S) + (S \rightarrow P) + (P \rightarrow R) \\ &= (-6) + (-5) + (10) \\ &= \underline{\underline{-1 \text{ J}}} \end{aligned}$$

Work done by Gravity

$$W = \pm mgh$$

$$\Delta U = \pm mgh$$



$$W_{mg} = mgh$$

$$\Delta U = -mgh$$



$$W_{mg} = -mgh$$

$$\Delta U = +mgh$$

Work done by Spring

$$F = -kx$$



$$W_{by} = -\frac{1}{2} k (x_f^2 - x_i^2)$$

$$\Delta U = \frac{1}{2} k (x_f^2 - x_i^2)$$

$$U = \frac{1}{2} k x^2 = \frac{1}{2} F x = \frac{F^2}{2k}$$

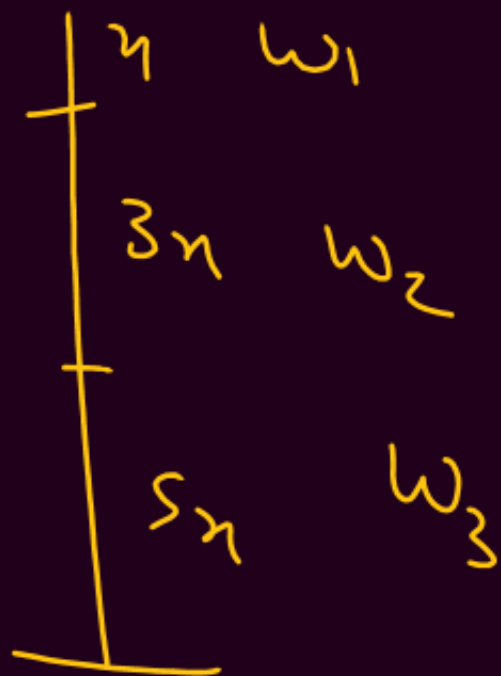
For successive equal extensions

$$W/\Delta U \quad 1:3:5:7$$

Pg-182
(2)

$$\frac{W_1}{W_2} = \frac{mgh}{mgh} = \frac{1}{1}$$

Pg-182
(9)



1:3:5

Pg-185
(2)

S → 10 J

Add. S → 30 J

Q.

by 10 cm

W_0

Additional

15 cm

$W = ?$

$$W_0 = \frac{1}{2} k (10)^2$$

$$W = \frac{1}{2} k (25^2 - 10^2)$$

$$W = \frac{W_0 (525)}{100}$$

$$W = \frac{21}{4} W_0$$

Same Extension

① Tension

$$\frac{T_1}{T_2} = \frac{k_1 x}{k_2 x}$$

$$\boxed{\frac{T_1}{T_2} = \frac{k_1}{k_2}}$$

② PE

$$\frac{U_1}{U_2} = \frac{\frac{1}{2} k_1 x^2}{\frac{1}{2} k_2 x^2}$$

$$\boxed{\frac{U_1}{U_2} = \frac{k_1}{k_2}}$$

Same Force/Tension

① Extension

$$k_1 x_1 = k_2 x_2$$

$$\boxed{\frac{x_1}{x_2} = \frac{k_2}{k_1}}$$

② PE

$$\frac{U_1}{U_2} = \frac{\frac{F^2}{2k_1}}{\frac{F^2}{2k_2}}$$

$$\boxed{\frac{U_1}{U_2} = \frac{k_2}{k_1}}$$

Same PE

① Extension

$$\frac{1}{2} k_1 x_1^2 = \frac{1}{2} k_2 x_2^2$$

$$\boxed{\frac{x_1}{x_2} = \sqrt{\frac{k_2}{k_1}}}$$

② Tension

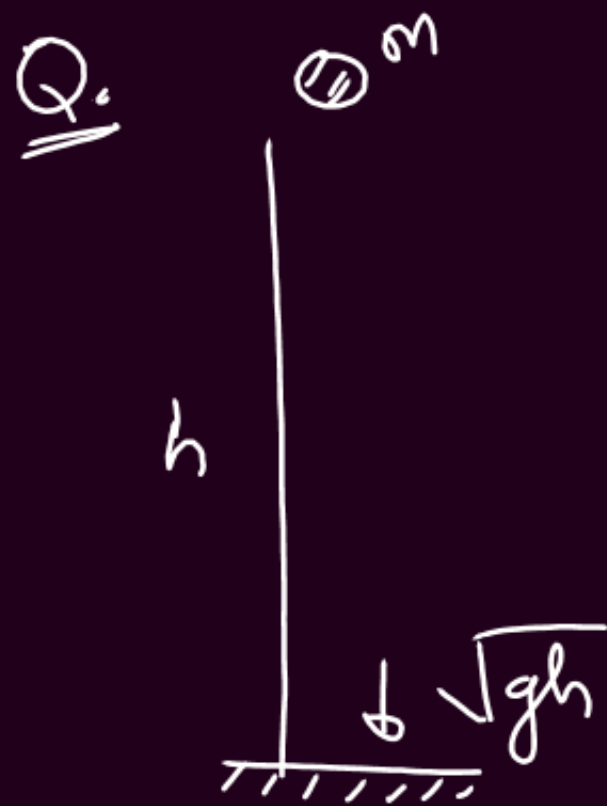
$$\frac{\frac{F_1^2}{2k_1}}{\frac{F_2^2}{2k_2}} = \frac{F_1^2}{2k_1} = \frac{F_2^2}{2k_2}$$

$$\boxed{\frac{F_1}{F_2} = \sqrt{\frac{k_1}{k_2}}}$$

Work-Energy Theorem

$$W_{\text{by all}} = \Delta K$$

(internal + external)



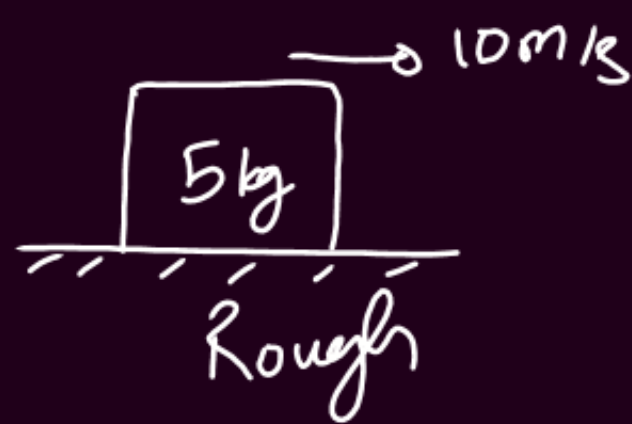
$$W_{\text{air}} = ?$$

$$W_{\text{air}} + W_{\text{gr}} = \Delta K$$

$$W_{\text{air}} + mgh = \frac{1}{2}m(gh) - 0$$

$$W_{\text{air}} = -\frac{mgh}{2}$$

Q



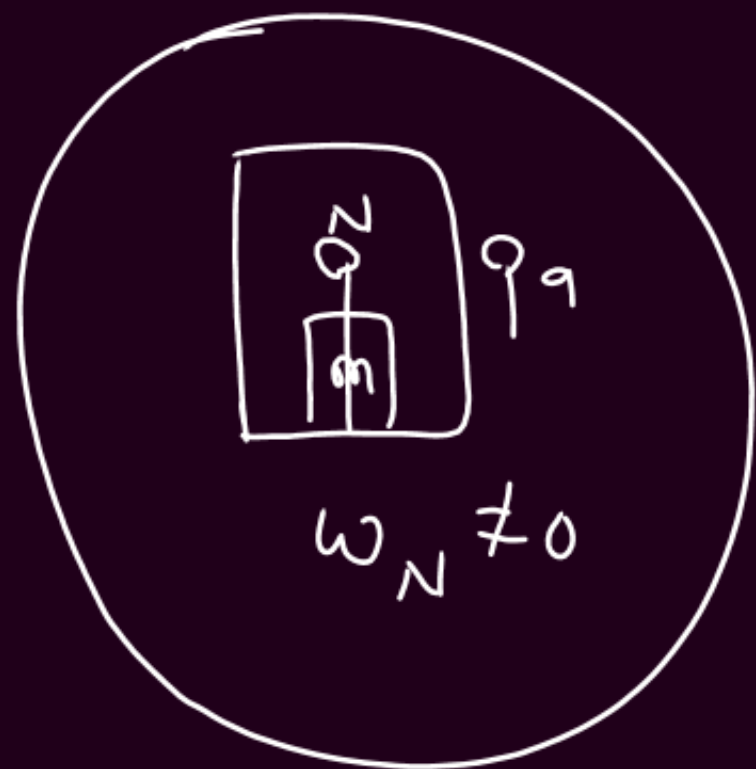
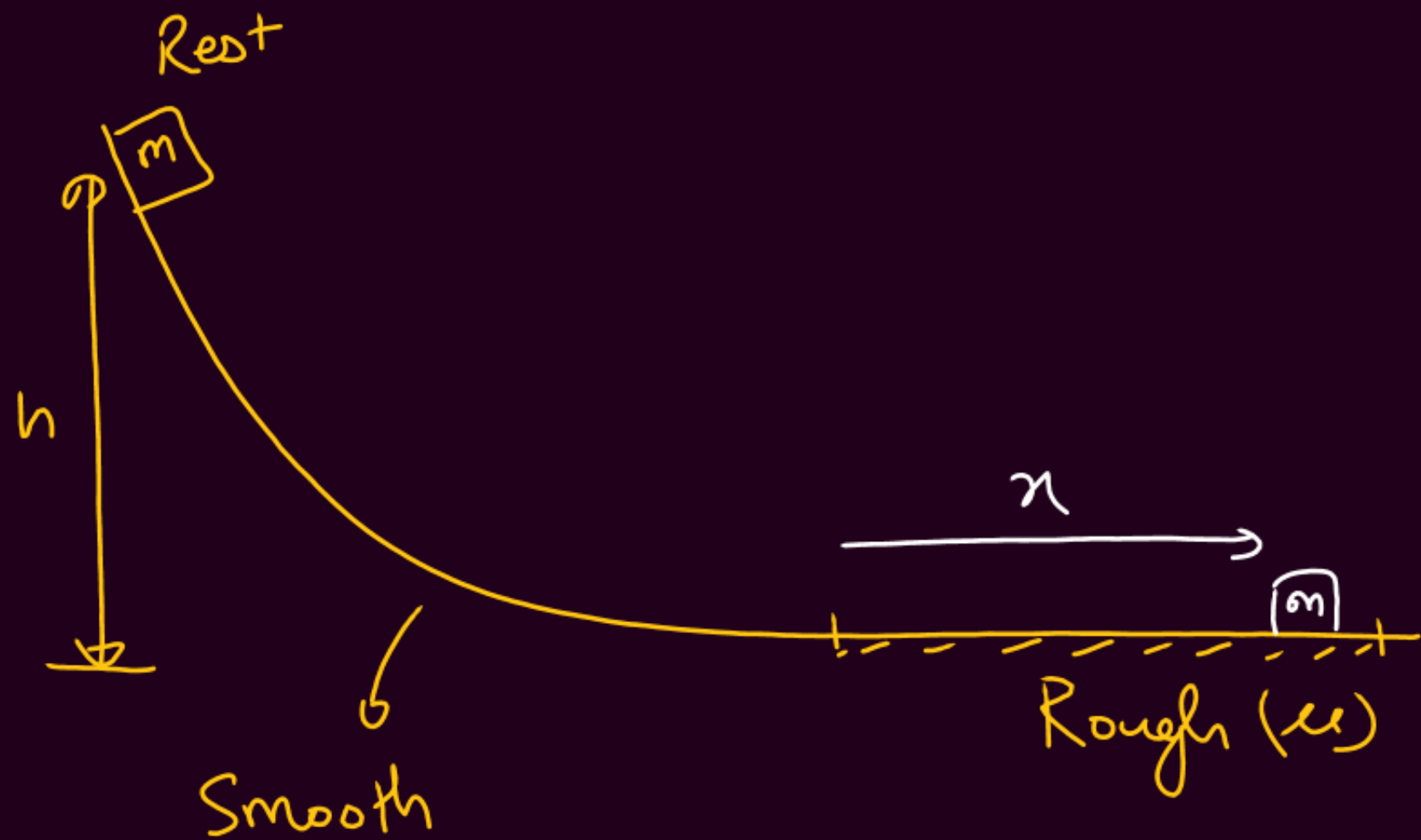
$$W_{\text{fr}} = ?$$

$$W_{\text{mg}} + W_{\text{N}} + W_{\text{fr}} = \Delta K$$

$$0 + 0 + W_{\text{fr}} = 0 - \frac{1}{2}(5)(10)^2$$

$$W_{\text{fr}} = -250 \text{ J}$$

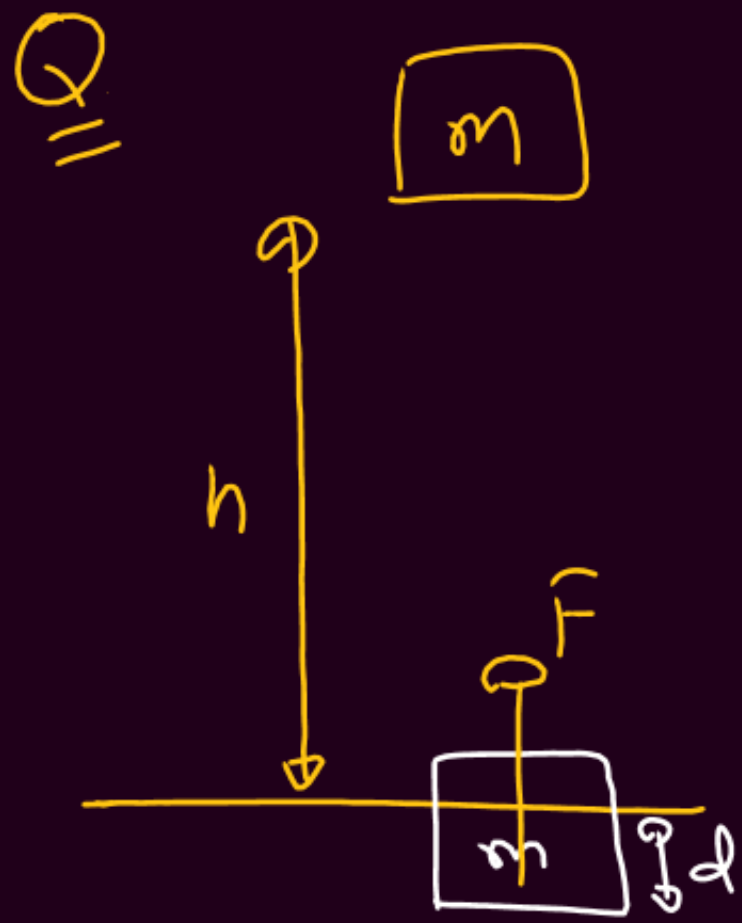
Q.11



$$W_{gr} + W_N + W_{fr} = \Delta K$$

$$mgh + 0 - \mu mg x = 0 - 0$$

$$x = \frac{h}{\mu}$$



Find force exerted
by floor?

$$W_{gr} + W_{floor} = \Delta K$$

$$mg(h+d) - Fd = 0 - 0$$

$$F = \frac{mg(h+d)}{d}$$

$$F = mg \left(1 + \frac{h}{d} \right)$$

Q. $x = (t^2 - 2t + 1) \text{ m}$

$m = 2 \text{ kg}$

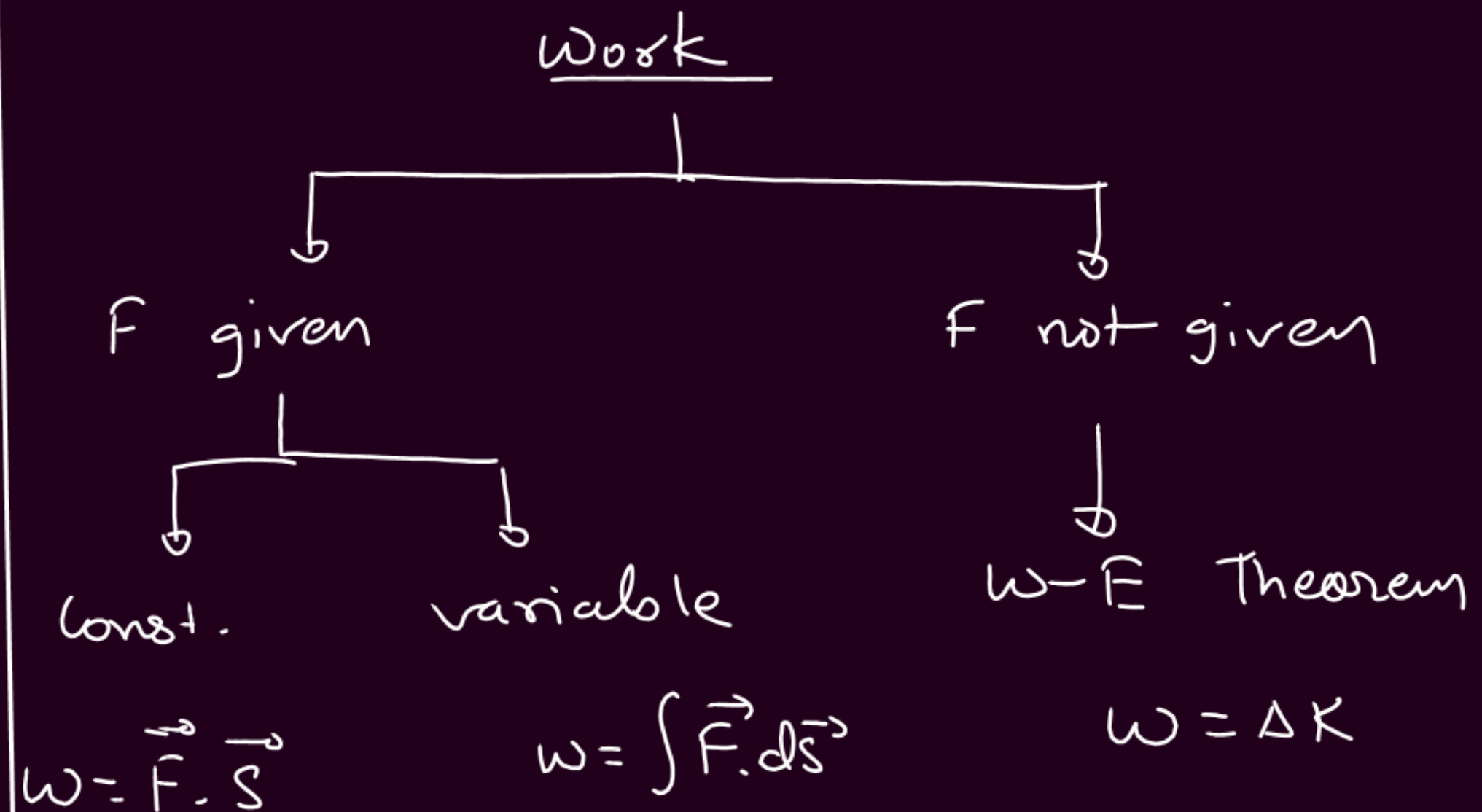
w.p. in 2s

$$v = (2t - 2)$$

$t = 0 \quad v = -2$

$t = 2 \quad v = +2$

$$W = \Delta K = \frac{1}{2} m (2^2 - 2^2) = 0$$



Q $v = (t^2 - 2t + 1) \text{ m/s}$

$m = 2 \text{ kg}$

W in 2s ?

$t = 0 \quad v_1 = 1$

$t = 2 \quad v_2 = 1$

$$W = \frac{1}{2} (2) (1^2 - 1^2) = 0$$

Q $v = (x^2 + 2)$

$m = 1 \text{ kg}$

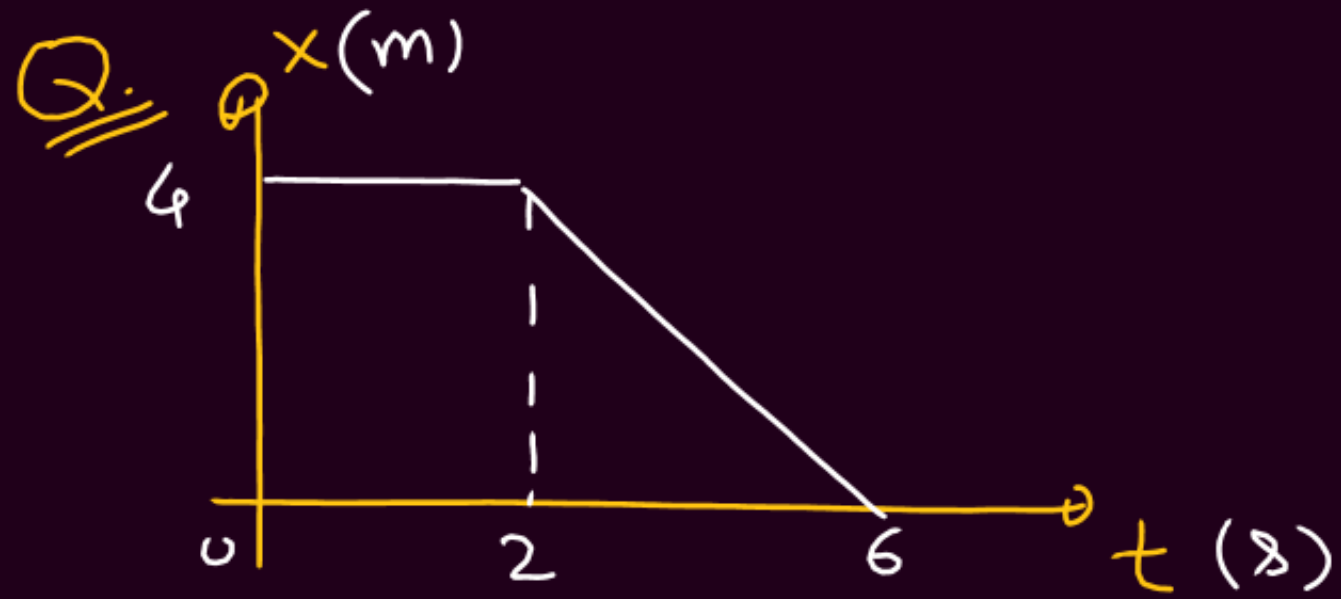
W.D from $x = 1 \text{ m}$ to $x = 2 \text{ m}$

$x = 1 \quad v = 3$

$x = 2 \quad v = 6$

$$W = \frac{1}{2} (1) (6^2 - 3^2)$$

$$W = \frac{36 - 9}{2} = \frac{27}{2} = \underline{13.5 \text{ J}}$$



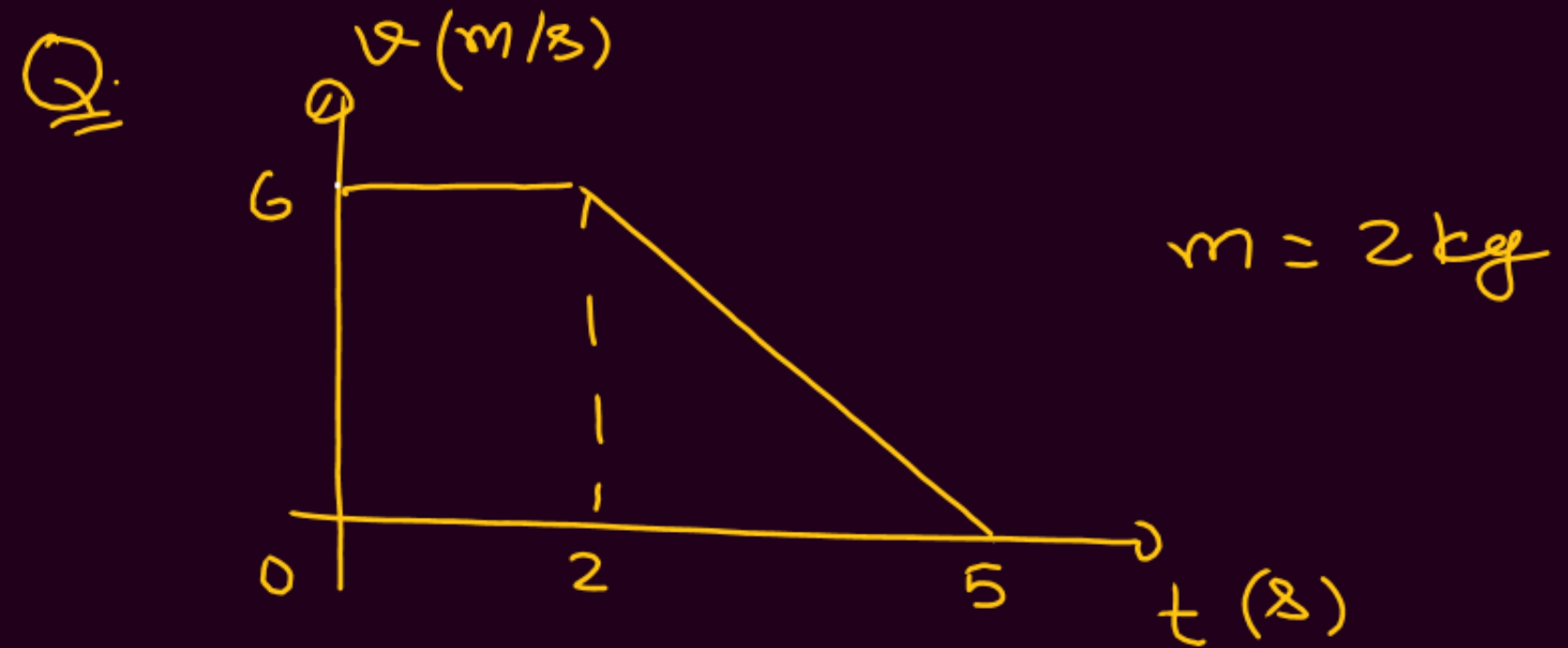
$$m = 2 \text{ kg}$$

W.D. in 5s?

$$t = 0 \quad v = 0$$

$$t = 5 \quad v = -\frac{4}{4} = -1 \text{ m/s}$$

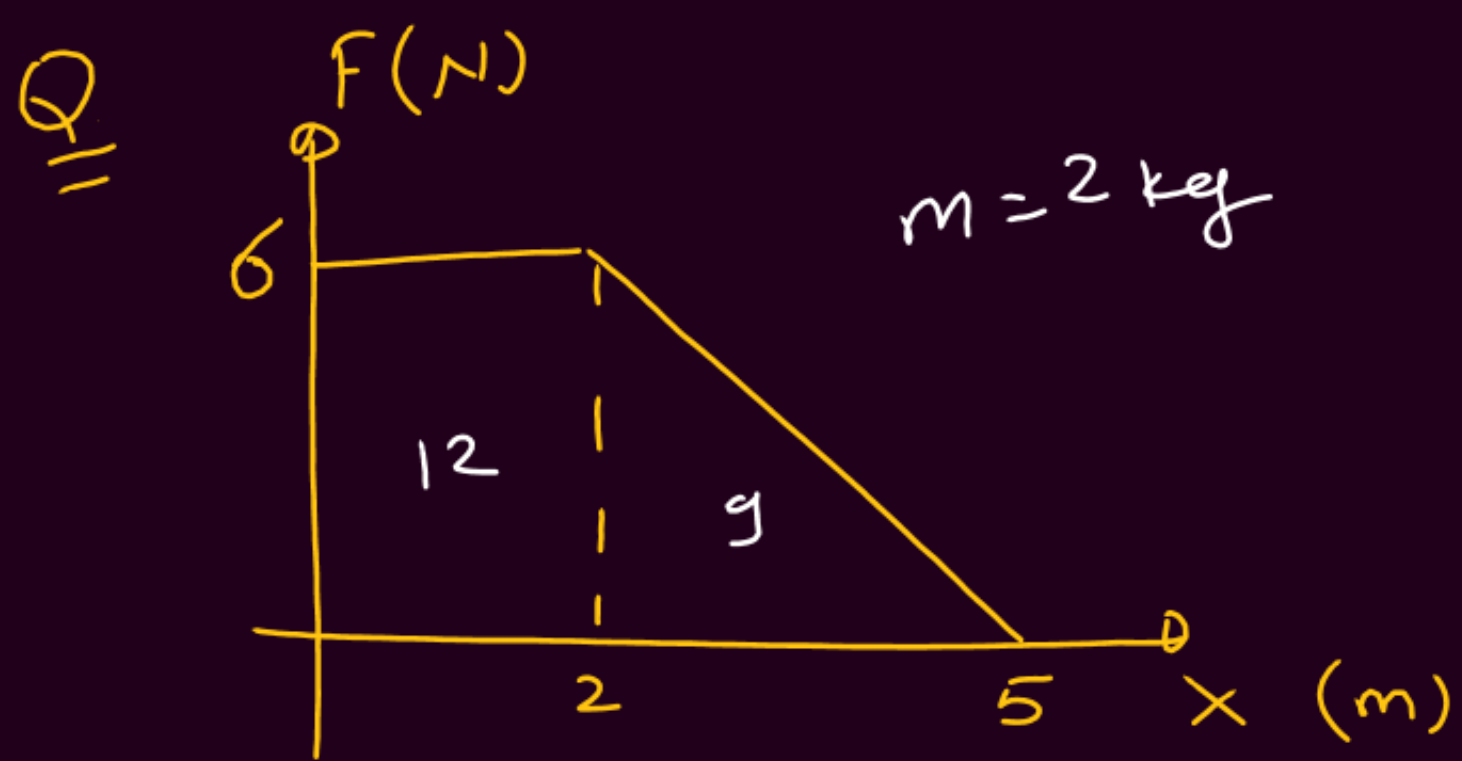
$$W = \frac{1}{2} (2) (1^2 - 0^2) = \underline{\underline{1 \text{ J}}}$$



W.D. in 5s?

$$W = \frac{1}{2} (2) (0^2 - 6^2)$$

$$W = \underline{\underline{-36 \text{ J}}}$$



If initial sp. is 10 m/s
then find v at 5s?

$$W = \frac{1}{2} (2) (v^2 - 10^2)$$

$$21 = v^2 - 100$$

$$v^2 = 121$$

$$v = 11 \text{ m/s}$$

Conservation of ME

① $ME = PE + KE$

② $W_c + W_{\text{others}} = \Delta K$

$$-\Delta U + W_{\text{others}} = \Delta K$$

$$W_{\text{others}} = \Delta K + \Delta U = \Delta ME$$

③ If $ME = \text{const.}$

$$U_i + K_i = U_f + K_f$$

① Drop

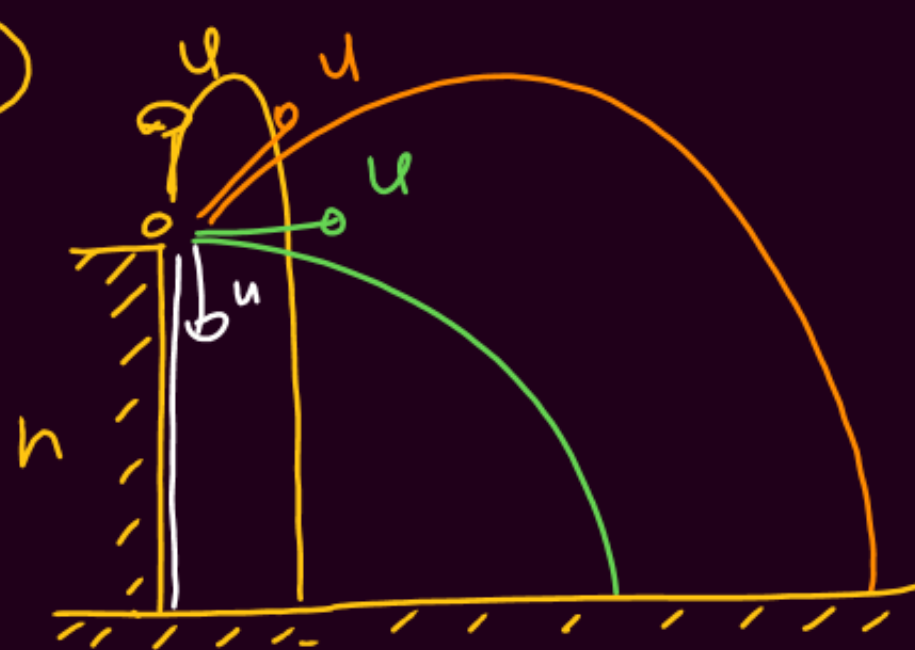


$$U_i + K_i = U_f + K_f$$

$$mgh + 0 = 0 + \frac{1}{2}mv^2$$

$$v^2 = 2gh$$

②

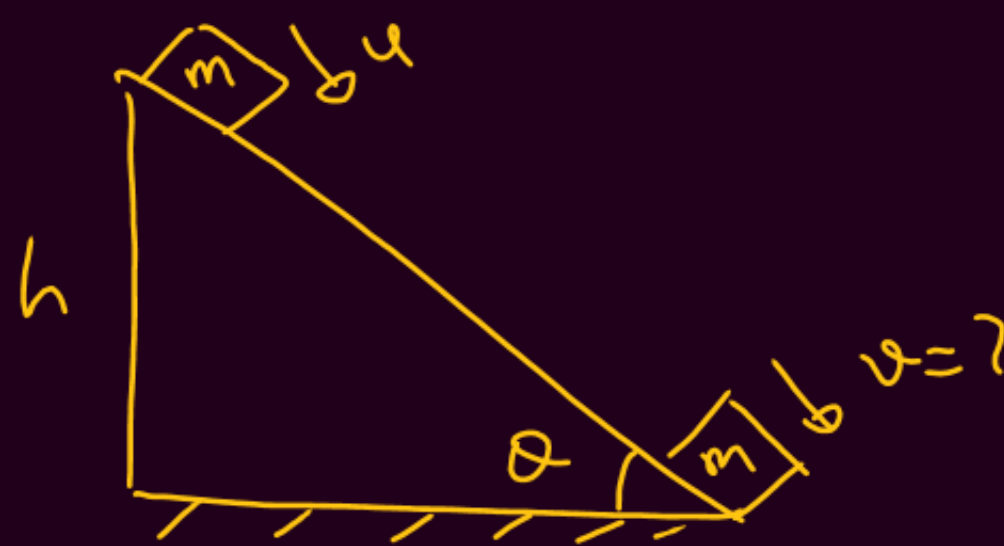


$$U_i + K_i = U_f + K_f$$

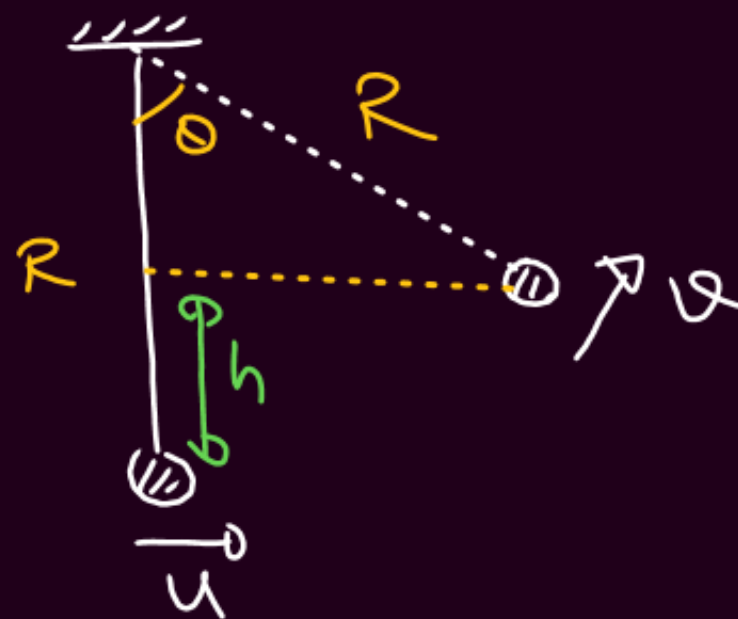
$$mgh + \frac{1}{2}mu^2 = 0 + \frac{1}{2}mv^2$$

$$v^2 = u^2 + 2gh$$

Irrespective of Angle of Projection



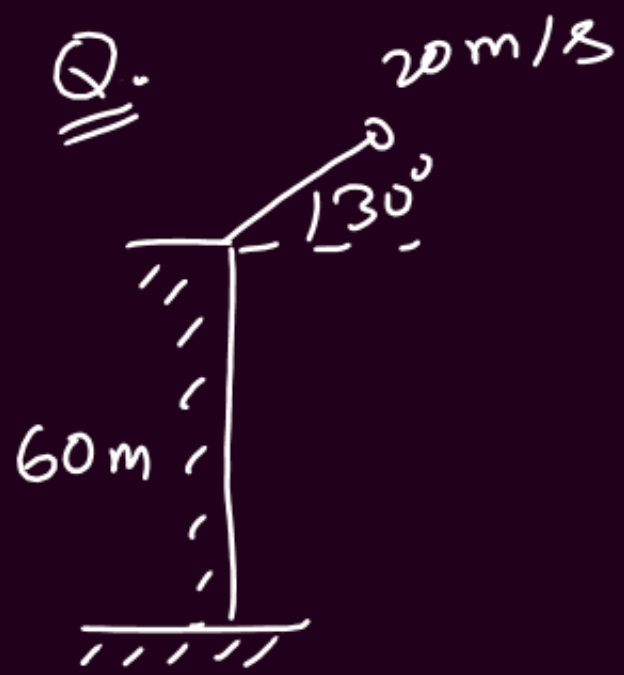
$$\omega_N = 0$$



$$① h = R(1 - \cos\theta)$$

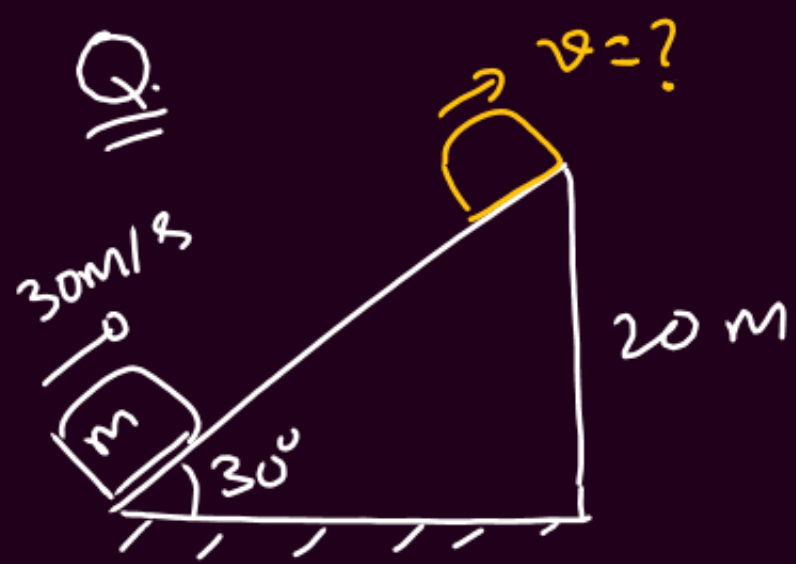
$$② \omega_T = 0$$

$$③ v^2 = u^2 - 2gh$$



$$v^2 = 20^2 + 2(10)(60)$$

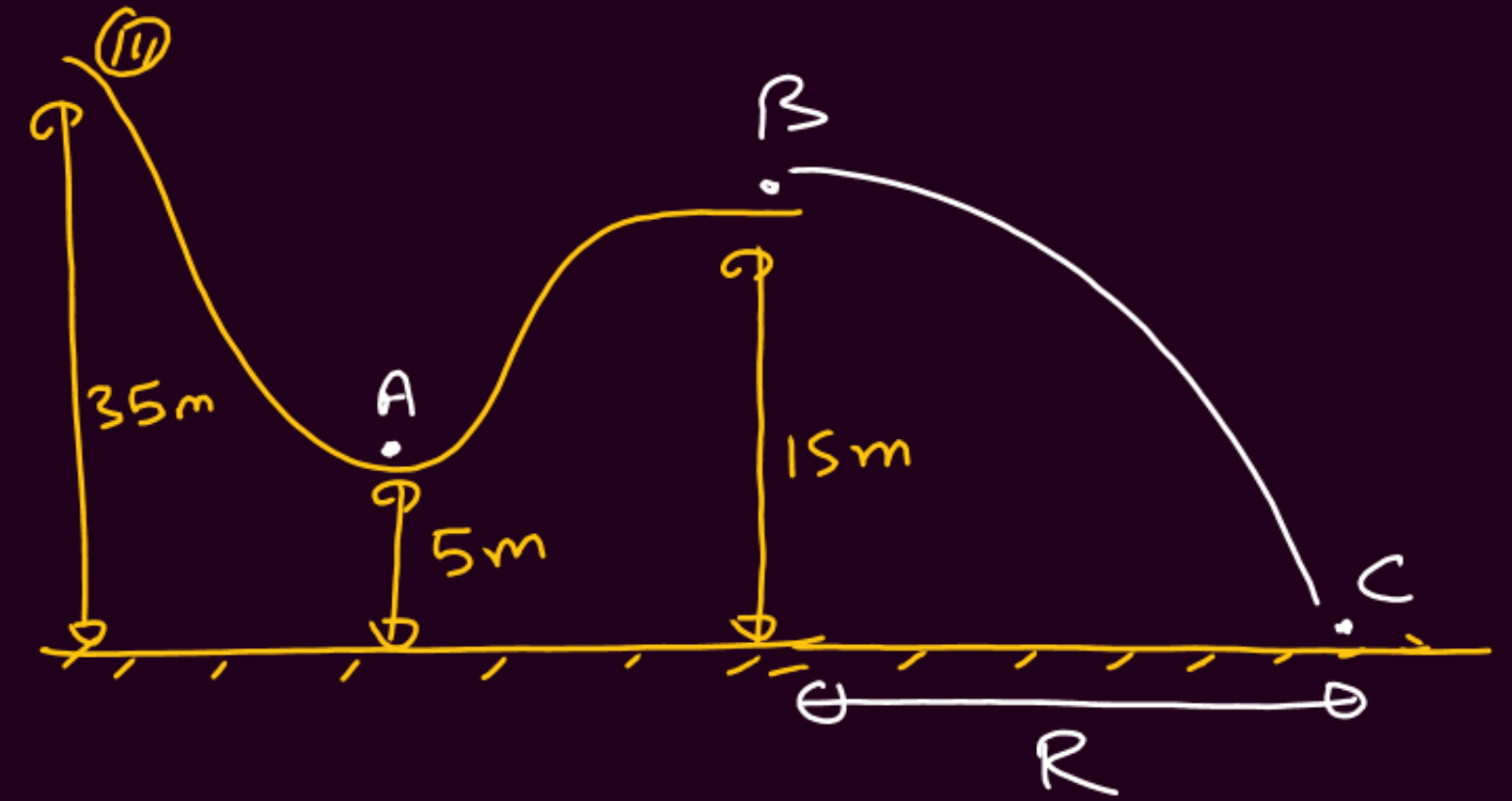
$$v = 40 \text{ m/s}$$



$$v^2 = (30)^2 - 2(10)(20)$$

$$v = 10\sqrt{5} \text{ m/s}$$

Q. Rest



$$\textcircled{1} v_A = \sqrt{2(10)(30)} = 10\sqrt{6} \text{ m/s}$$

$$\textcircled{2} v_B = \sqrt{2(10)(20)} = 20 \text{ m/s}$$

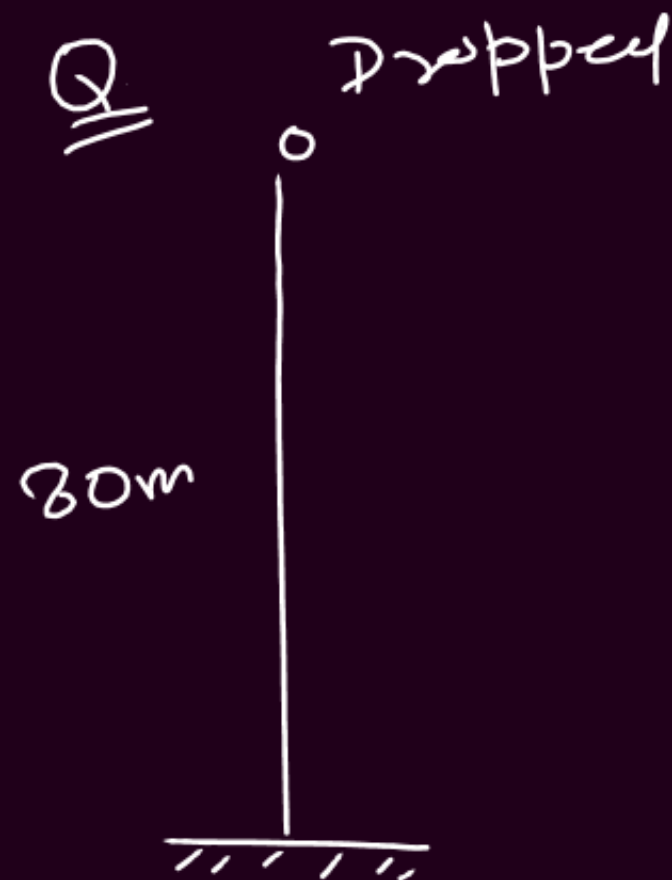
$$\textcircled{3} v_C = \sqrt{2(10)(35)} = 10\sqrt{7} \text{ m/s}$$

$$\textcircled{4} R = u \sqrt{\frac{2H}{g}} = (20) \sqrt{\frac{2 \times 15}{10}} = 20\sqrt{3} \text{ m}$$



$$\frac{KE}{PE} = \frac{H-h}{h}$$

$$\frac{KE}{PE} = \frac{mg(H-h)}{mgh}$$



① at 30m $\frac{KE}{PE} = \frac{50}{30} = \frac{5}{3}$

② Height $KE = 2(PE)$

$$\frac{KE}{PE} = \frac{2}{1} = \frac{80-h}{h}$$

$$h = \frac{80}{3} \text{ m}$$

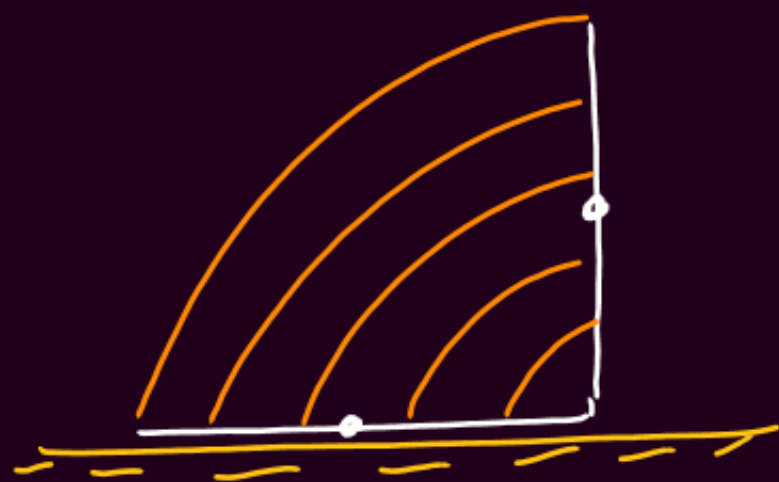
② Height

$$2(KE) = 3(PE)$$

$$\frac{KE}{PE} = \frac{3}{2} = \frac{80-h}{h}$$

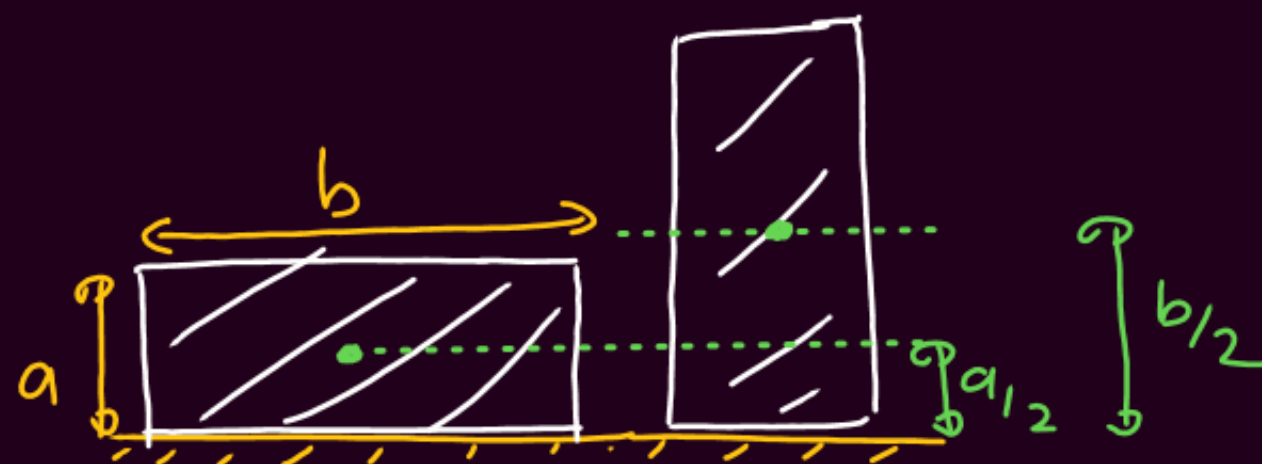
$$h = 32 \text{ m}$$

Rope / chain / Rod (Center of mass)



"Horizontal" $\longleftrightarrow$ "Vertical"

$$W = mg \frac{l}{2}$$



$$W = mg \left(\frac{b}{2} - \frac{a}{2} \right)$$

n -identical cubes (m, l)



$$W = (nm) g \left(\frac{nl}{2} - \frac{l}{2} \right)$$

$$W = \frac{n(n-1)}{2} mgl$$

W.D.



$$W = \frac{mgl}{2n^2}$$

Q $\frac{1}{3}$ rd part Hanging



$$\frac{l}{n} = \frac{l}{3}$$

$$n = 3$$

$$W = \frac{mgl}{2(3)^2} = \frac{mgl}{18}$$

Q $\frac{2}{3}$ rd part is Hanging



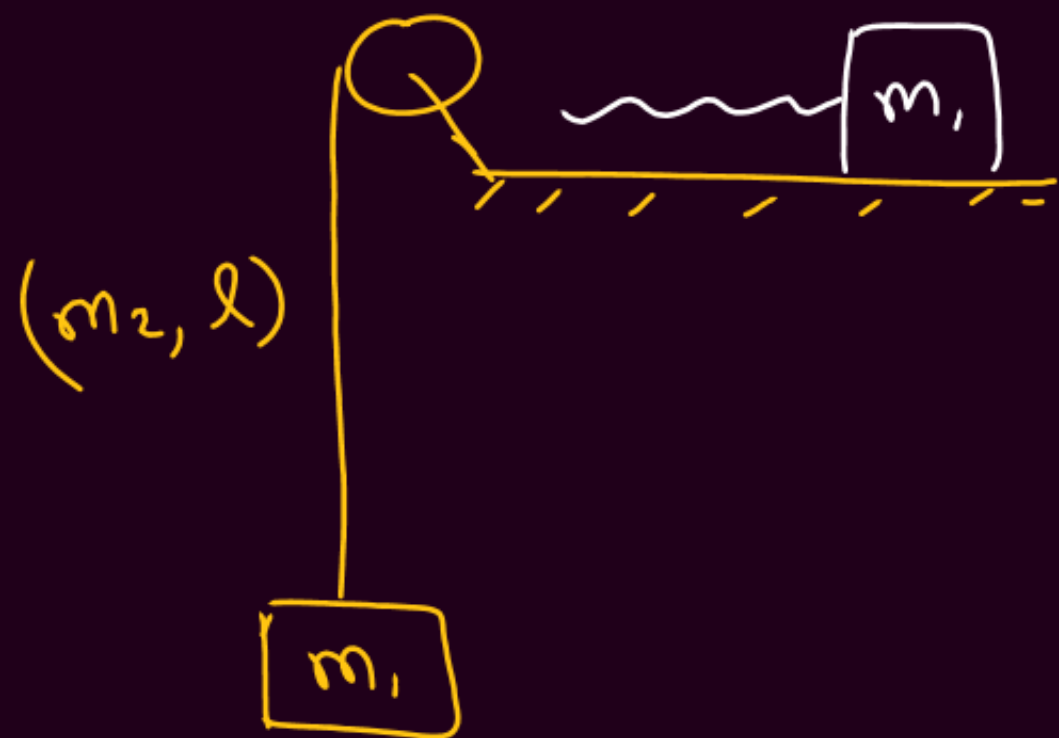
$$\frac{l}{n} = \frac{2l}{3}$$

$$n = \frac{3}{2}$$

$$W = \frac{mgl}{2(3/2)^2}$$

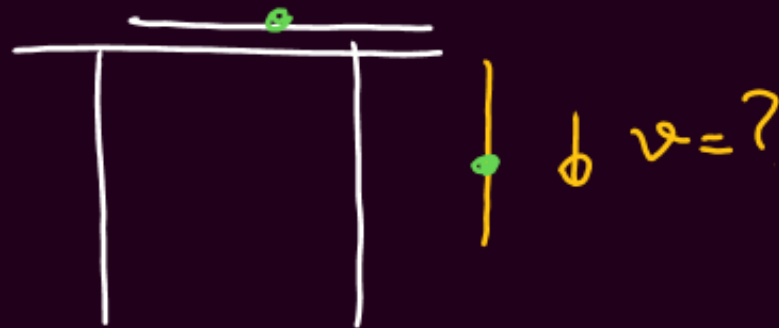
$$W = \frac{2mgl}{9}$$

Bucket & Rope



$$W = m_1 g l + m_2 g \frac{l}{2}$$

Q



$$U_i + K_i = U_f + K_f$$

$$mg \frac{l}{2} + 0 = 0 + \frac{1}{2} m v^2$$

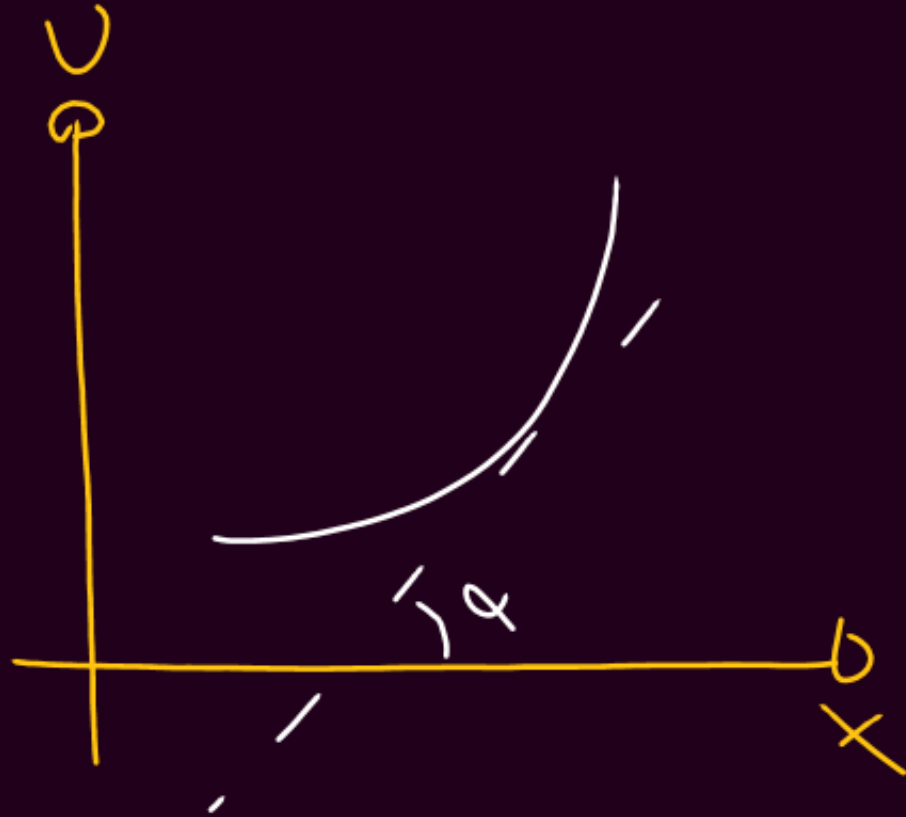
$$mg \frac{l}{2} = \frac{1}{2} m v^2$$

$$v = \sqrt{gl}$$

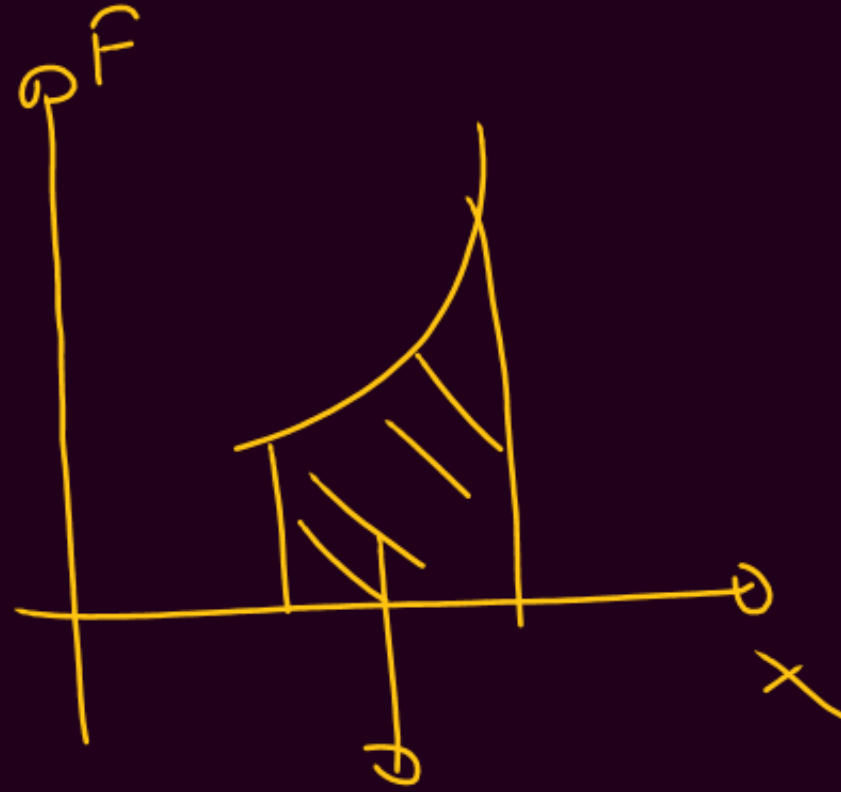
Relation betⁿ F & U

1D

$$F = - \frac{dU}{dx}$$



$$F = - (\text{slope})$$



$$W = (\text{Area})$$

$$\Delta U = - (\text{Area})$$

Q $U = (3x^2 - 2x + 1) \text{ J}$

F at $x = 2\text{m}$

$$\frac{dU}{dx} = 6x - 2$$

$$= 6(2) - 2$$

$$\frac{dU}{dx} = 10$$

$$F = -10\text{N}$$

Q $U = (x^2 - 4x + 3)$

Find U in equilibrium?

① $F = 0$

$$\frac{dU}{dx} = 0$$

$$2x - 4 = 0$$

$$x = 2\text{m}$$

② $U = (2)^2 - 4(2) + 3$

$$\underline{U = -1\text{J}}$$

$$Q = U = \frac{a}{r^6} - \frac{b}{r^{12}}$$

PE in Equilibrium?

$$U = a(r^{-6}) - b(r^{-12})$$

$$\frac{dU}{dr} = a(-6r^{-7}) - b(-12r^{-13})$$

$$0 = -6ar^{-7} + 12br^{-13}$$

$$a = 2br^{-6}$$

$$\boxed{\frac{a}{2b} = \frac{1}{r^6}}$$

$$U = a\left(\frac{a}{2b}\right) - b\left(\frac{a}{2b}\right)^2$$

$$U = \frac{a^2}{2b} - \frac{a^2}{4b}$$

$$\boxed{U = \frac{a^2}{4b}}$$

$$\left\{ \begin{array}{l} U = \frac{a}{r} - \frac{b}{r^2} \\ U = \frac{a}{r^3} - \frac{b}{r^6} \\ U = \frac{a}{r^4} - \frac{b}{r^8} \end{array} \right.$$

3D $F_x = -\frac{\partial U}{\partial x}$

$$F_y = -\frac{\partial U}{\partial y}$$

$$F_z = -\frac{\partial U}{\partial z}$$

$$\vec{F} = F_x \hat{i} + F_y \hat{j} + F_z \hat{k}$$

Q $U = -3x^2yz$

$$\vec{F}(1, -1, 1) = ?$$

$$\frac{\partial U}{\partial x} = -6xyz = +6$$

$$\frac{\partial U}{\partial y} = -3x^2z = -3$$

$$\frac{\partial U}{\partial z} = -3x^2y = +3$$

$$\vec{F} = -6\hat{i} + 3\hat{j} - 3\hat{k}$$

$$F = 3\sqrt{6} \text{ N}$$

Q $U = x^2y - 3z + 4yz^2$

$\vec{F}(1, 0, -1) = ?$

$$\frac{\partial U}{\partial x} = 2xy = 0$$

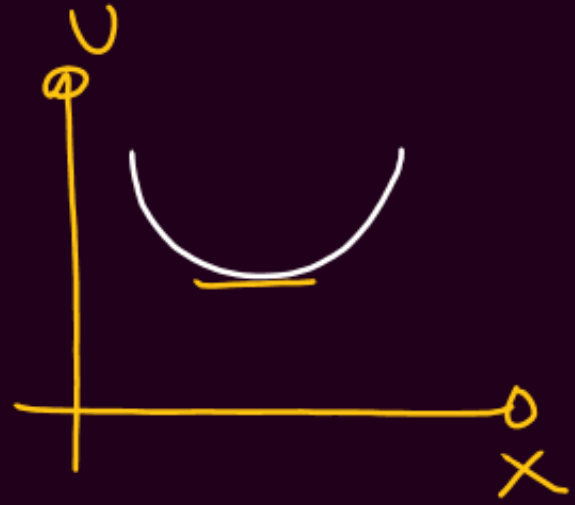
$$\frac{\partial U}{\partial y} = x^2 + 4z^2 = 1 + 4 = 5$$

$$\frac{\partial U}{\partial z} = -3 + 8yz = -3$$

$$\boxed{\vec{F} = (-5\hat{j} + 3\hat{k}) \text{ N}}$$

Types of Equilibrium

Stable



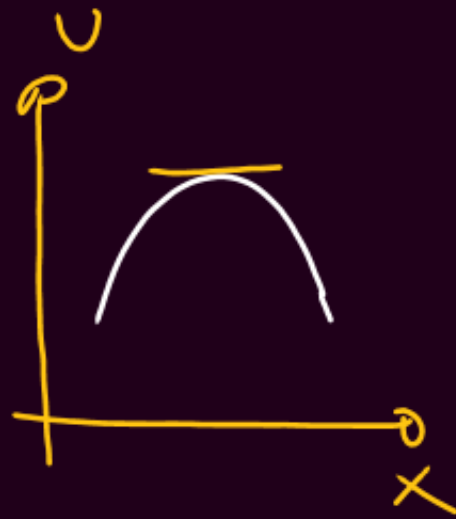
$$F = 0$$

$$\frac{dU}{dx} = 0$$

$$\frac{d^2U}{dx^2} > 0$$

(minima)

Unstable



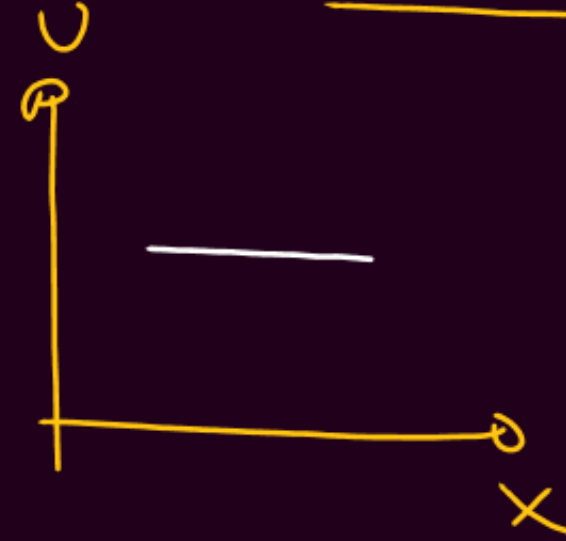
$$F = 0$$

$$\frac{dU}{dx} = 0$$

$$\frac{d^2U}{dx^2} < 0$$

(maxima)

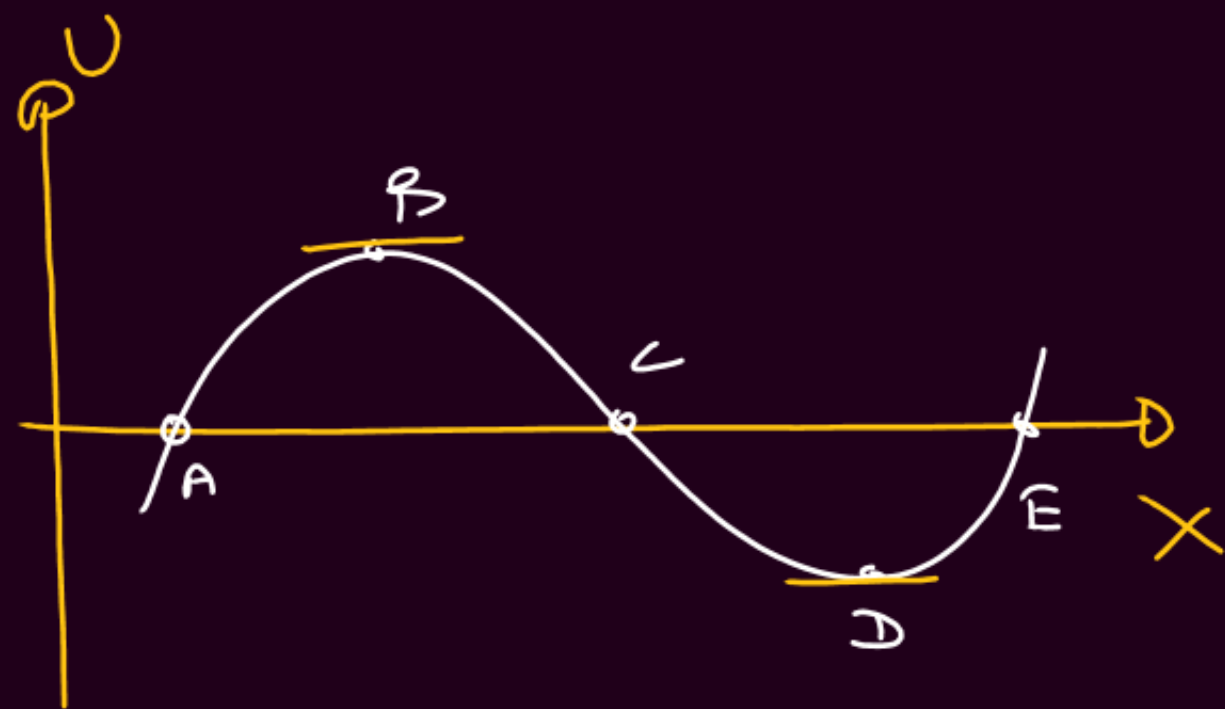
Neutral



$$F = 0$$

$$\frac{dU}{dx} = 0$$

$$\frac{d^2U}{dx^2} = 0$$



Equilibrium B, D

Stable D

Unstable B

Power

① Inst. Power

$$P_{\text{inst}} = \vec{F} \cdot \vec{v} = \frac{dW}{dt}$$

② Avg Power

$$P_{\text{av}} = \frac{W}{\Delta t}$$

Unit

$$W = \frac{J}{s}$$

$$1 \text{ hp} = 746 \text{ W}$$

Power

$$1 \text{ kWhr} = 3.6 \times 10^6 \text{ J}$$

Commercial unit of Energy

Net Power

$$P_{\text{inst}} = \vec{F}_{\text{net}} \cdot \vec{v} = \frac{dK}{dt}$$

$$P_{\text{av}} = \frac{W_{\text{by all}}}{\Delta t} = \frac{\Delta K}{\Delta t}$$

Q. $\vec{F} = (3\hat{i} - 4\hat{j} + 5\hat{k}) \text{ N}$
 $\vec{v} = (2\hat{i} + \hat{j} + 3\hat{k}) \text{ m/s}$

$P_{\text{inst}} = ?$

$$P = \vec{F} \cdot \vec{v}$$

$$P = 6 - 4 + 15$$

$$P = 17 \text{ W}$$

Q Rest const. force v_0 at t_0
mass m

① Power delivered at t

$$P = F v = m(a)(at) = m\left(\frac{v_0}{t_0}\right)^2 t$$

$$[v_0 = 0 + at_0]$$

② Power deliver in t

$$P = \frac{\Delta K}{\Delta t} = \frac{\frac{1}{2} m v^2}{t} = \frac{1}{2} m \frac{a^2 t^2}{t}$$

$$P = \frac{1}{2} m \left(\frac{v_0}{t_0}\right)^2 t$$

Pg-219
(45)

$$\begin{aligned} P_{av} &= \frac{W}{t} \\ &= \frac{\frac{1}{2}mv^2}{t} \\ &= \frac{\frac{1}{2}m(at)^2}{t} \\ &= \frac{1}{2}(ma)(at) \\ &= \frac{Fv}{2} \end{aligned}$$

(43)

$$f_r = 0.5 \text{ kgf / quintal}$$

$$1000 \text{ N} \rightarrow f = 5 \text{ N}$$

$$10^7 \text{ N} \rightarrow f = \frac{5}{10^3} \times 10^7$$

$$P = (5 \times 10^4) \left(36 \times \frac{5}{18} \right)$$

$$\begin{aligned} P &= 5 \times 10^5 \text{ W} \\ &= \underline{500 \text{ kW}} \end{aligned}$$

(48)



$$F - \mu mg = ma$$

$$F = (\mu mg + ma)$$

$$v = at$$

$$P = m(\mu g + a)at$$

Pg-192
(2)

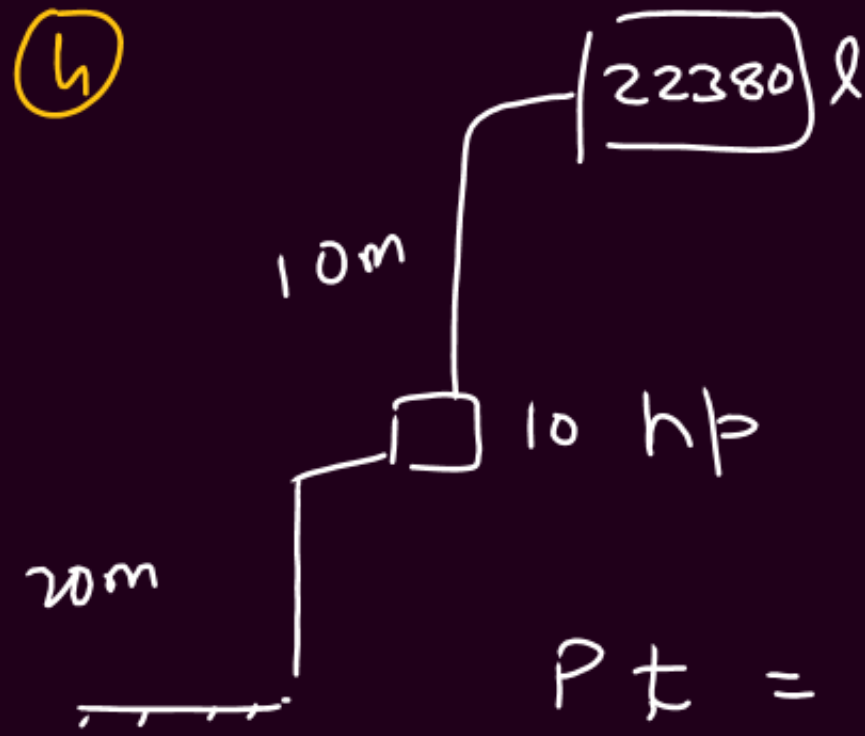
$$\frac{(12)(746)}{1000} \text{ kW}$$

$$\frac{(12)(746)}{1000} \times (8)(10) \text{ kWhr}$$

$$\frac{2.8 \times 10^3 \times 12 \times 750 \times 8 \times 10}{1000}$$

$$= 360$$

(4)



$$P_t = E = mgh$$

$$t = \frac{(22380)(10)(30)}{(10)(746)}$$

$$t = \frac{30 \times 30}{60} = 15 \text{ min}$$

(10)

Heart

$$\text{Power} = \frac{dW}{dt} = P \frac{dV}{dt}$$

$$\text{Power} = (20000)(10^{-6})$$

$$= 0.02 \text{ W}$$

Q $m = 2 \text{ kg}$

$$v = (2t^2 - 4t + 1) \text{ m/s}$$

① Power delivered in 3 s ?

$$P_{av} = \frac{\Delta K}{\Delta t} = \frac{\frac{1}{2} m (v^2 - u^2)}{\Delta t}$$

$$= \frac{2 (7^2 - 1^2)}{2 (3)} = 16 \text{ W}$$

$t = 0 \quad u = 1$

$t = 3 \quad v = 18 - 12 + 1 = 7$

② Power delivered at 3 s ?

$$\frac{dv}{dt} = a = (4t - 4)$$

$$P = F v = (2) (4 \times 3 - 4) (7)$$

$$\underline{P = 112 \text{ W}}$$

Case-1 $F = \text{const.}$

$$x \propto t^2$$

$$v \propto t$$

$$a \propto t^0$$

$$P \propto t$$

$$P = F v$$

$$P = F (at)$$

$$P = F \sqrt{2ax}$$

$$v \propto \sqrt{x}$$

$$a \propto x^0$$

$$P \propto \sqrt{x}$$

Case $P = \text{const}$

$$P = \frac{\Delta K}{\Delta t}$$

$$\boxed{\frac{1}{2} m (v^2 - u^2) = Pt}$$

Rest ($t=0$)

$$\frac{1}{2} m v^2 = Pt$$

$$\boxed{v = \sqrt{\frac{2Pt}{m}}}$$

$$x \propto t^{3/2}$$

$$v \propto t^{1/2}$$

$$a \propto t^{-1/2}$$

$$P = Fv$$

$$P = m \frac{dv}{dt} v$$

$$v^2 \propto t$$

$$v \propto x^{1/3}$$

$$a \propto x^{-1/3}$$

$$P = m \left(v \frac{dv}{dx} \right) v$$

$$v^3 \propto x$$

Water Jet



$$F = \rho A v^2$$

$$P = \rho A v^3$$

Motor

$$\textcircled{1} \text{ Power of motor} = \rho A v^3$$

$$\textcircled{2} \left(\text{Rate at which the KE is imparted} \right) = \frac{1}{2} \rho A v^3$$

$$\text{mass per unit length} = \rho A$$

Py-228
(2)

$$\begin{aligned} P &= (SA) v^3 \\ &= 100 (2)^3 \\ &= \underline{800 \text{ W}} \end{aligned}$$

(35)

$$P = \frac{mgh}{t} \left(\frac{90}{100} \right)$$

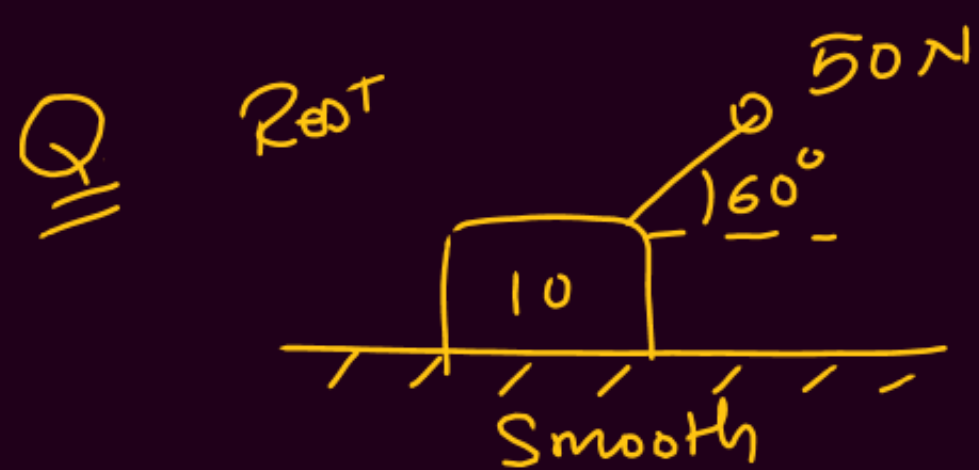
$$\begin{aligned} P &= 15 \times 10 \times (60) (0.9) \\ &= 8100 \text{ W} \\ &= 8.1 \text{ W} \end{aligned}$$

(26)

$$\begin{cases} \vec{F} = 2t \hat{i} + 3t^2 \hat{j} \\ \vec{a} = 2t \hat{i} + 3t^2 \hat{j} \\ \vec{v} = t^2 \hat{i} + t^3 \hat{j} \end{cases}$$

$$P = \vec{F} \cdot \vec{v}$$

$$P = (2t^3 + 3t^5) \text{ W}$$



Power delivered by force
at 2s?

$$\textcircled{1} \quad a = \frac{25}{10} = 2.5 \text{ m/s}^2$$

$$\textcircled{2} \quad v = at = (2.5)(2) = 5 \text{ m/s}$$

$$P = \vec{F} \cdot \vec{v}$$

$$P = F v \cos \theta$$

$$P = (50)(5) \cos 60^\circ$$

$$P = 125 \text{ W}$$